# QUANTUM COMPUTING AND HIGH-ENERGY PHYSICS

Heather M. Gray UC Berkeley/LBNL









# INITIAL IDEAS OF QUANTUM COMPUTING

#### The Computer as a Physical System: A Microscopic Quantum Mechanical Hamiltonian Model of Computers as Represented by Turing Machines

Paul Benioff<sup>1,2</sup>

Received June 11, 1979; revised August 9, 1979

In this paper a microscopic quantum mechanical model of computers as represented by Turing machines is constructed. It is shown that for each number N and Turing machine Q there exists a Hamiltonian  $H_N^Q$  and a class of appropriate initial states such that if  $\Psi_Q^N(0)$  is such an initial state, then  $\Psi_Q^N(t) = \exp(-iH_N^Q t) \Psi_Q^N(0)$  correctly describes at times  $t_3$ ,  $t_6, \ldots, t_{3N}$  model states that correspond to the completion of the first, second,..., Nth computation step of Q. The model parameters can be adjusted so that for an arbitrary time interval  $\Delta$  around  $t_3$ ,  $t_6, \ldots, t_{3N}$ , the "machine" part of  $\Psi_Q^N(t)$  is stationary.

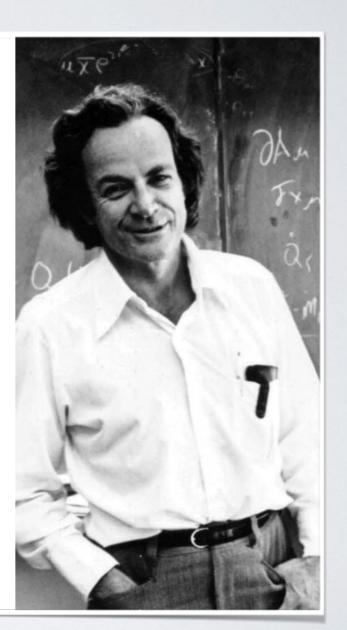
**KEY WORDS:** Computer as a physical system; microscopic Hamiltonian models of computers; Schrödinger equation description of Turing machines; Coleman model approximation; closed conservative system; quantum spin lattices

Journal of Statistical Physics, Vol. 22, No. 5, 1980

"Let the computer itself be built of quantum mechanical elements which obey quantum mechanical laws."

#### LOS ALAMOS NATIONAL LABORATORY 40th ANNIVERSARY CONFERENCE NEW DIRECTIONS IN PHYSICS AND CHEMISTRY April 13-15, 1983 Wednesday, April 13 6:00-8:00 P.M.—Informal Reception at Fuller Lodge Thursday, April 14 Main Auditorium, Administration Building Welcome-Donald M. Kerr, Director Los Alamos National Laboratory Session I-Robert Serber, Chairman Richard Feynman "Tiny Computers Obeying Quantum-Mechanical 10:00 A.M. I. I. Rabi "How Well We Meant" 11:00-11:15 а.м.—Intermi Session II-Donald W. Kerst, Chairman "Tuning Up the Time Projection Chamber 12:15-1:15 р.м.—Lunch Felix Bloch "Past, Present and Future of Nuclear Magnetic Resonance' 2:15-2.30 P.M.-Intermission Session III-Edwin McMillan, Chairman Robert R. Wilson "Early Los Alamos Accelerators and New Accelerators' Norman Ramsey "Experiments on Time-Reversal Symmetry and Parity" 'Physics with Heavy Ion Accelerators'

**RICHARD FEYNMAN (1982)** 



#### ALMOST 40 YEARS LATER

IBM 20Q Tokyo chip



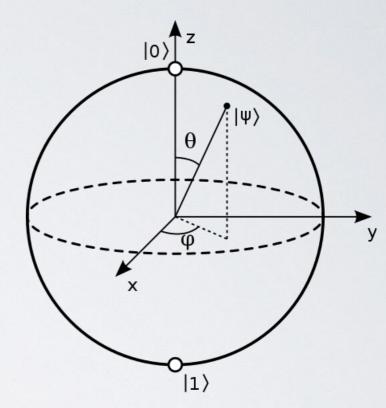
D Wave 2000Q

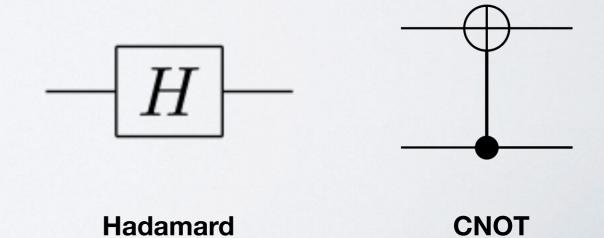


Forest Stearns, Google Al Quantum Artist in Residence Erik Lucero, Research Scientist and Lead Production Quantum Hardware

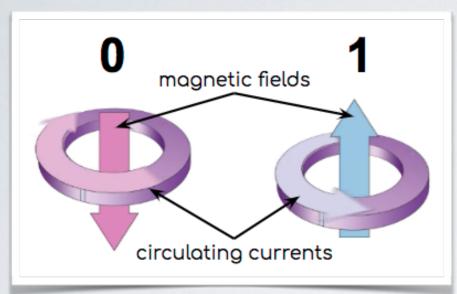
# WHAT IS A (UNIVERSAL) QUANTUM COMPUTER?

- Bits → qubits
- Exploit quantum properties: superposition, entanglement, interference
- Quantum logic gates
- Obey unitarity → reversible computing

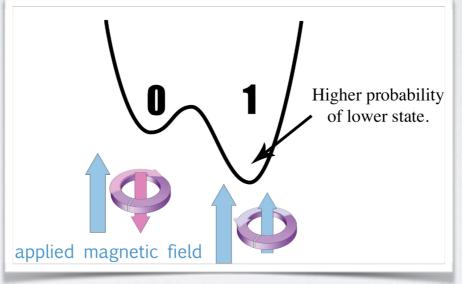




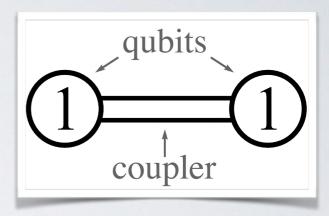
# WHAT IS A QUANTUM ANNEALER?



qubits  $\Rightarrow$  q<sub>i</sub>



bias weights  $\Rightarrow$   $a_i$ 



coupling strength  $\Rightarrow$  b<sub>ij</sub>

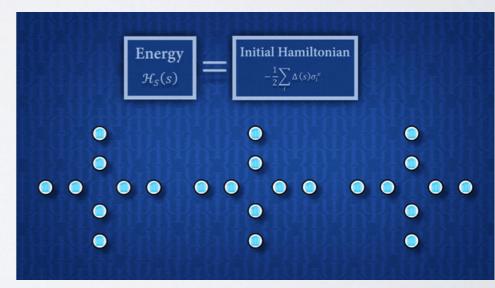
$$O(a; b; q) = \sum_{i=1}^{N} a_i q_i + \sum_{i=1}^{N} \sum_{j=1}^{N} b_{ij} q_i q_j \quad q_i \in \{0, 1\}$$

QUBO

Quadratic
Unconstrained
Binary
Optimisation

Kadowaki and Nishimori, PRE58 5355, 1998

Glover et al, arXiv:1811.11538

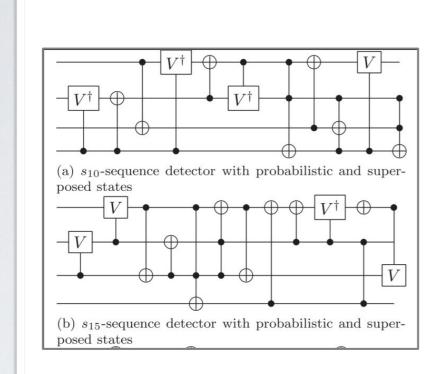


annealing time ~20µs

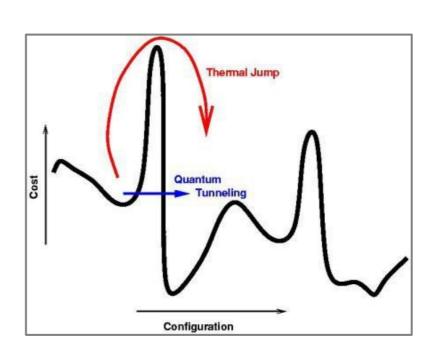
Slide credit: L. Linder

### QUBIT AND QUBIT





Quantum Circuits
Series of quantum gates
operating on a set of
quantum states.

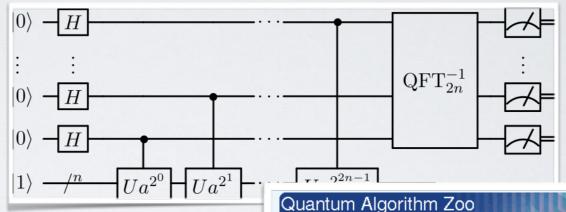


Quantum Annealing
Evolution of a quantum
system to a low T Gibbs state
That's D-Wave!

