

# Terahertz diagnostic tool for sub-relativistic electron beams

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# Why use terahertz radiation for electron beam diagnostic?

## Advantages of THz Technology

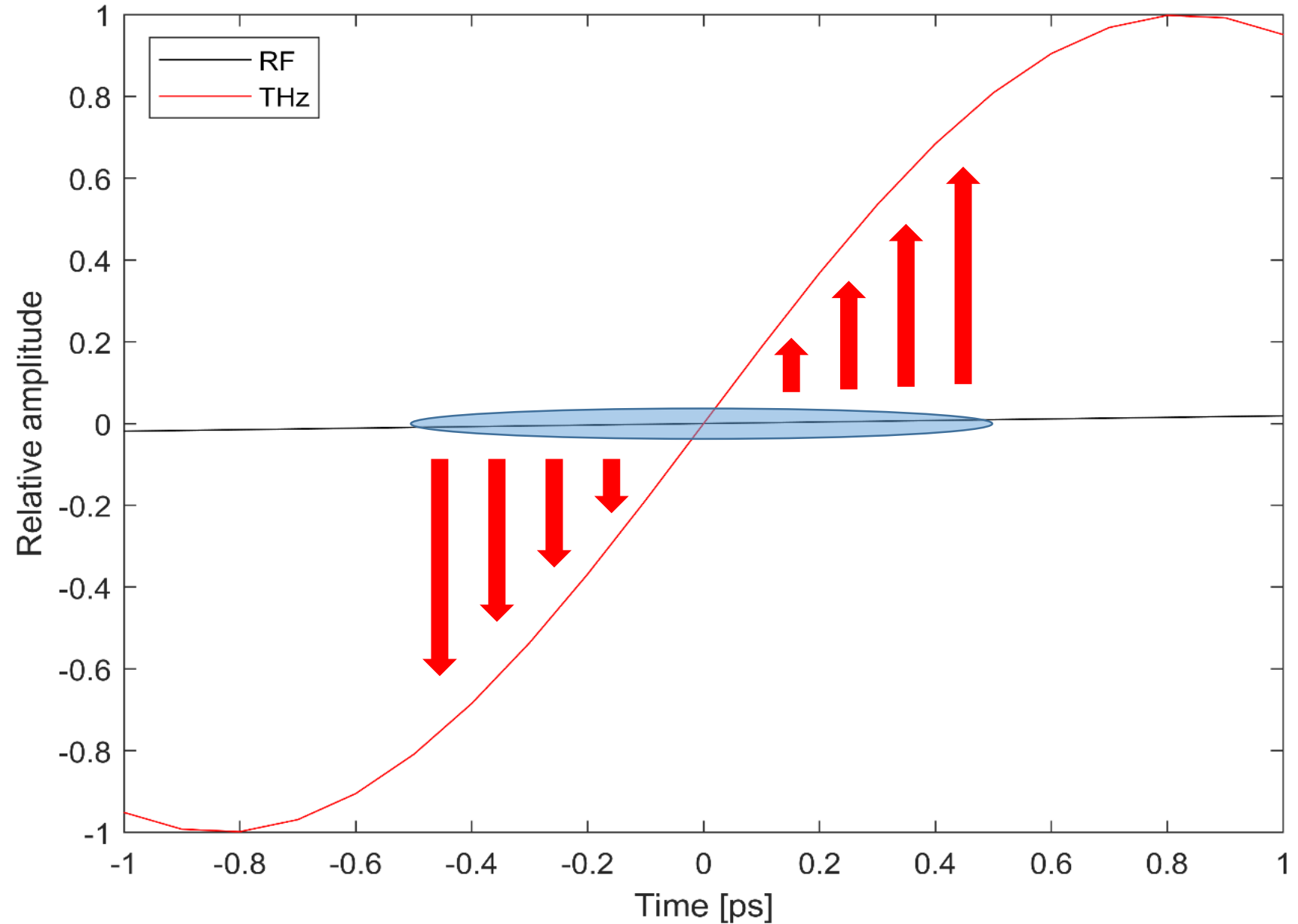
- Oscillation period well-matched to typical bunch duration allowing for fs resolution electron bunch diagnostics
- Inherent timing synchronisation and reduced timing system complexity
- High field strengths possible (100 MV/m to >GV/m)

## Radio Frequency Limitations

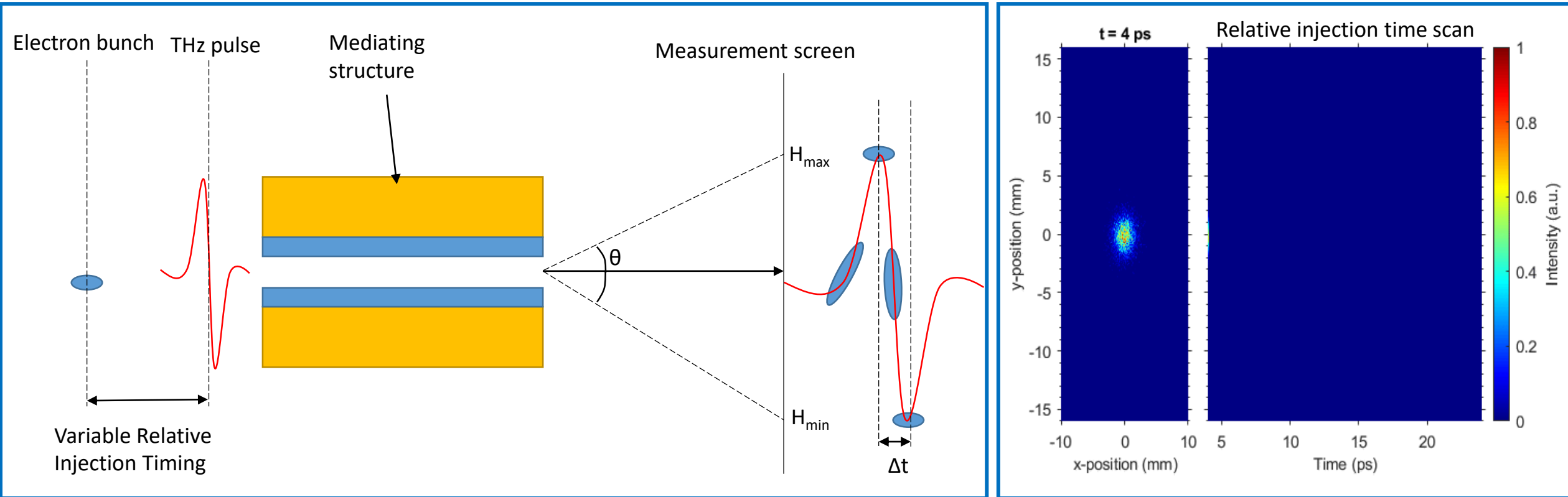
- Complicated timing systems
- Hard to achieve fs bunch diagnostics

## Diagnostics Uses

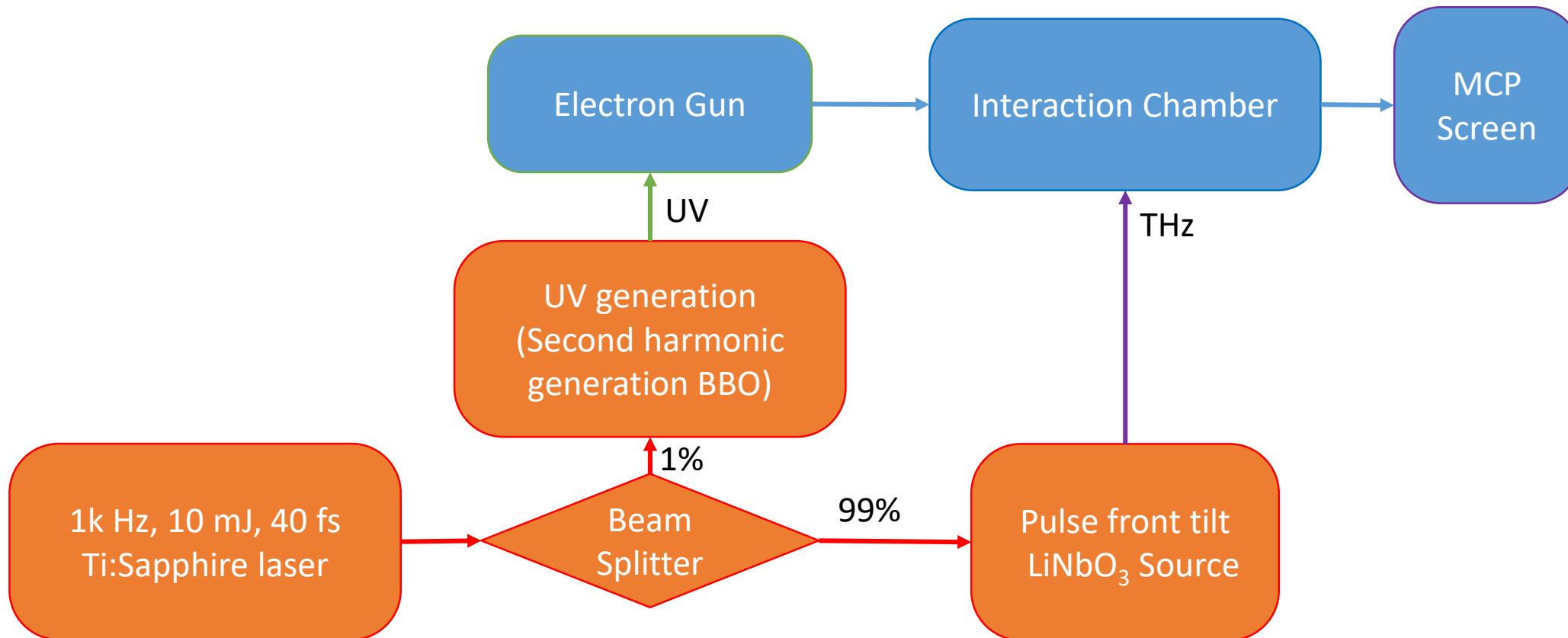
- Streaking to transfer longitudinal bunch information into measurable transverse change for ultrashort bunches



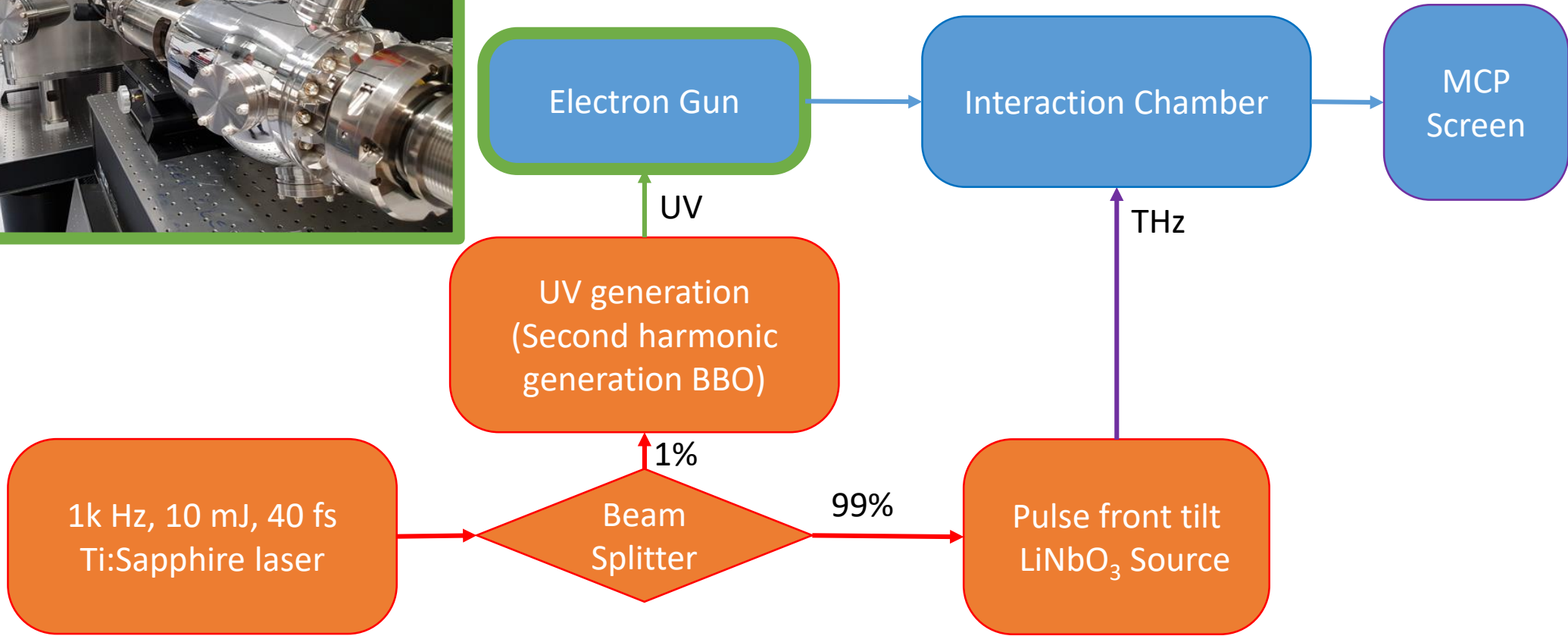
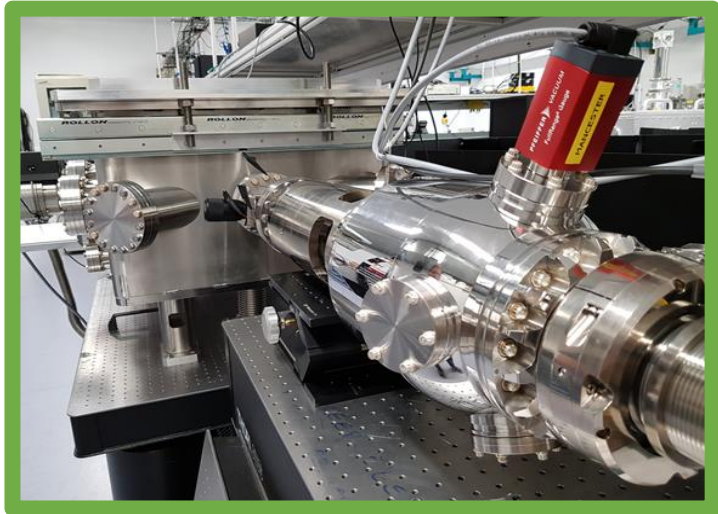
# Ultrafast Electron Diagnostics: Terahertz Deflectograms