#### WHY ARE PEOPLE EXCITED?

- Quantum cryptography
  - Shor's algorithm
- Quantum simulation
- Quantum search
  - Grover's algorithm
- Huge information capacity
- Quantum machine learning
- Quantum supremacy

Circuit from Shor's Algorithm



This is a comprehensive catalog of quantum algorithms. If you notice any errors or omissions, please email me at stephen.jordan@microsoft.com. Your help is appreciated and will be acknowledged

#### **Algebraic and Number Theoretic Algorithms**

Algorithm: Factoring Speedup: Superpolynomial

**Description:** Given an *n*-bit integer, find the prime factorization. The quantum algorithm of Peter Shor solves this in  $\widetilde{O}(n^3)$  time [82,125]. The fastest known classical algorithm for integer factorization is

#### **Quantum supremacy using a programmable** superconducting processor

https://doi.org/10.1038/s41586-019-1666-5 Received: 22 July 2019

Published online: 23 October 2019

Accepted: 20 September 2019

ang¹. Dvir Kafri¹. Kostvantvn Kechedzhi¹. Julian Kellv¹. Paul V. Klimov¹. Sergev Kny

 $\overline{\ \ \, }$  The promise of quantum computers is that certain computational tasks might be executed exponentially faster on a quantum processor than on a classical processor<sup>1</sup>. A distribution, which we verify using classical simulations. Our Sycamore processor takes benchmarks currently indicate that the equivalent task for a state-of-the-art classical supercomputer would take approximately 10,000 years. This dramatic increase in speed compared to all known classical algorithms is an experimental realization of uantum sunremacy<sup>8-14</sup> for this specific computational task, heralding a muchanticipated computing paradigm

#### Quantum zoo

pelieved to run in time  $2^{\widetilde{O}(n^{1/3})}$ . The best rigorously prove

"the point when quantum computers can do things that classical computers can't"

John Preskill, Caltech

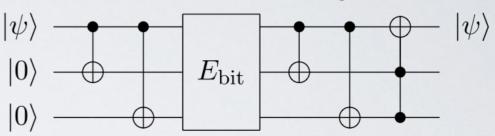
# ASIDE: QUANTUM SUPREMACY

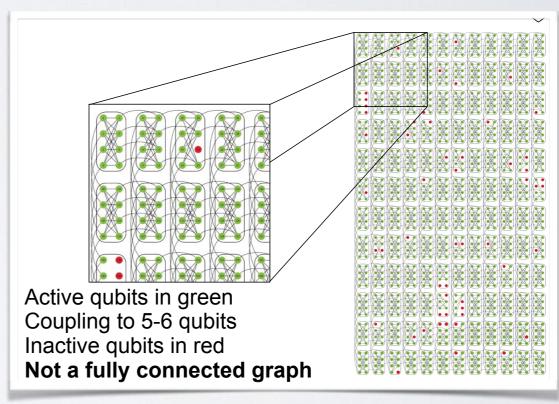
- In Oct 2019, Google published a <u>paper</u> in Nature claiming they had achieved quantum supremacy by solving a problem in 200s on Sycamore that would take Summit 10k years
  - The problem: sampling numbers from a pseudo-random quantum circuit
- Response from IBM: "We argue that an ideal simulation of the same task can be performed on a classical system in 2.5 days and with far greater fidelity."
  - They argue that Google had neglected to account for disk space

#### WHAT ARE THE PROBLEMS?

- · Quantum decoherence
- Quantum noise
  - Quantum error correcting codes
- Scalability (typically O(10s) qubits)
- Connectivity

#### **Quantum error correcting code**





Credit: J.R. Vlimant

# UNIVERSAL QUANTUM COMPUTERS

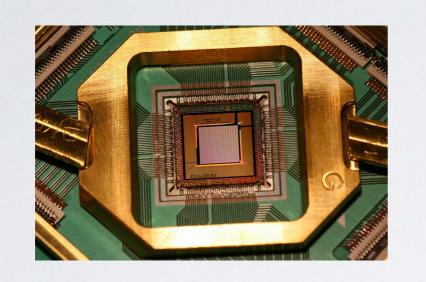
#### Circuit-based quantum processors [edit]

These QPUs are based on the quantum circuit and quantum logic gate-based model of computing.

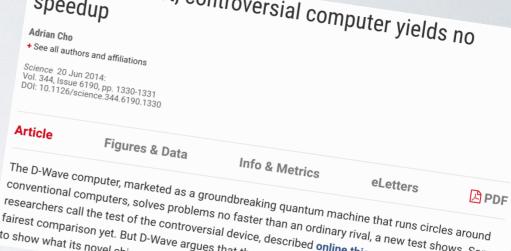
Manufacturer +	Name/Codename/Designation +	Architecture +	Layout \$	Socket +	Fidelity +	Qubits -	Release date +
Google	Bristlecone	Superconducting	6×12 lattice	N/A	99% (readout) 99.9% (1 qubit) 99.4% (2 qubits)	72 qb <sup>[3][4]</sup>	5 March 2018
Google	Sycamore	Nonlinear superconducting resonator	N/A	N/A	N/A	transmon qb 53 qb effective	2019
IBM	IBM Q 53	Superconducting	N/A	N/A	N/A	53 qb	October 2019
IBM	IBM Q 50 prototype	Superconducting	N/A	N/A	N/A	50 qb <sup>[7]</sup>	
Google	N/A	Superconducting	7×7 lattice	N/A	99.7% <sup>[1]</sup>	49 qb <sup>[2]</sup>	Q4 2017 (planned)
Intel	Tangle Lake	Superconducting	N/A	108-pin cross gap	N/A	49 qb <sup>[10]</sup>	9 January 2018
Google	N/A	Superconducting	N/A	N/A	99.5% <sup>[1]</sup>	20 qb	2017
IBM	IBM Q 20 Tokyo	Superconducting	5x4 lattice	N/A	99.812% (average gate) 93.21% (readout)	20 qb <sup>[7]</sup>	10 November 2017

Quantum processors on wikipedia

## QUANTUM ANNEALERS



## Quantum or not, controversial computer yields no

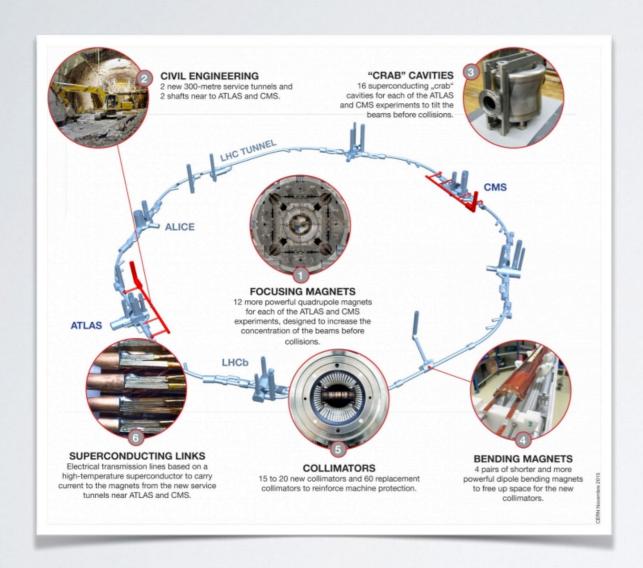


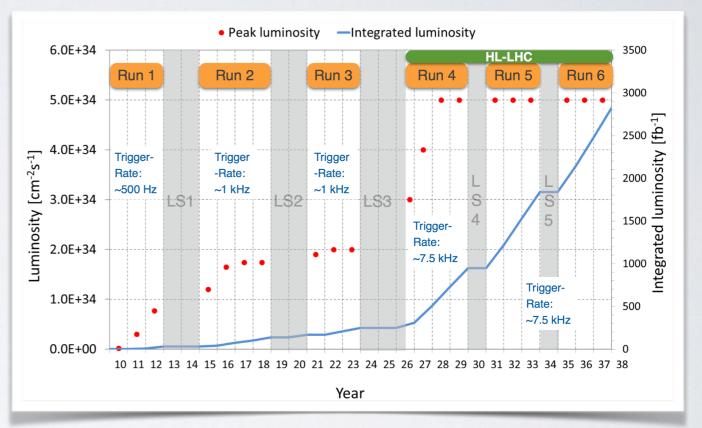
conventional computers, solves problems no faster than an ordinary rival, a new test shows. Some researchers call the test of the controversial device, described online this week in Science, the fairest comparison yet. But D-Wave argues that the computations used in the study were too easy

Manufacturer +	Name/Codename/Designation +	Architecture +	Layout +	Socket +	Fidelity +	Qubits +	Release date +
D-Wave	D-Wave One (Ranier)	Superconducting	N/A	N/A	N/A	128 qb	11 May 2011
D-Wave	D-Wave Two	Superconducting	N/A	N/A	N/A	512 qb	2013
D-Wave	D-Wave 2X	Superconducting	N/A	N/A	N/A	1152 qb	2015
D-Wave	D-Wave 2000Q	Superconducting	N/A	N/A	N/A	2048 qb	2017
D-Wave	D-Wave Advantage	Superconducting	N/A	N/A	N/A	5000 qb	2020

Note: Quantum annealers are intended for use in specific technical applications.