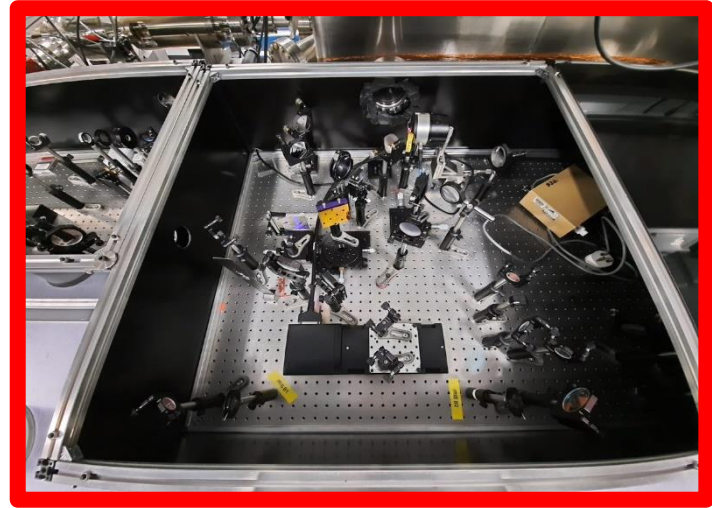
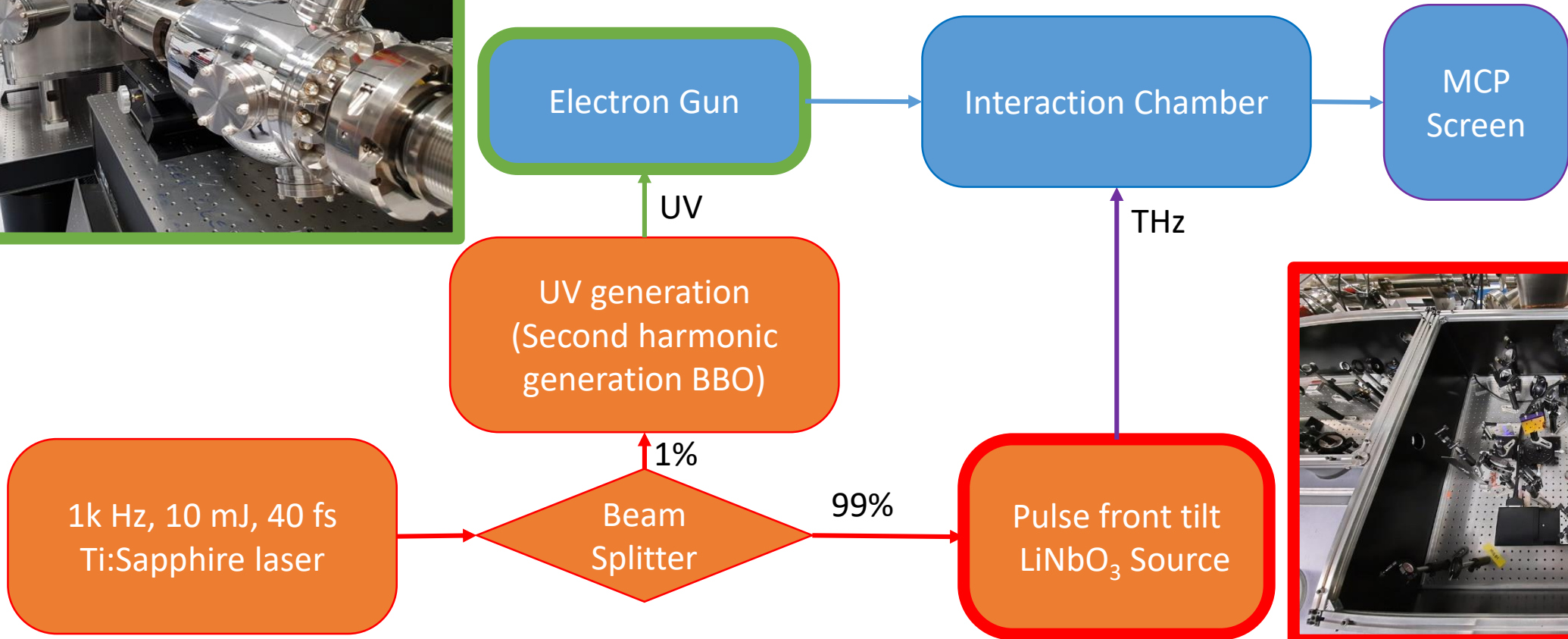
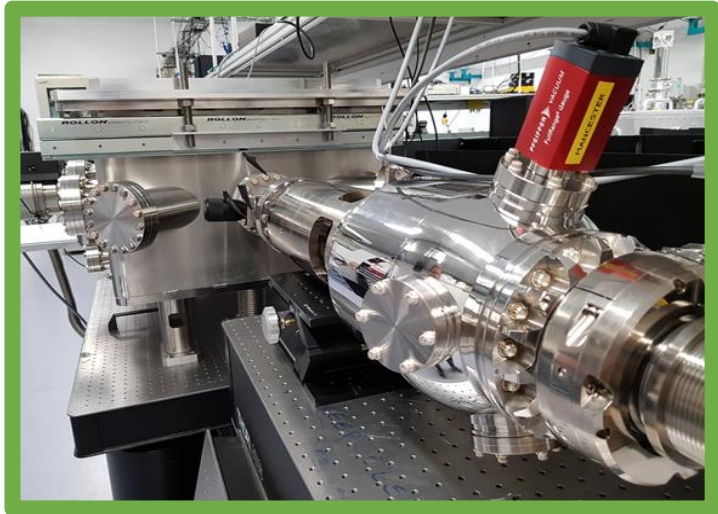
# 100 keV Sub-Relativistic Experimental Test Bed



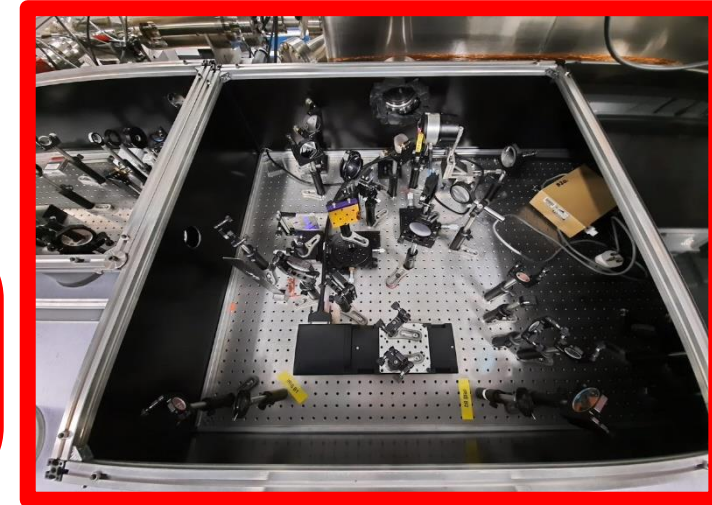
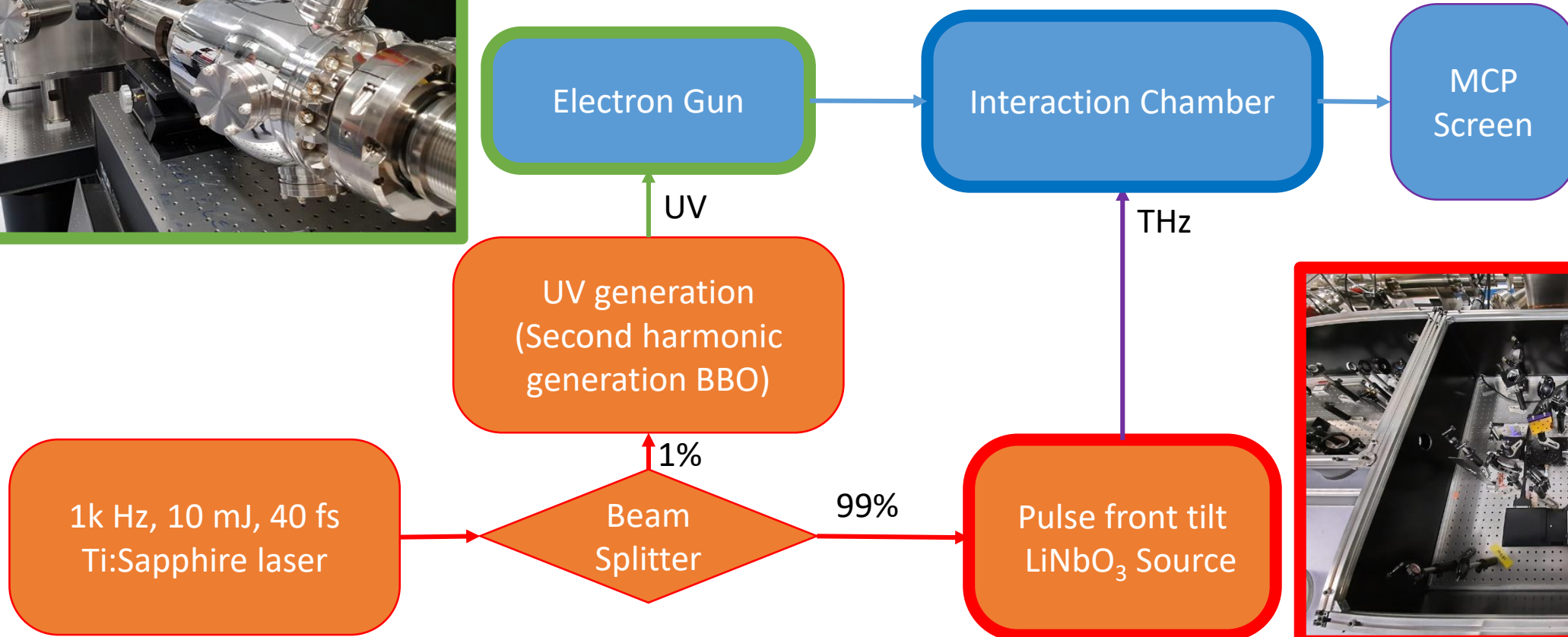
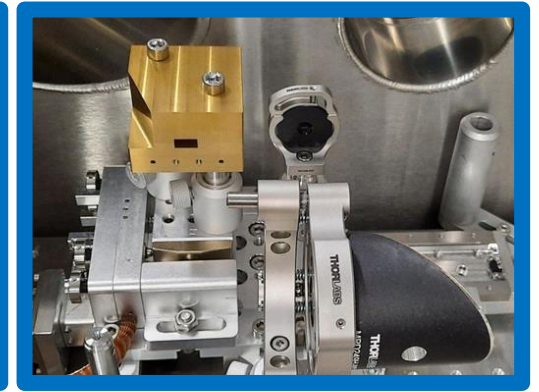
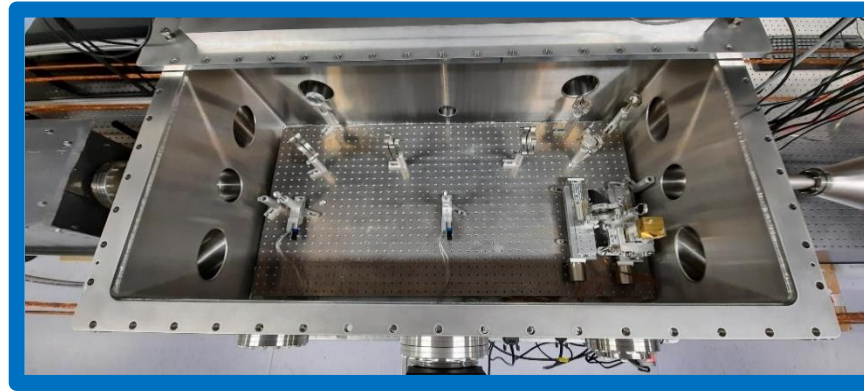
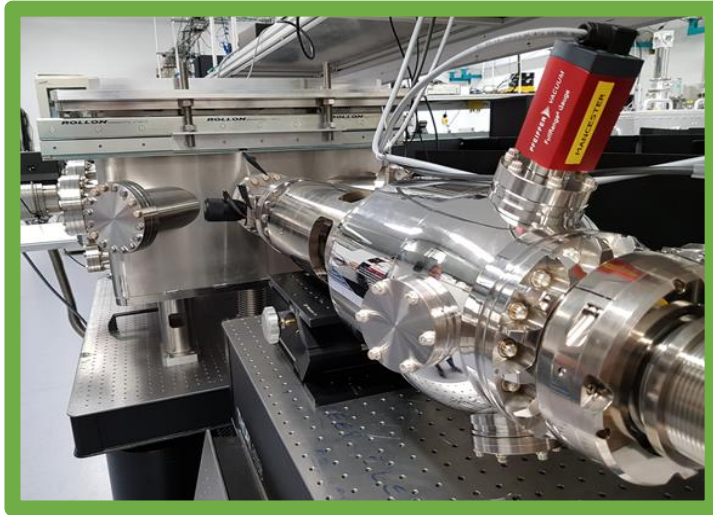
# 100 keV Sub-Relativistic Experimental Test Bed



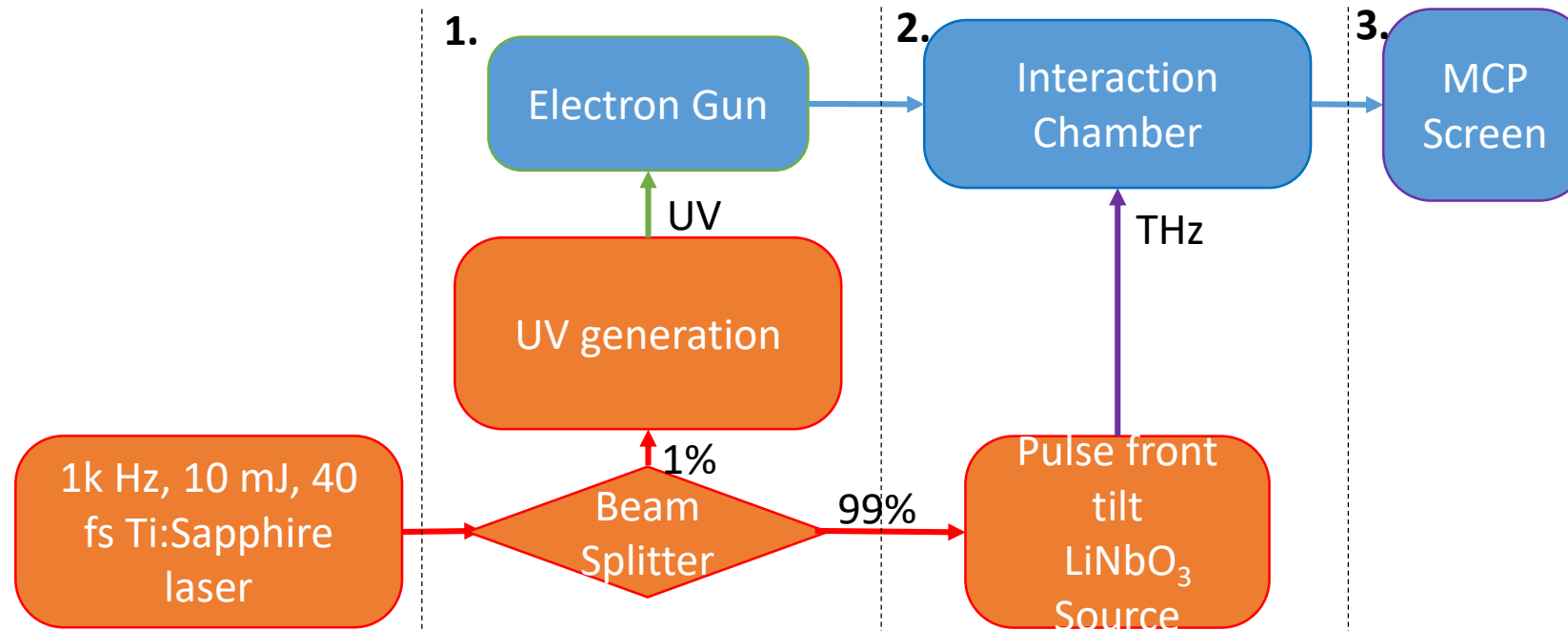
# 100 keV Sub-Relativistic Experimental Test Bed



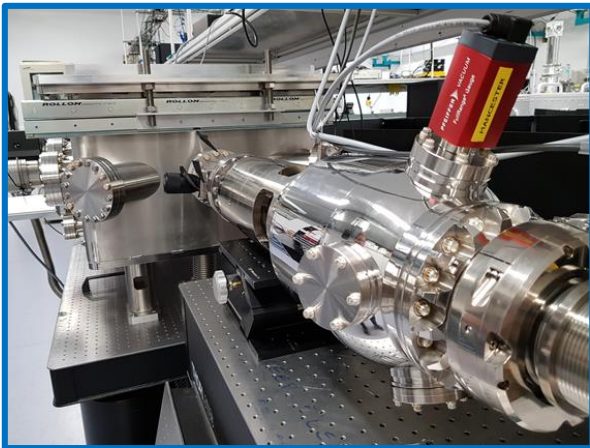
# 100 keV Sub-Relativistic Experimental Test Bed