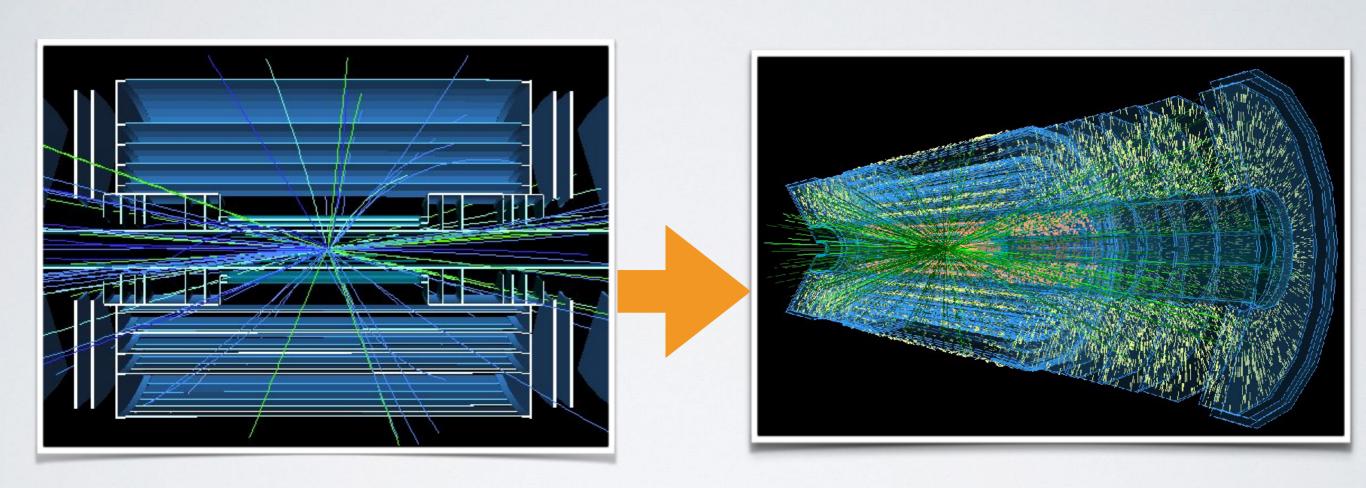
#### UPGRADE ALERT: HL-LHC





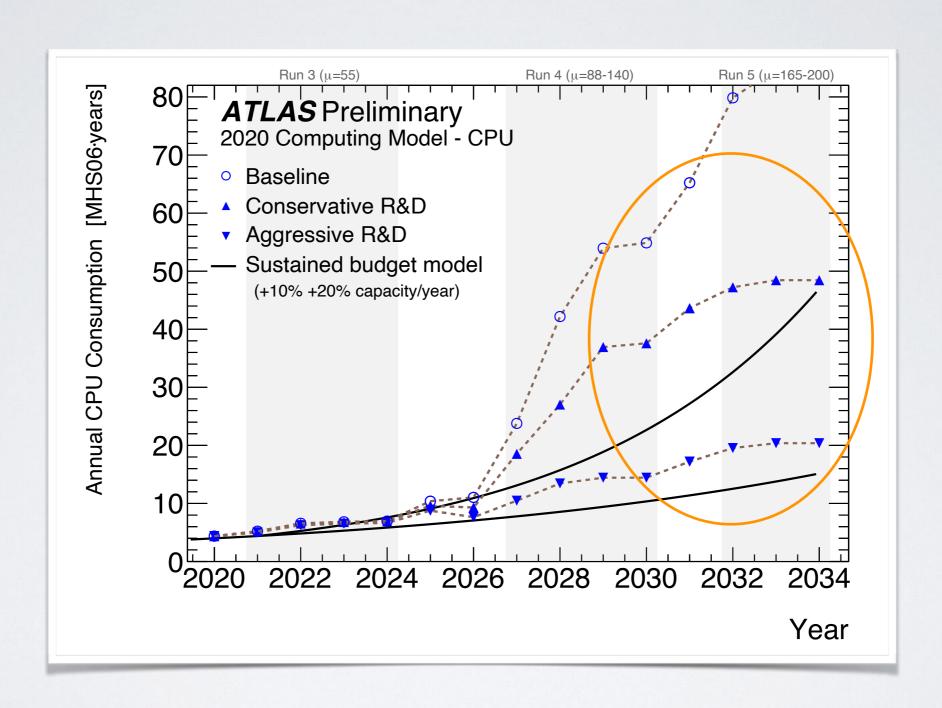
Great for physics ... but a challenge for computing

# HL-LHC COMPUTING CHALLENGE

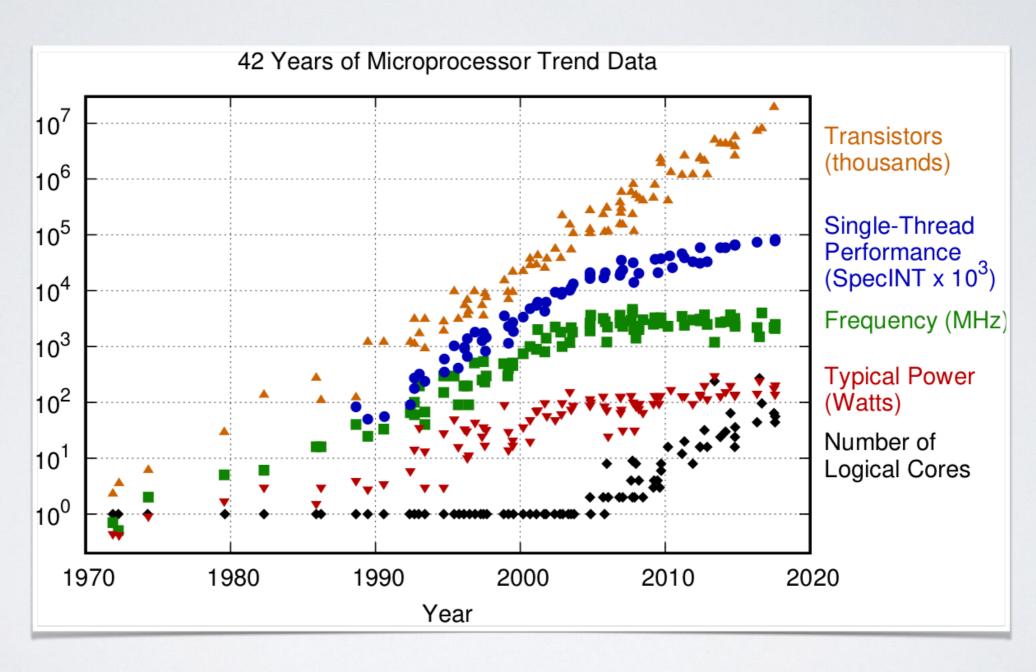


Combinatoric explosion that naively scales as n!

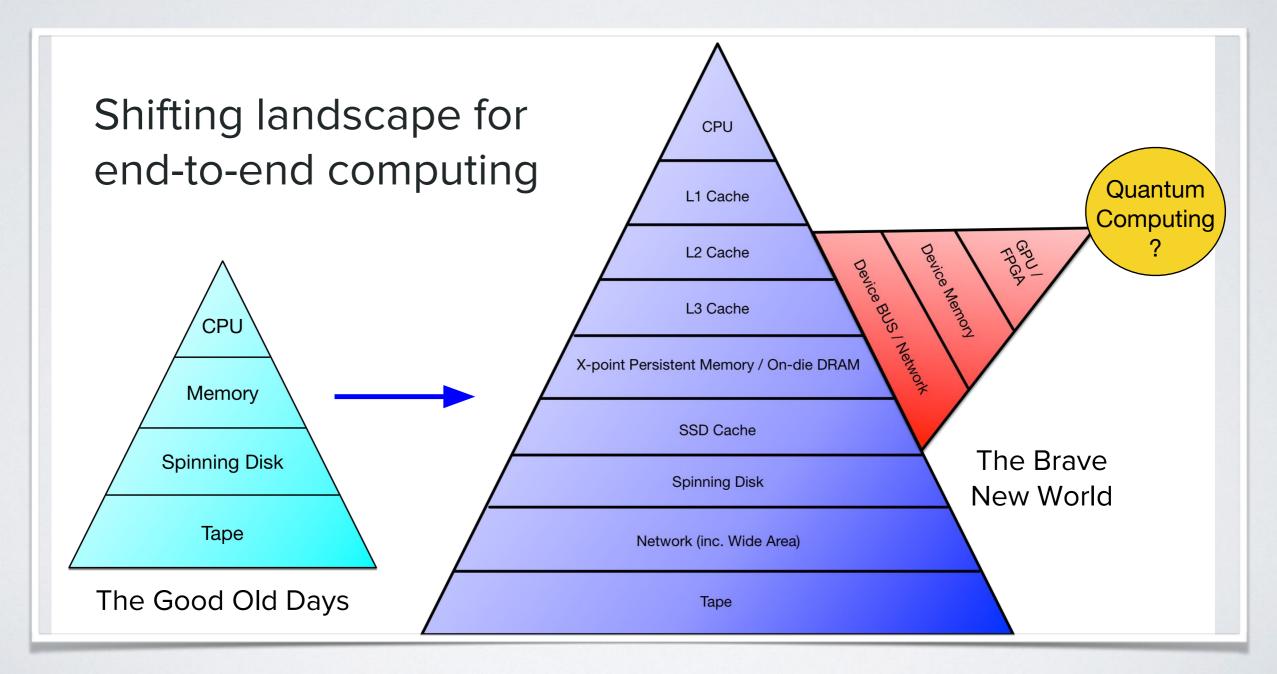
#### TRACKING: KEY FOR HL-LHC



## A SECOND PROBLEM: TECHNOLOGY



# SHIFTING COMPUTING LANDSCAPE

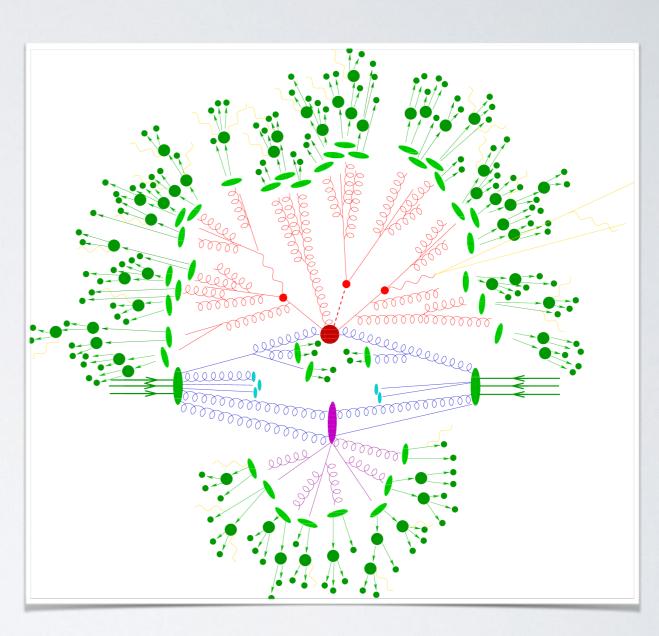


# COULD QUANTUM COMPUTING BE USEFUL FOR PARTICLE PHYSICS?



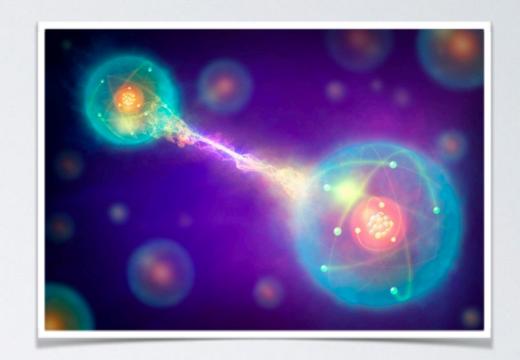
## SIMULATING CORRELATIONS

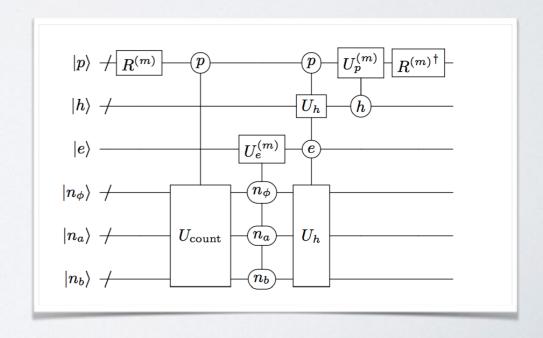
Currently simulate events assuming the evolution of each particle is independent