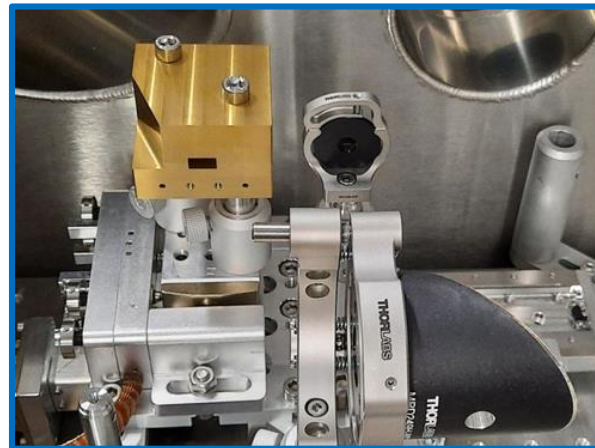
# 100 keV Simulation Development



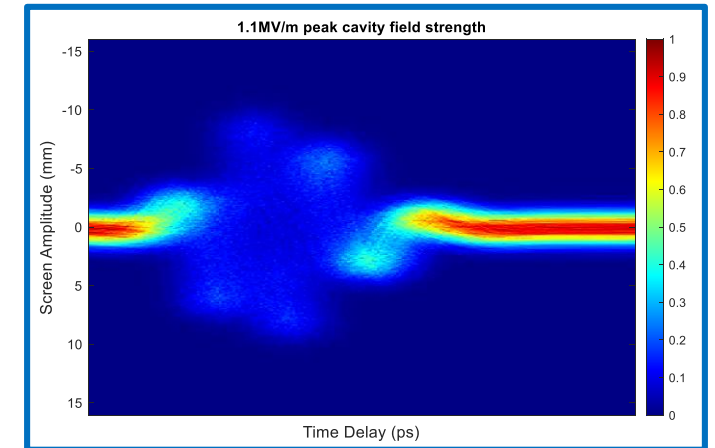
## 1. Electron gun modelling



## 2. Waveguide field simulations

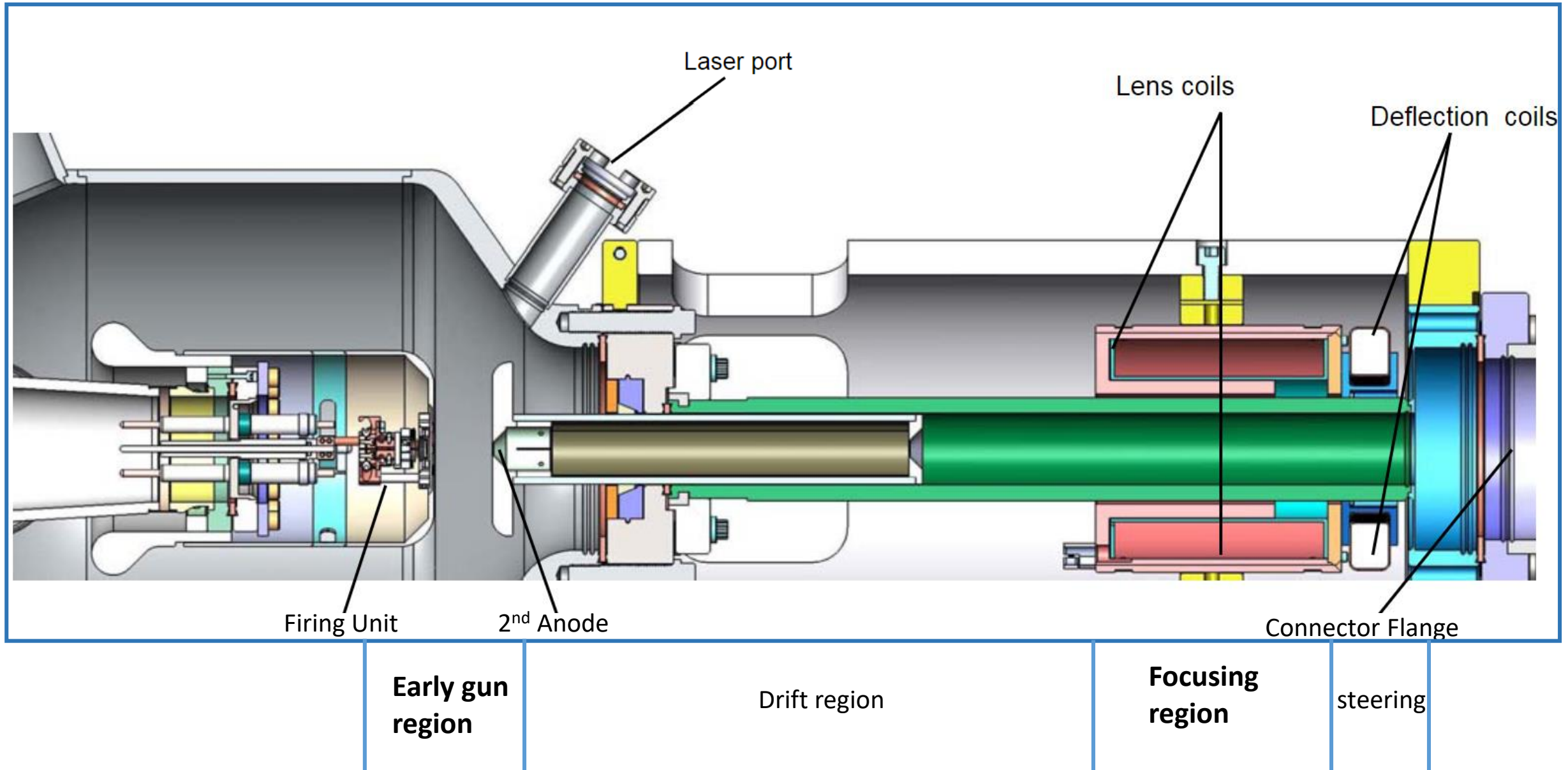


## 3. Experimental and Simulation Results

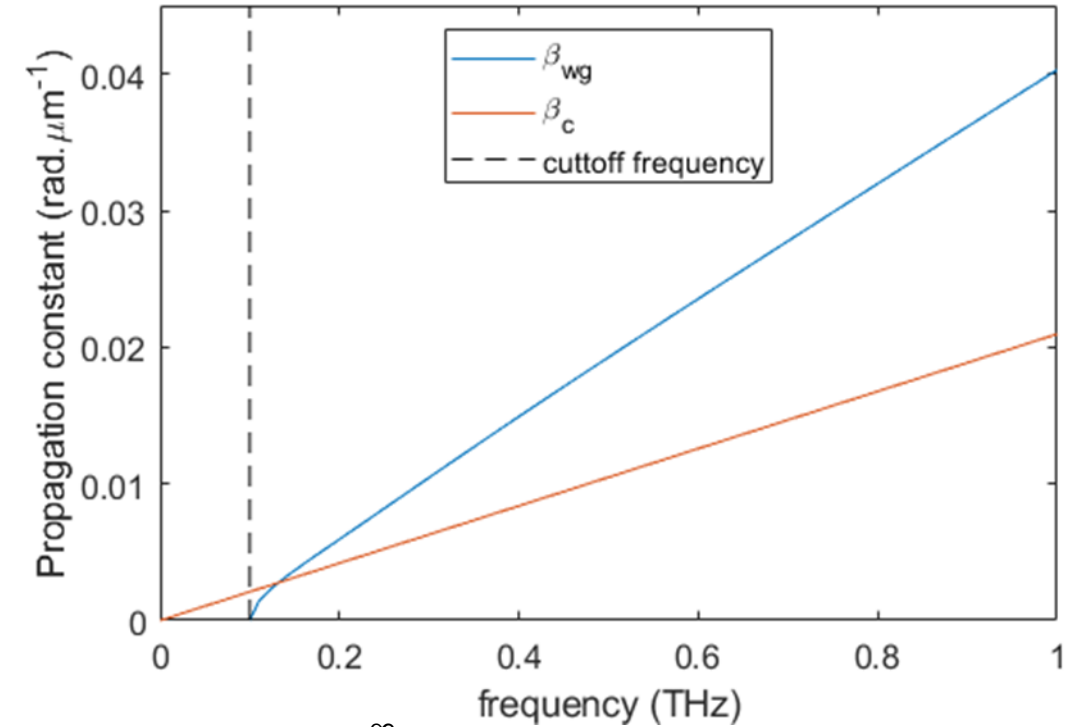
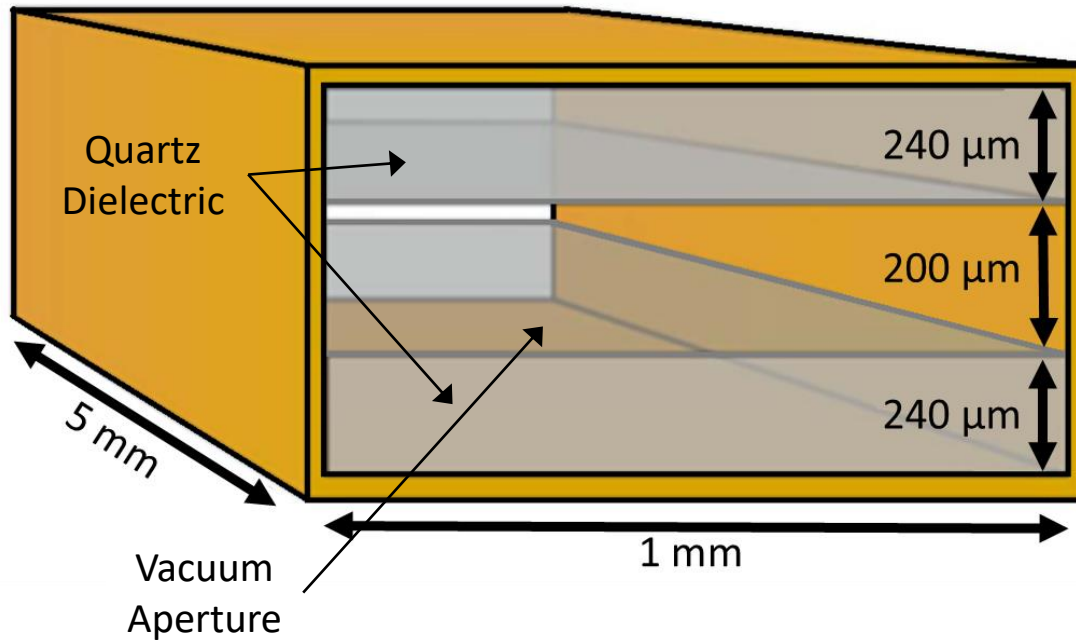