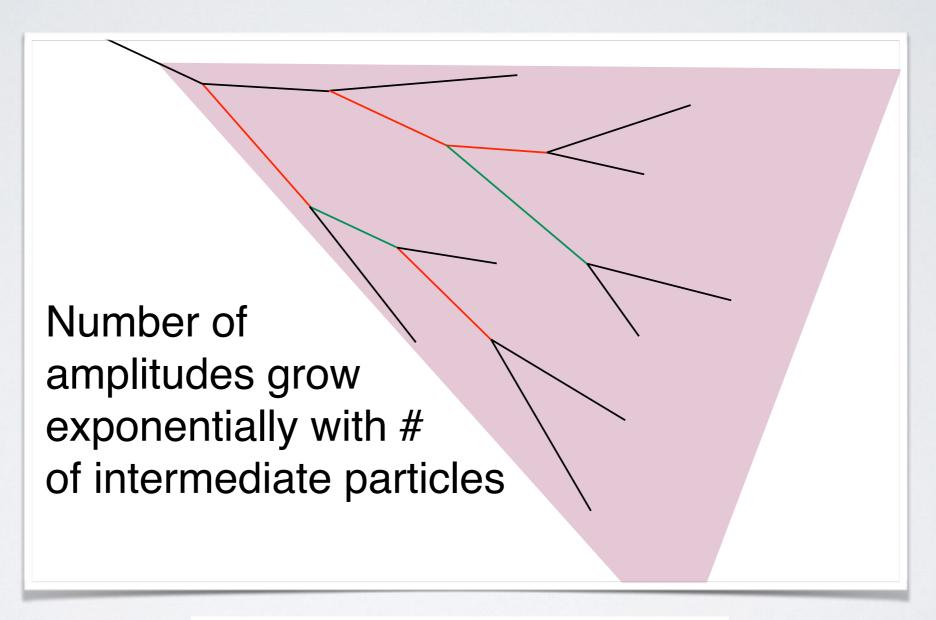
#### ENTANGLEMENT

- This isn't the full picture
  - Particles are quantum mechanical objects
  - Correlations exist between them
- Idea: exploit entanglement between qubits on a quantum computer to improve the description of the parton shower





#### CLASSICALLY



Christian Bauer
Quantum algorithms for High Energy Physics Simulations

#### TOY MODEL

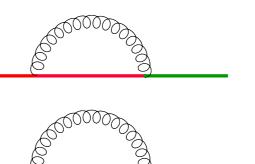
$$\mathcal{L} = \bar{f}_1(i\partial + m_1)f_1 + \bar{f}_2(i\partial + m_2)f_2 + (\partial_\mu \phi)^2 + g_1\bar{f}_1f_1\phi + g_2\bar{f}_2f_2\phi + g_{12}\left[\bar{f}_1f_2 + \bar{f}_2f_1\right]\phi$$

The mixing g<sub>12</sub> gives several interesting effects

Different real emission amplitudes give rise to interference

کے کے

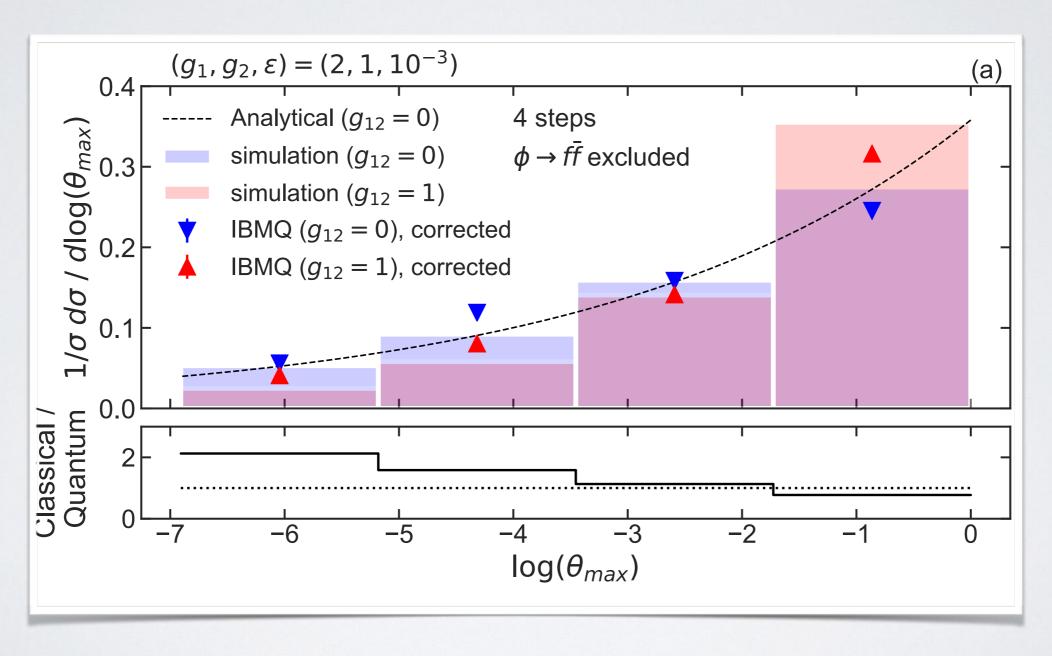
Virtual diagrams give rise to flavor change without radiation

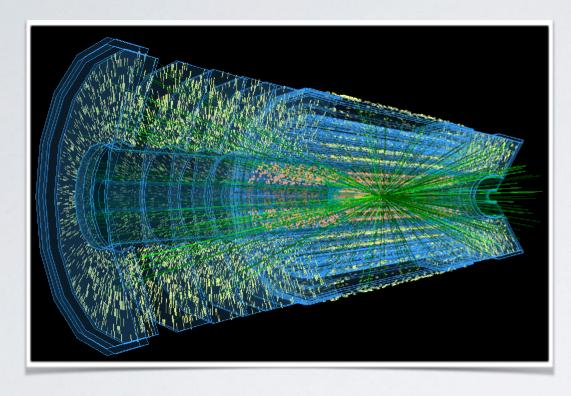


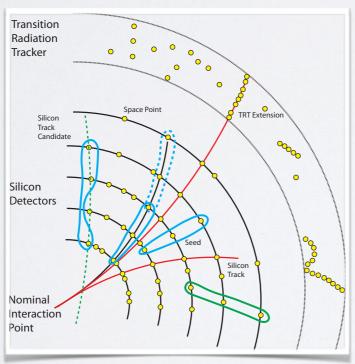
Need to correct both real and virtual effects

Similar to including subleading color

#### EARLY RESULTS



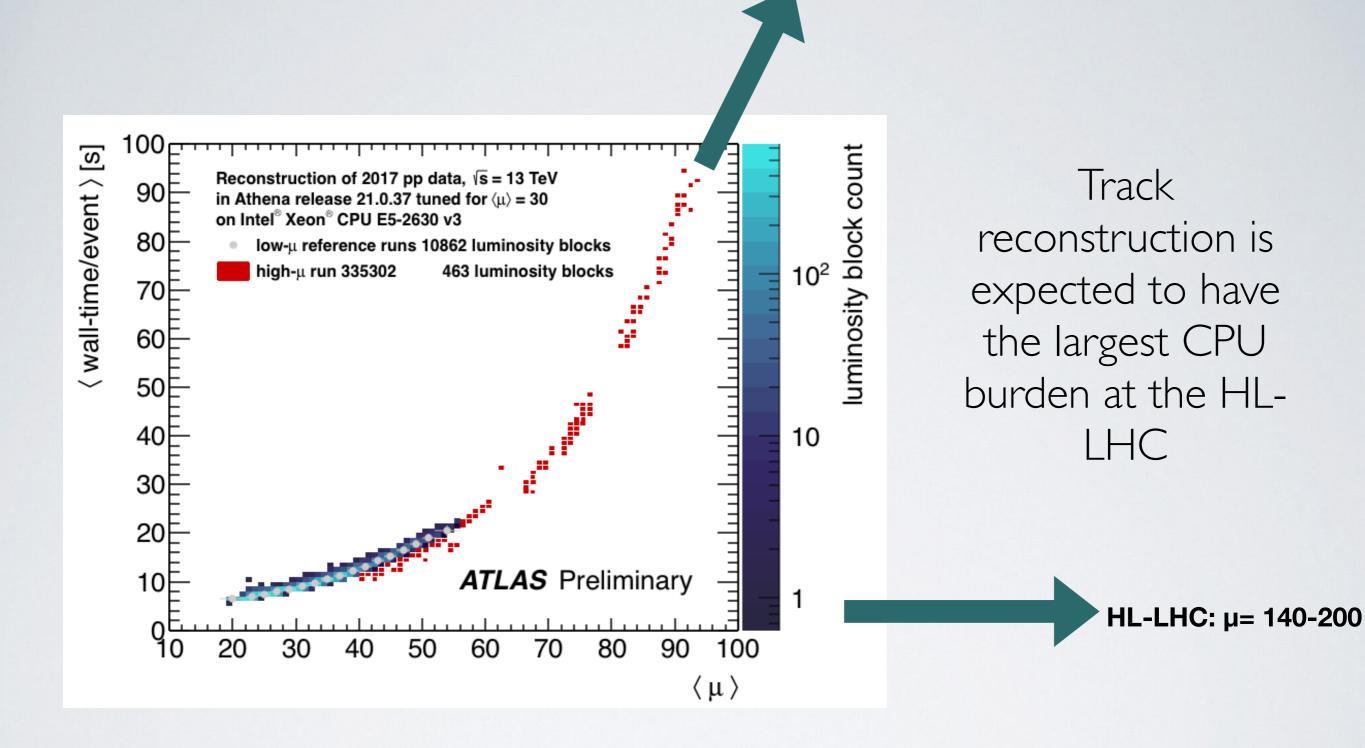






## RECONSTRUC TINGTRACKS

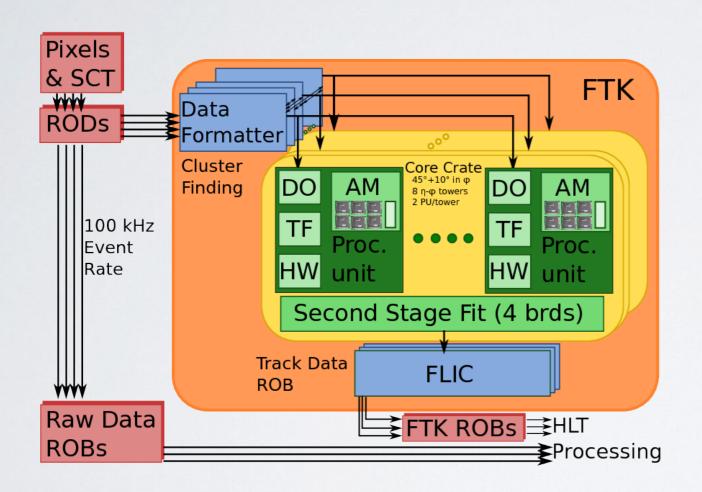
https://sites.google.com/lbl.gov/hep-qpr



Storage is also (probably more significant) problem

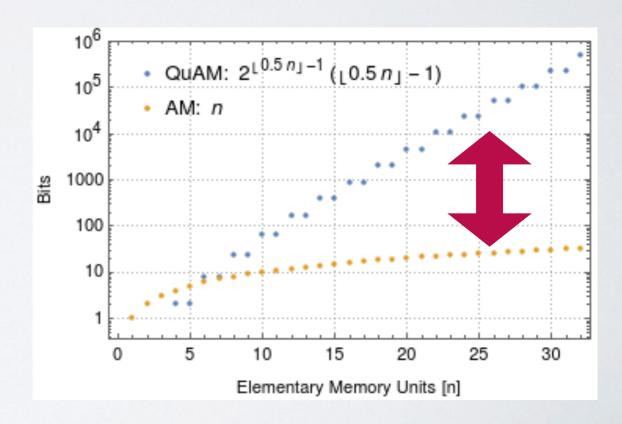


# DIFFERENT ALGORITHMS: ASSOCIATIVE MEMORY



Inspired by ideas for FTK

Memory required scales far more slowly with the number of tracks



arXiv:1902.00498

Slide credit: I. Shapoval



## IMPLEMENTATION (I)

- We developed QuAM circuit generators implementing the Trugenberger's initialization and generalized Grover's algorithms.
  - use open-source quantum computing platform,
     Qiskit
- Supported backends
  - IBM QE cloud-based quantum chips [5Q Yorktown/Tenerife, I4Q Melbourne, 20Q Tokyo]
  - Local/remote noisy simulators

#### Storage QuAM

```
1 OPENOASM 2.0;
2 include "qelibl.inc";
3 qreg qr[6];
4 creg cr[6];
5 x qr[3], qr[0];
6 cx qr[3],qr[0];
7 ccx qr[0],qr[3],qr[4];
8 ccx qr[1],qr[5];
9 cx qr[1],qr[5];
10 cx qr[0],qr[4];
11 x qr[5];
12 x qr[4];
13 ccx qr[5],qr[4],qr[2];
14 cu3(1.23095941734077,3.14159265358979,3.14159265358979) qr[2],qr[3]
15 ccx qr[5],qr[4],qr[2];
16 x qr[6];
17 x qr[4];
18 cx qr[1],qr[5];
19 cx qr[0],qr[4];
20 ccx qr[0],qr[3],qr[4];
21 ccx qr[1],qr[3],qr[5];
22 reset qr[0];
23 reset qr[0];
24 cx qr[3],qr[0];
25 cx qr[3],qr[0];
```

#### Retrieval QuAM

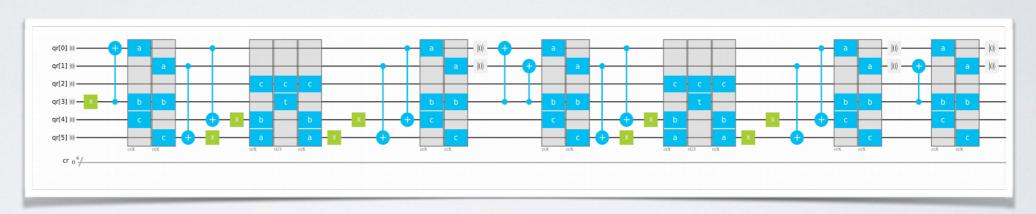
```
51 s qr[5];
52 h qr[5];
53 cx qr[4],qr[5];
54 h qr[5];
55 s qr[5];
66 h qr[4];
77 h qr[5];
78 x qr[4];
79 x qr[5];
60 h qr[5];
61 cx qr[4],qr[5];
62 h qr[5];
63 x qr[4];
64 x qr[5];
65 h qr[5];
66 h qr[5];
67 h qr[5];
68 cx qr[4],qr[5];
69 h qr[5];
```

arXiv:1902.00498

# QUAM DEMONSTRATION ON IBM-Q

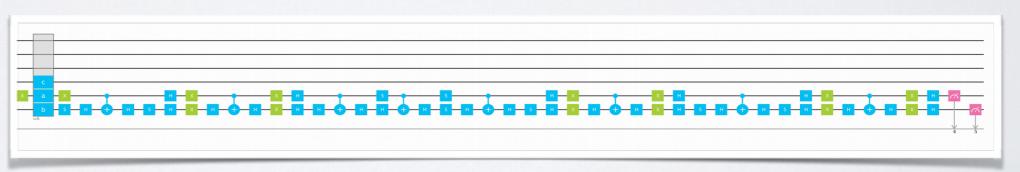
QuAM storage circuit generator

Ex.: complete circuit for retrieving one 2-bit pattern



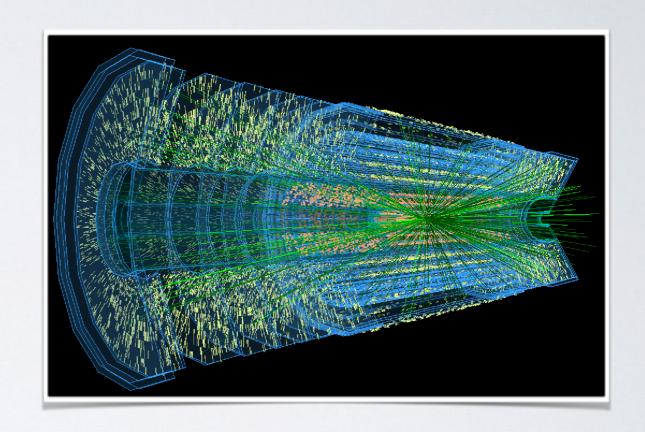
QuAM retrieval circuit generator

Ex.: complete circuit for retrieving one 2-bit pattern



## DIFFERENT ALGORITHMS: QUANTUM ANNEALING

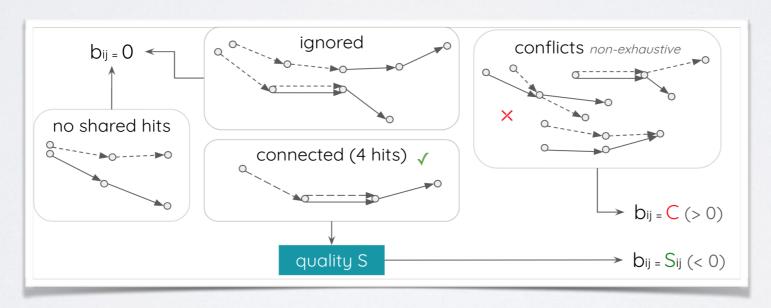
- Reformulate track
   reconstruction as an energy
   minimisation problem
  - Solve using the D-Wave quantum annealer
- Solution time won't scale with number of tracks





#### QUANTUM ANNEALING

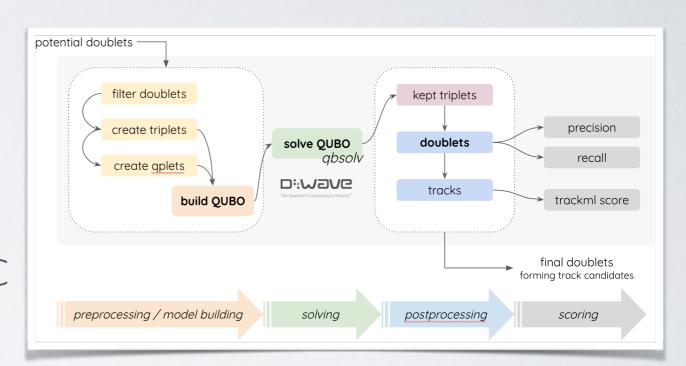
- Implement QUBO minimisation on D-Wave and study scaling with track multiplicity
- Inspired from \*, but use triplets (3 hits) as the qubits
- Encode the quality of the triplets based on physics properties. Pair-wise connections b act as constraints (>0) or incentives (<0):



Minimizing O means selecting the best triplets to form track candidates.