# Electron Gun Modelling



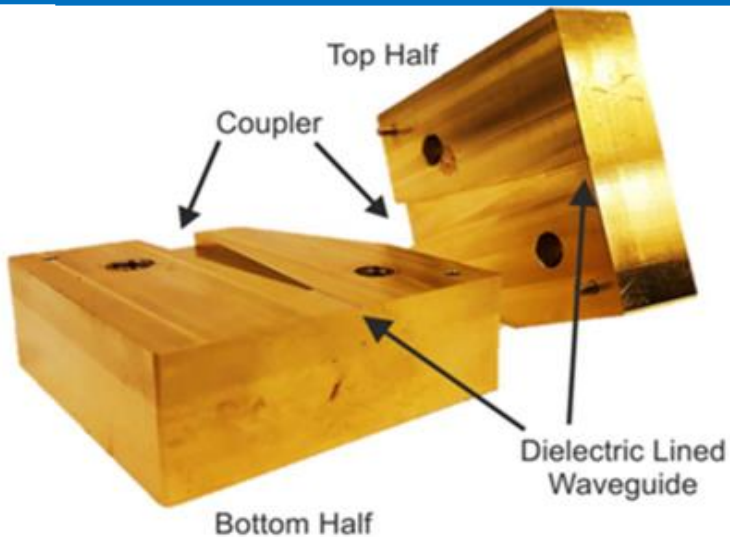
# Waveguide Simulation: Waveguide Features



$$\tilde{E}(t) = \int_{\omega_c}^{\infty} \tilde{A}(\omega) \exp[i\beta(\omega)z] \exp[-i\omega t] d\omega$$

V. Georgiadis, et al.  
Appl. Phys. Lett. **118**,  
144102 (2021)

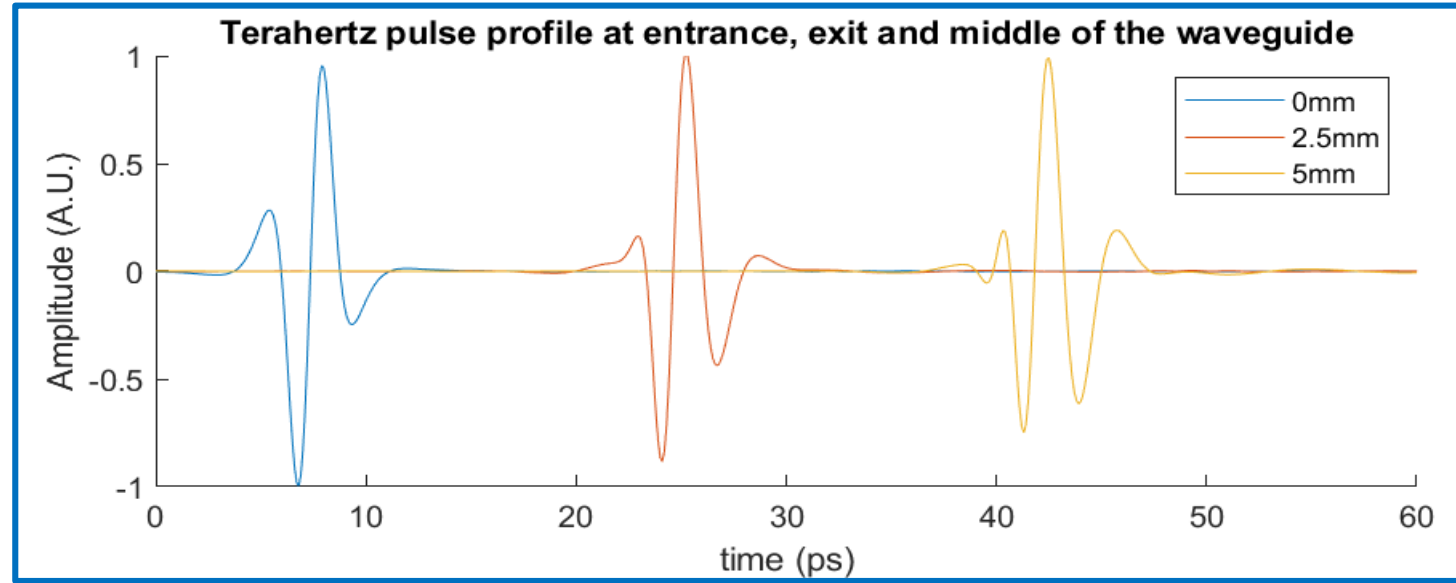
- 44 mm coupler used to transport  $\text{TE}_{10}$  mode THz pulse to waveguide
- $\text{LSM}_{01}$  mode waveguide structure is designed to match THz phase velocities with 100 keV electrons (0.548c) at frequency 0.47 THz
- Dispersion calculate for individual frequencies according to the  $\text{LSM}_{01}$  mode equations with boundaries defined by the waveguide dimensions



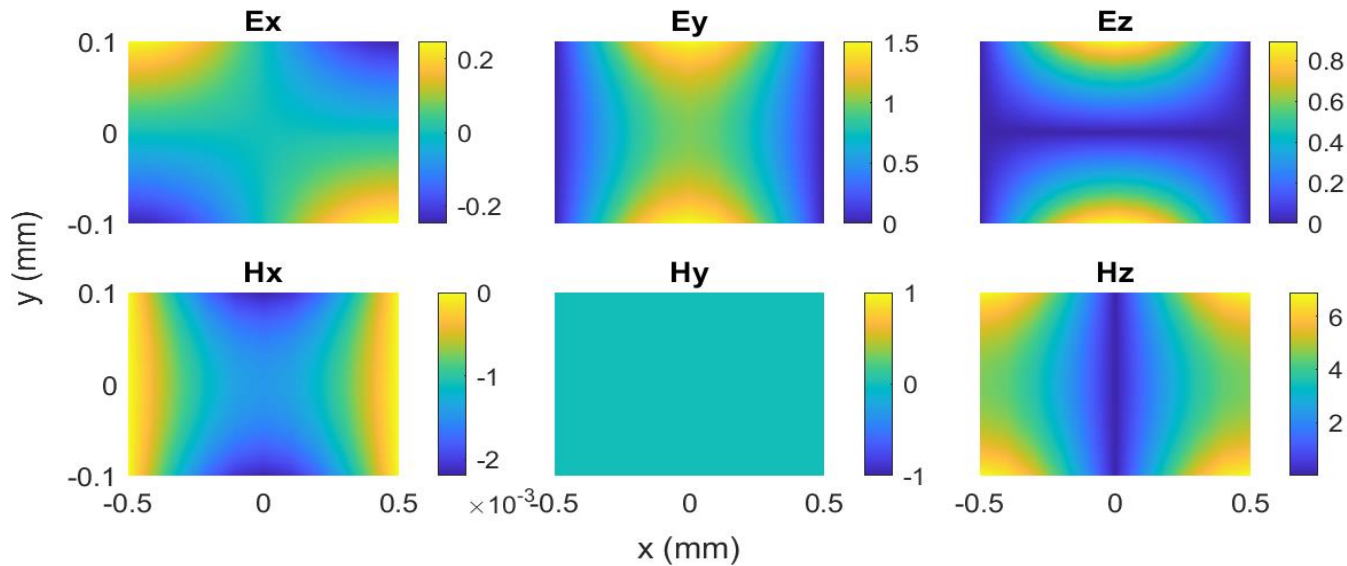
# Waveguide Simulation: Field Map Construction

$$\tilde{E}(t) = \int_{\omega_c}^{\infty} \tilde{A}(\omega) \exp[i\beta(\omega)z] \exp[-i\omega t] d\omega$$