#### IMPLEMENTATION

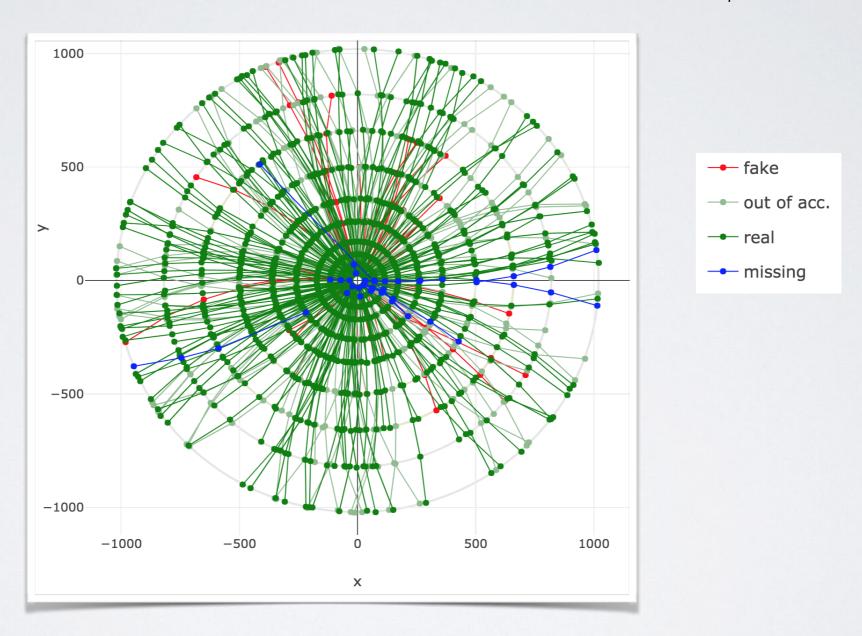
- Dataset: simplified HL-LHC-like\*
   dataset (focus on barrel, I + GeV, 5+
   hits)
  - Toy dataset, but representative of expected conditions at the HL-LHC
- QUBO solvers: qbsolv (D-Wave + simulation), neal (simulation)
- D-Wave 2X (1152 qubits), D-Wave 2000Q (2048 qubits)



\*trackml

#### PERFORMANCE

Doublets for a dataset of 2456 particles and 16855 hits



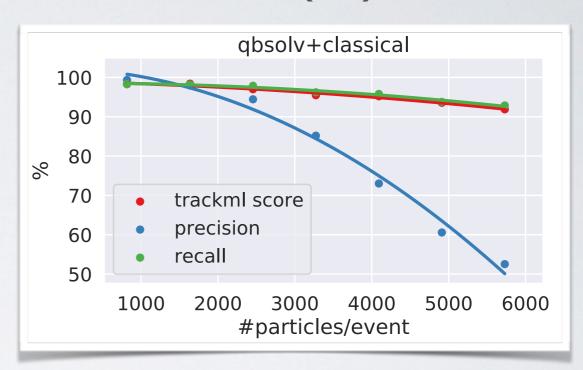
Slide credit: L. Linder

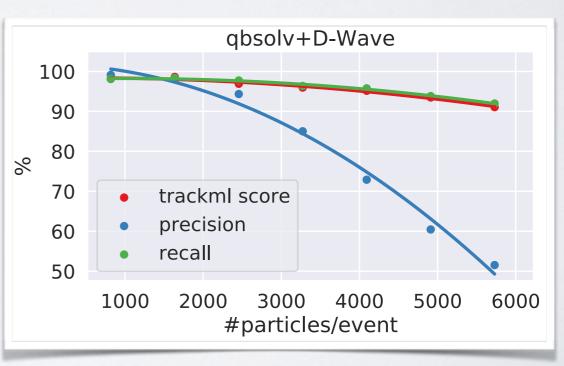
## PERFORMANCE (2)

Physics performance as a function of occupancy using a D-Wave 2X (qbsolv).

Timing building: 0-20 min | solving: 0-12s (sim), 0-56 min (D-Wave)

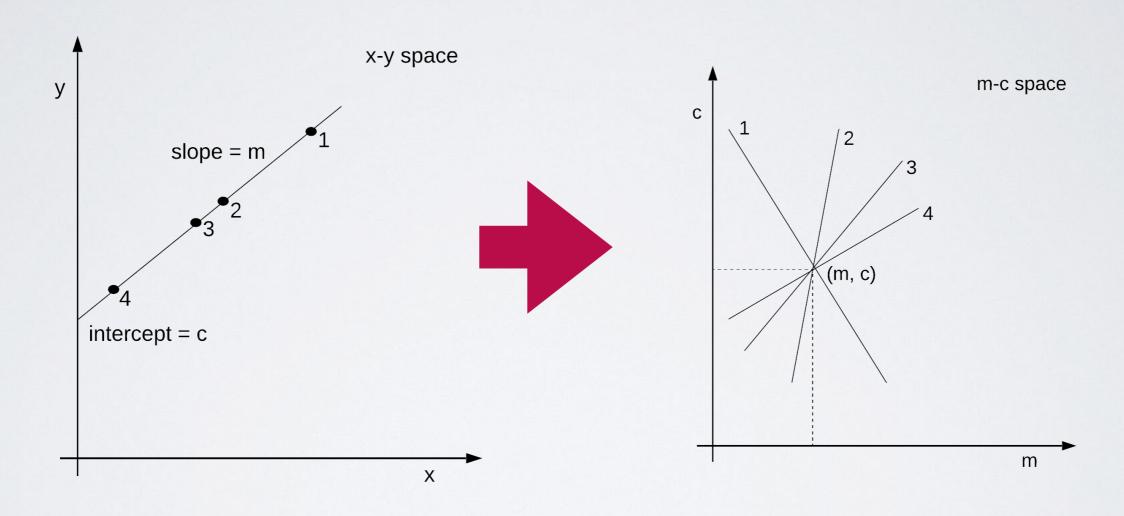
D-Wave | sim. Same physics, important time overhead with D-Wave





Slide credit: L. Linder

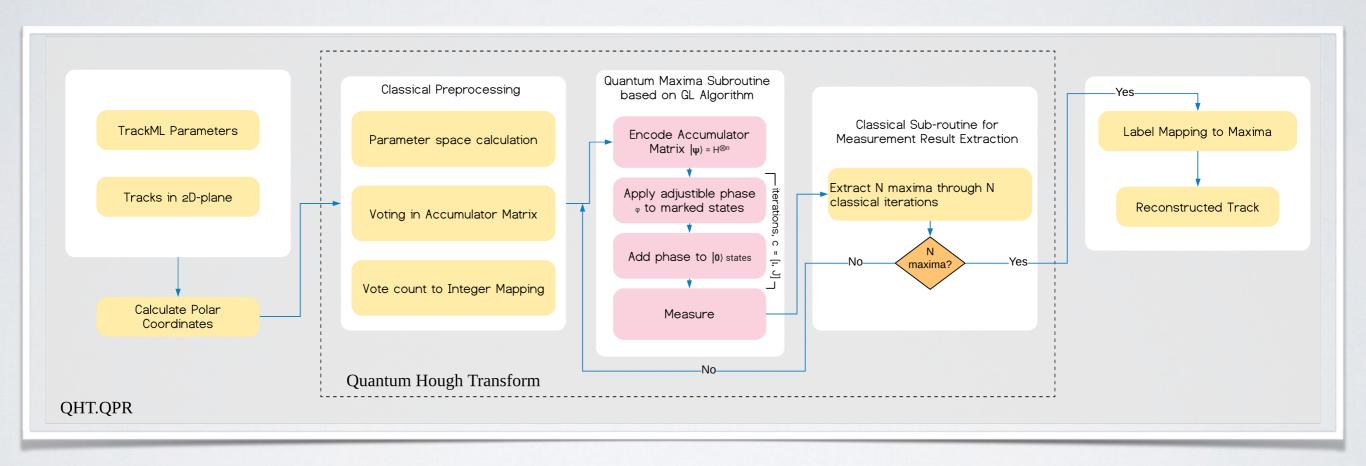
#### DIFFERENT ALGORITHMS: QUANTUM HOUGHTRANSFORM



P.V.C. Hough (1962), R.O. Dude, P.E. Hart (1972), D.H. Ballard (1980)

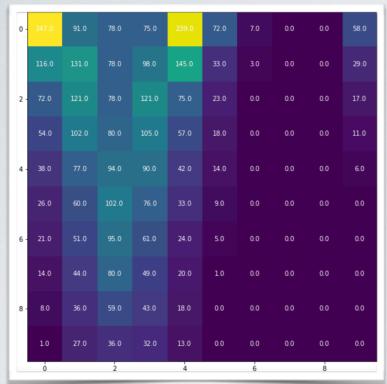


#### IMPLEMENTATION

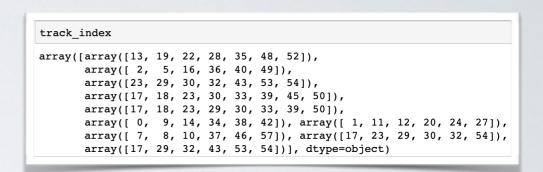


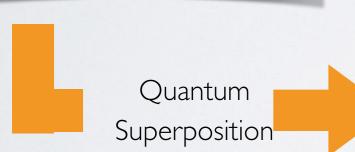
An Optimized Quantum Maximum or Minimum Searching Algorithm and its Circuits.

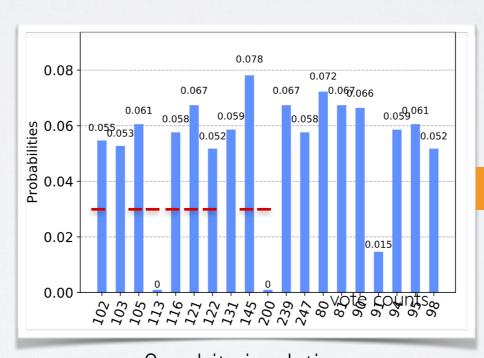
## RESULTS: QUANTUM MAXIMA FINDING



Accumulator Space for 8 tracks







8-qubit simulation #tracks = 4, #bins up to  $2^8$  = 256, time = 58.6s



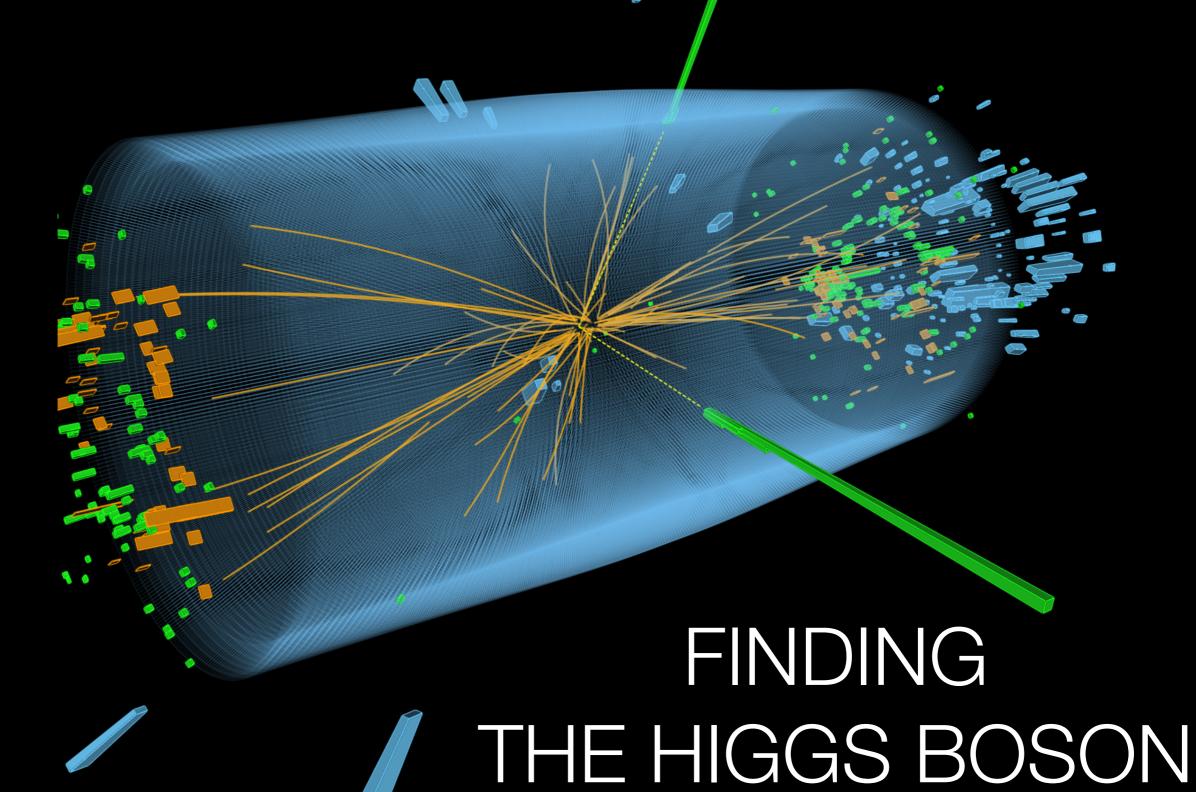
Local Maxima
Detection using
Grover-Long
Algorithm

An Optimized Quantum Maximum or Minimum Searching Algorithm and its Circuits.

Slide Credit: A. Yadav

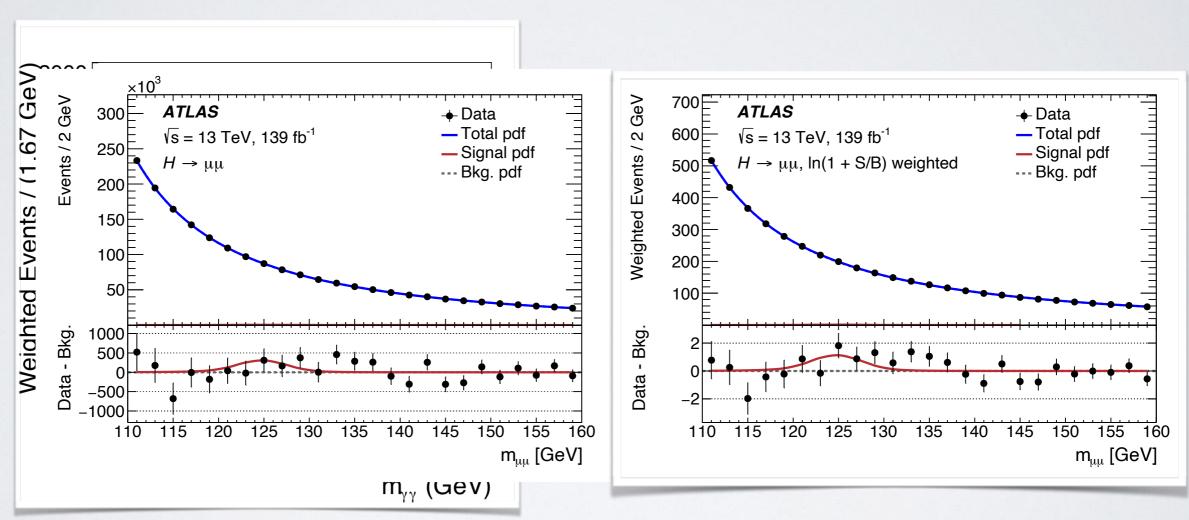






# THE $H \rightarrow \gamma \gamma$ AND $H \rightarrow \mu \mu$ CHANNELS

Something old and something new



CMS, PLB 716, 30-61

ATLAS, arXiv:2007.07830

Quantum computers for machine learning



#### QAML CLASSIFIERS

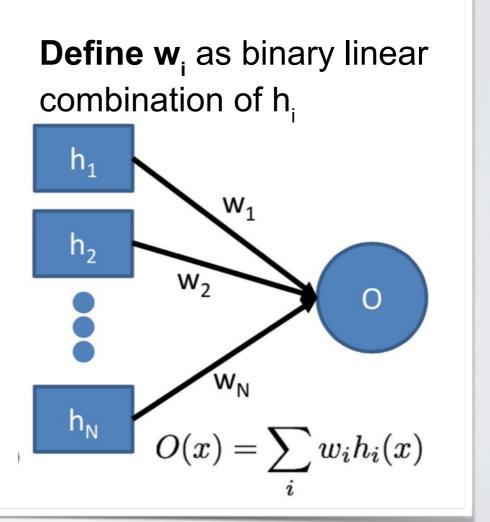
(Quantum Adiabatic Machine Learning)

Abstract—We develop an approach to machine learning and anomaly detection via quantum adiabatic evolution. In the training phase we identify an optimal set of weak classifiers, to form a single strong classifier. In the testing phase we adiabatically evolve one or more strong classifiers on a superposition of inputs in order to find certain anomalous elements in the classification space. Both the training and testing phases are executed via quantum adiabatic evolution. We apply and illustrate this approach in detail to the problem of software verification and validation.

Pudenz and Lidar, arXiv:1109.0325

**Define** functions **h**<sub>i</sub> of the input variables into [-1,1] such that

- P(signal|h>0) > P(bkg|h>0)
- P(bkg|h<0) > P(signal|h<0)</p>
- i.e. Most signal on h>0, most bkg on h<0



## QAML OBJECTIVE FUNC

Define as a "target" function

$$y(x) = \begin{cases} +1, & \text{if } \in S, \\ -1, & \text{if } \in B \end{cases}$$

Per event error 
$$E(x) = y(x) - \sum_{i=1}^N w_i h_i(x)$$

Full error

$$\delta(\vec{w}) \propto \sum_{i,j} C_{ij} w_i w_j + \sum_i (\lambda - 2C_{iy}) w_i$$

- → C<sub>ii</sub> and C<sub>iv</sub> are summations over the values of h<sub>i</sub> over the training set
- → λ is a parameter penalizing the number of non-zero w<sub>i</sub>

## IMPLEMENTATION WITH OUBO

$$\delta(\vec{w}) \propto \sum_{i,j} C_{ij} w_i w_j + \sum_i (\lambda - 2C_{iy}) w_i$$

Simple conversion of binary weights to ±1

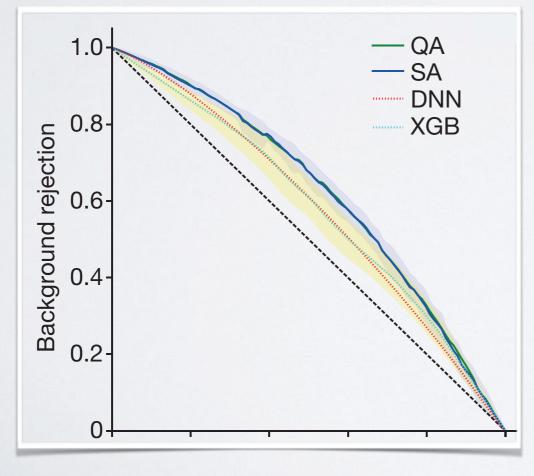
$$H_{\text{Ising}} = \sum_{i} h_i \sigma_i^z + \sum_{ij} J_{ij} \sigma_i^z \sigma_j^z$$