- Phase advance calculate for individual frequencies according to the LSM<sub>01</sub> mode propagation constants
- Normalised longitudinal pulse profile calculated and recorded for each waveguide step in z



Waveguide Aperture Transverse Fields

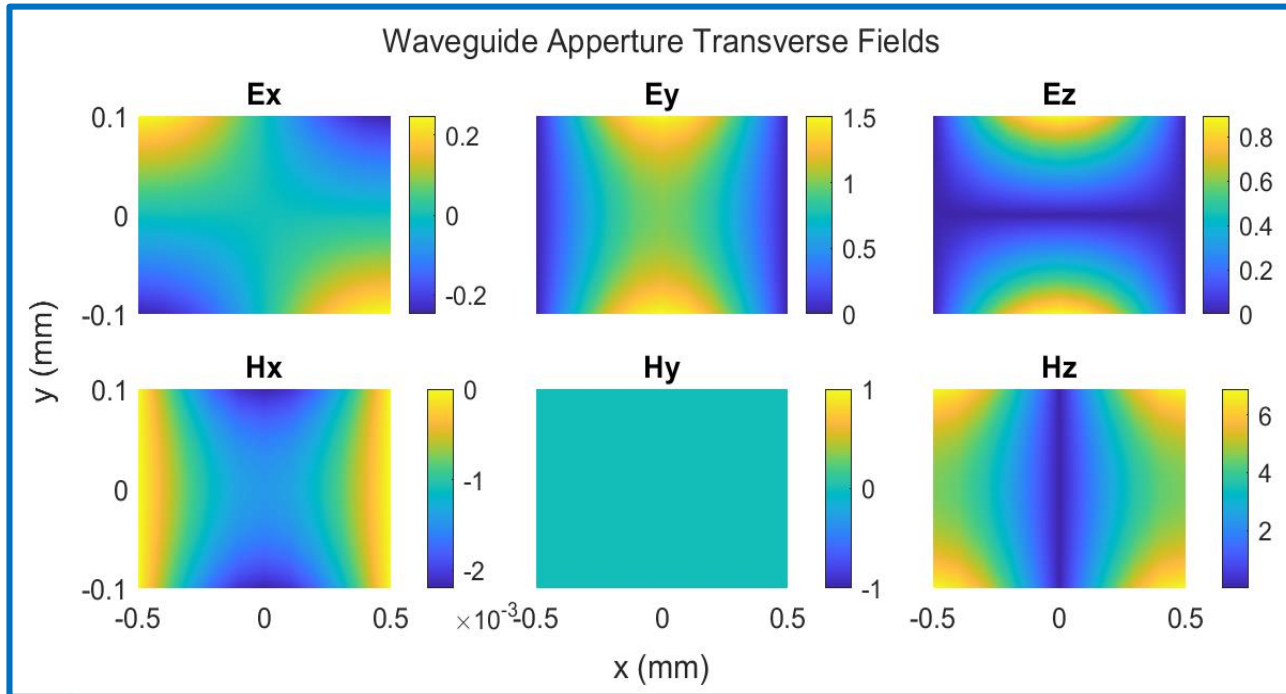


- Transverse THz field distribution calculated from the LSM<sub>01</sub> mode field equations
- All points normalised relative to on design axis Ey field
- Cartesian EM Field components stored as a 3D grid for each time step and scaled by a maximum field amplitude at the waveguide entrance

# Simulation Results

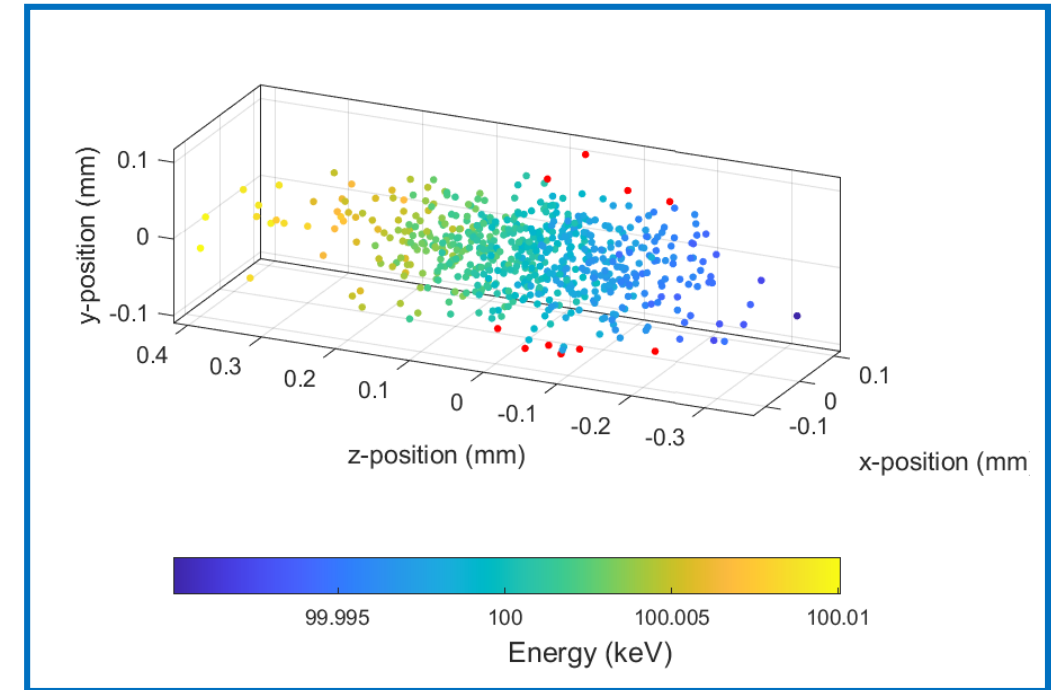
## Terahertz parameters in waveguide

- 0.33 THz central frequency
- 0.5 THz bandwidth ( $1/e^2$ )
- 1.1 MV/m induced peak field within the cavity



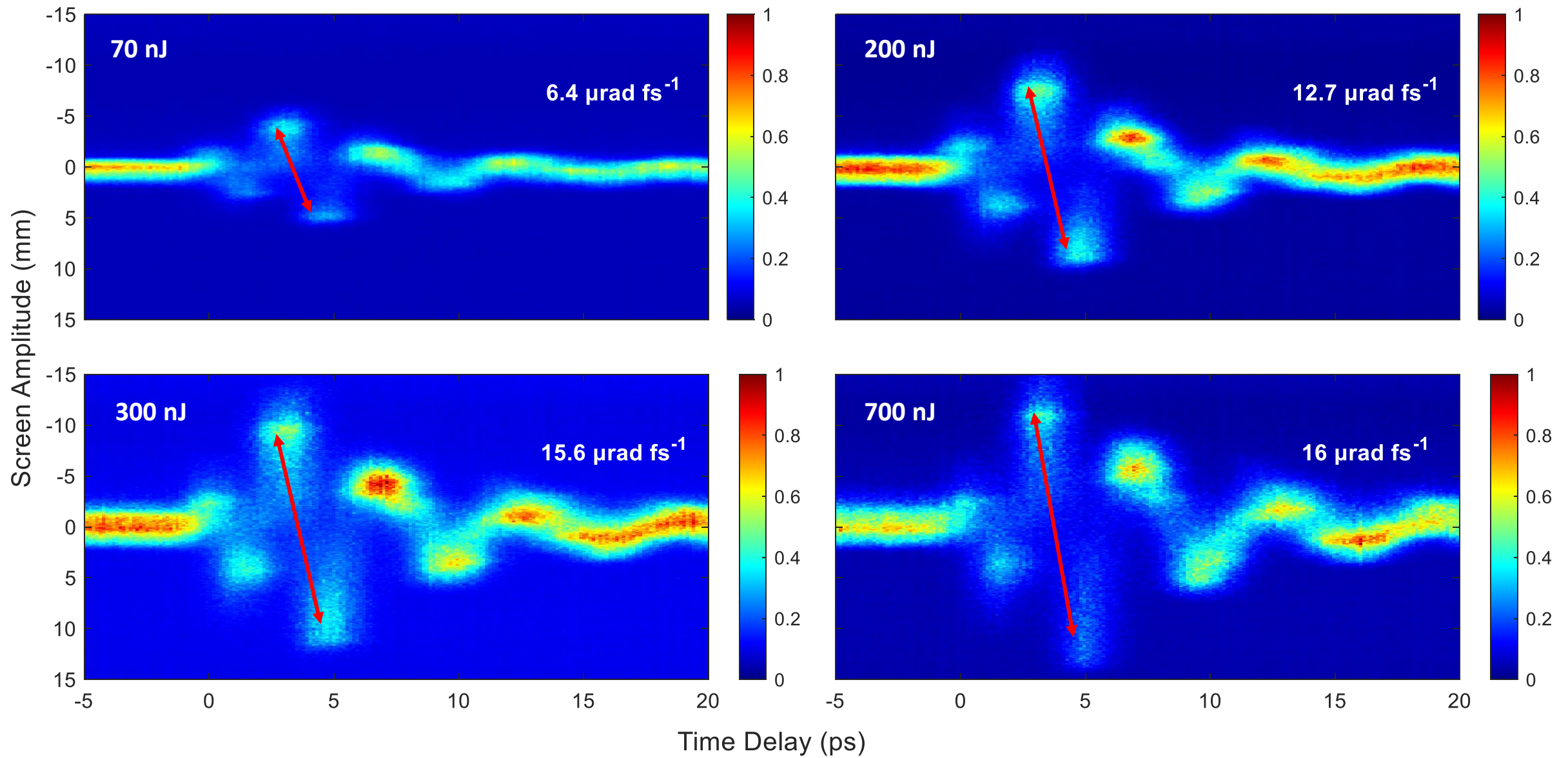
## Bunch Parameters at a waveguide focus :

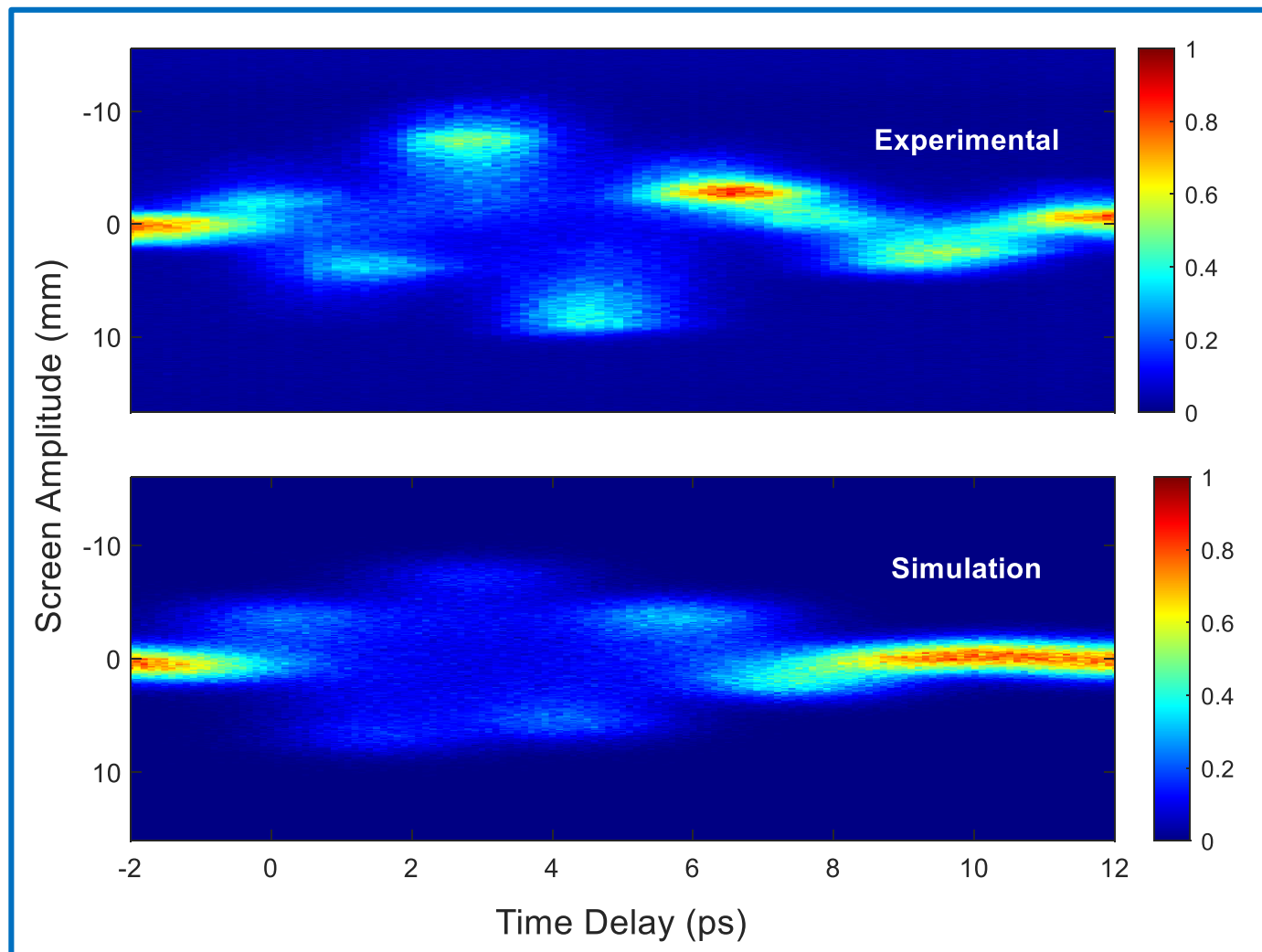
- 0.1 fC charge
- 240  $\mu\text{m}$  transverse diameter ( $1/e^2$ )
- 1.2 mrad divergence (RMS)
- 1.9 ps bunch duration (FWHM)



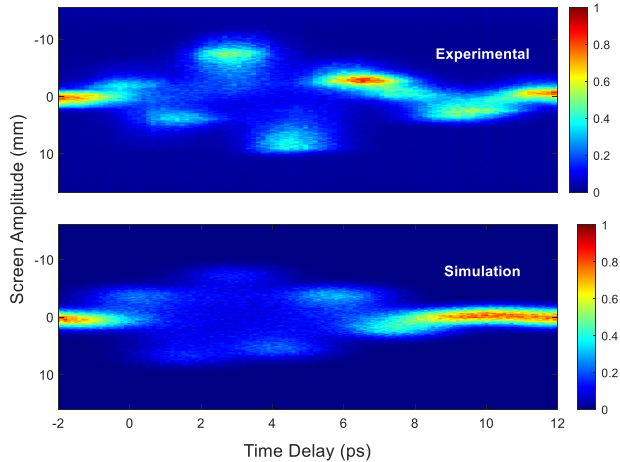
- Electrons stepped through generated field grid using Runge-Kutta 4<sup>th</sup> order in MATLAB simulation
- Electron bunches for each relative injection time transported to MCP screen by GPT simulation
- Y projections used to reconstruct final deflectogram

# Experimental Results





- 200 nJ case corresponds well to the 1.1 MV/m peak field simulation which agrees with calculated field estimates
- 240  $\mu\text{m}$  transverse diameter ( $1/e^2$ ) shows good match to lab results indicating a good charge match as primarily driven by space charge broadening vs solenoid focusing
- Divergence features show match to trends in experimental data with minimal clipping when matched to a 200nJ THz pulse energy
- Width of key peaks in lab measurements allows the bunch length to be determined as 1.9 ps FWHM as used in simulations
- Trailing oscillations in the lab measurement are attributed to coupler dispersion on the THz pulse – CST simulations to include coupler effects are currently in development



## Where we are:

- Electron gun simulations developed
- THz field map constructed from idealised  $\text{LSM}_{01}$  equations and EO measured pulse
- Successful matching of simulations with experimental results to analyse key features of the longitudinal electron bunch phase space



## What's next?

- Continued development of CST simulations to better understand the effect of coupler dispersion on the interaction
- Tomography based analysis using beam transfer maps derived from simulation
- Alternative PPLN THz sources for narrowband deflection fields
- THz based compression in our 100 keV experimental test bed