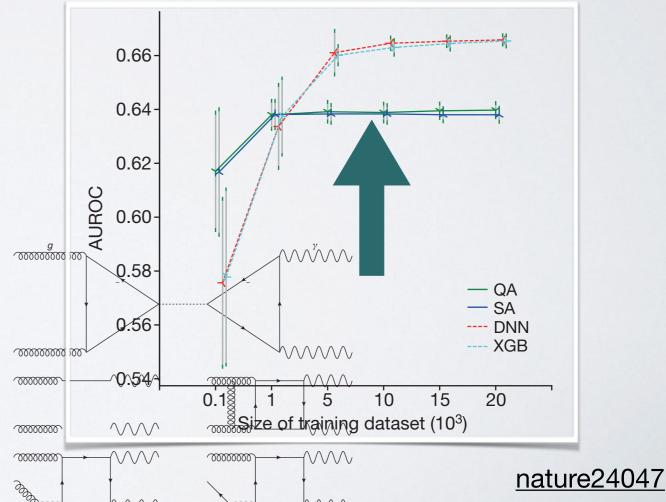
## $\rho_T^2/(p-E) \xrightarrow{\tau} \gamma \gamma ON D-QVAVE$



#### Solving a Higgs optimization problem with quantum annealing for machine learning

Alex Mott<sup>1</sup>†\*, Joshua Job<sup>2,3</sup>\*, Jean-Roch Vlimant<sup>1</sup>, Daniel Lidar<sup>3,4</sup> & Maria Spiropulu<sup>1</sup>

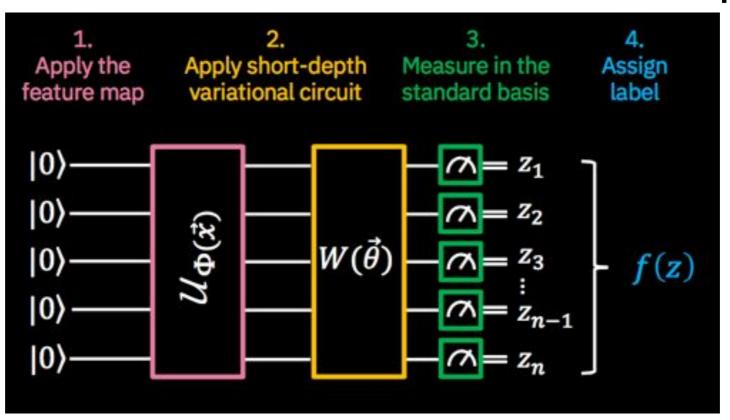






#### VARIATIONAL SVM

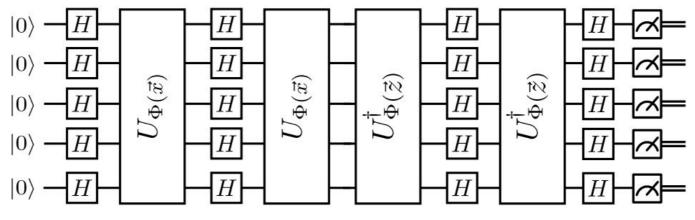
 In 2018, a variational Quantum SVM method was introduced by IBM, published in Nature 567 (2019) 209. The variational Quantum SVM method can be summarized in four steps:



 During the training phase, a set of events are used to train the circuit W(θ) to reproduce correct classification

#### SVM KERNEL METHOD

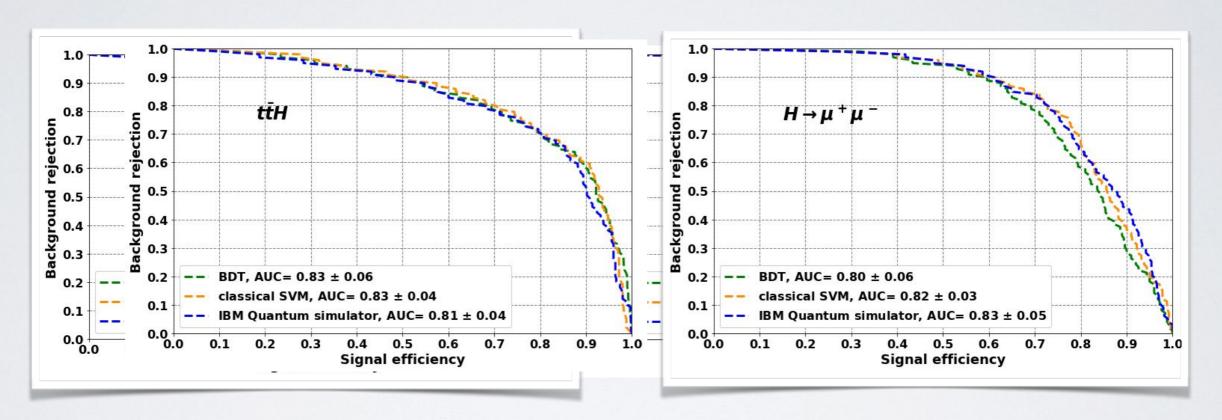
- Kernel Trick for Classical SVM: mapping the non-linear separable data into a higher dimensional feature space using a kernel function that measures the similarity between two data points; then using the kernel to find a separating hyperplane.
- Quantum Kernel Estimation (introduced by IBM, published in Nature 567 (2019) 209): mapping classical data  $\vec{x}$  non-linearly to a quantum state using Quantum Feature Map function; calculating the kernel matrix  $K(\vec{x}, \vec{z}) = |\langle \Phi(\vec{x}) | \Phi(\vec{z}) \rangle|^2$  using a quantum computer; then training the quantum SVM in the same way as a classical SVM.



Nature 567 (2019) 209

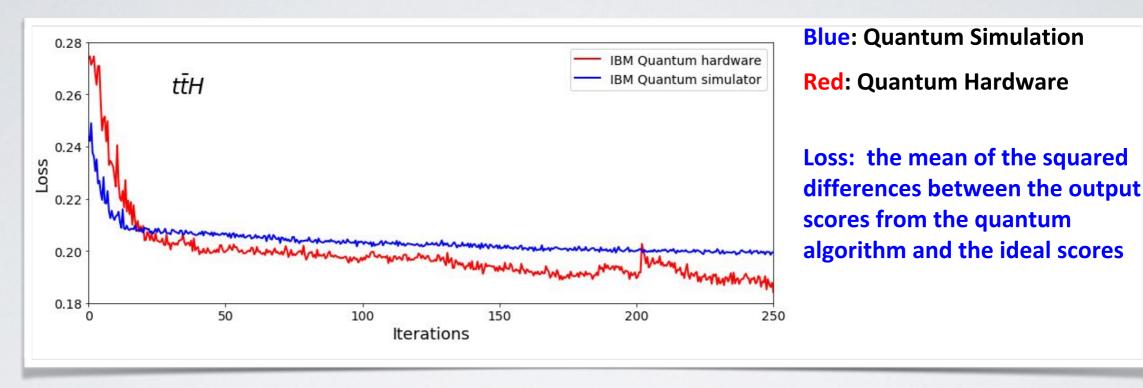
#### SIMULATION RESULTS

Using the Qiskit Qasm simulator

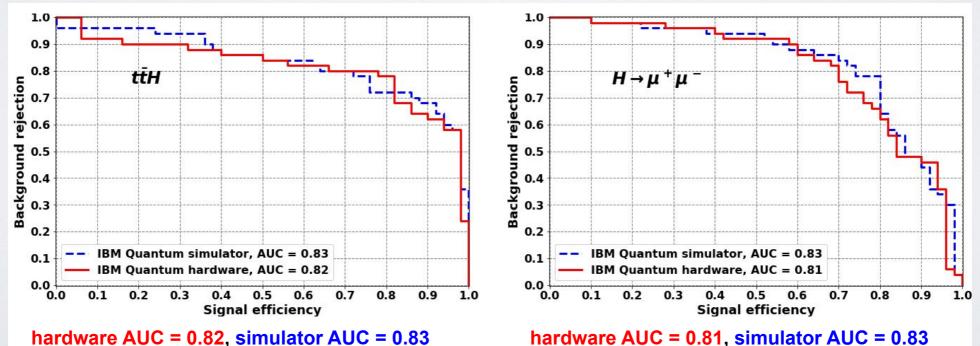


10 qubits, 100 training/testing events

#### RESULTS ON IBM HARDWARE



#### ibmq\_boelingen (20 qubits); ibmq\_paris (27 qubits)



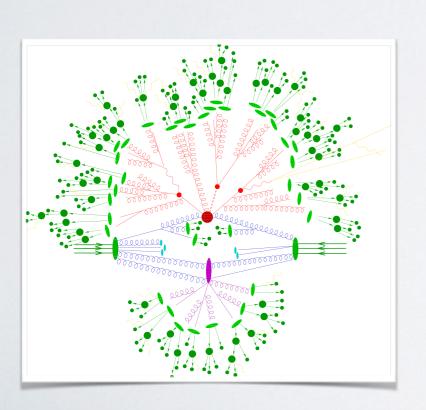
Slide Credit: S.L. Wu and C. Zhou

#### SUMMARY

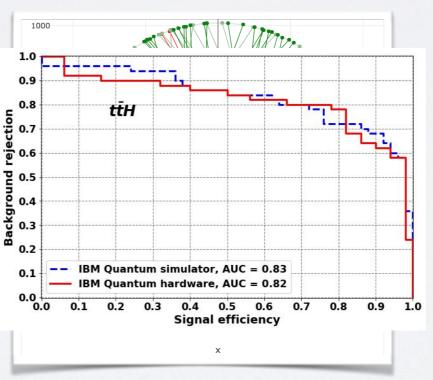
Exciting recent developments in quantum computing

How might they be useful for particle physics?

Simulation



Track Reconstruction



Analysis

