

# Neutrino Interactions and Oscillations: Modelling Neutrino Cross Section Uncertainties for Fundamental Physics

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PPD Seminar

18.03.2026



# Introduction

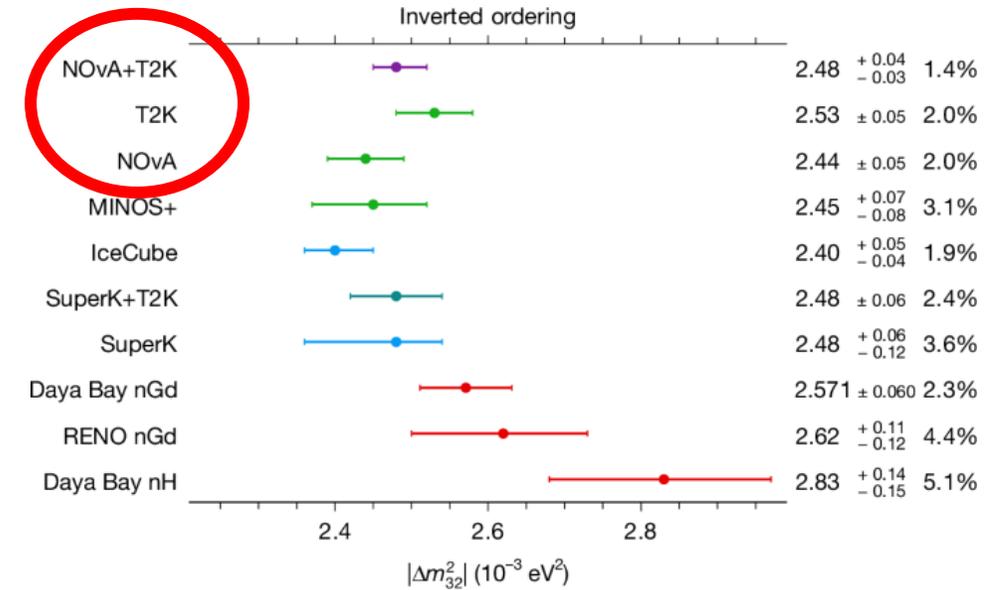
Neutrino experiments are reaching precision era measurement.

Recently joint fit between two experiments **T2K** and **NOvA** has finished and got published in *Nature* 646 (2025) 8086, 818-824

To reach this precision, we need to have uncertainty under control

Especially modelling of neutrino interactions is challenging

## Spoiler Alert!!!



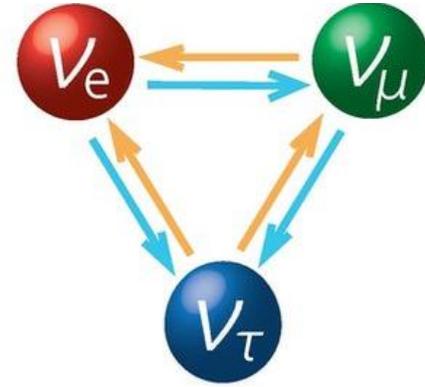
# Prologue: Neutrinos

# Neutrino Oscillations

Neutrinos while travelling can change the flavour, this phenomenon is called neutrino oscillations.

The crucial objective of current neutrino experiments is to study if there is CP violation in the lepton sector or not. **Appearance channel**

$$\frac{P(\nu_\mu \rightarrow \nu_e)}{P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)} \approx \sin^2(2\theta_{13}) \sin^2(\theta_{23}) \sin^2\left(\frac{1.27\Delta m_{32}^2 L}{E}\right) \pm \frac{1.27\Delta m_{21}^2 L}{E} 8J_{CP} \sin^2\left(\frac{1.27\Delta m_{32}^2 L}{E}\right)$$



# Neutrino Oscillations

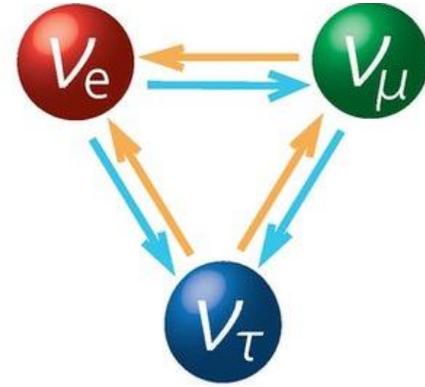
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CP violation in lepton sector means that neutrino oscillation probabilities are different than for antineutrino.

Parameter describing CP violation is  $\delta_{CP}$ .



**Jarlskog Invariant** in general

$$J = \frac{1}{8} \text{Im} [U_{23}U_{12}U_{22}^*U_{13}^*]$$

**Jarlskog Invariant** In lepton sector

$$J_{CP,l} = 0.033 \sin(\delta_{CP})$$

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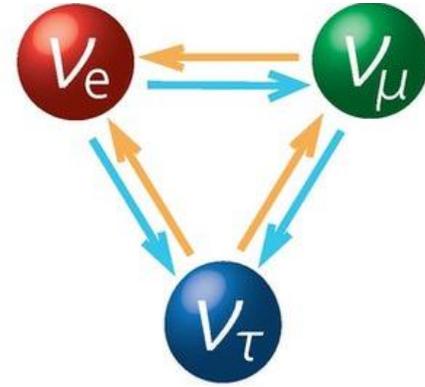
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CP violation in lepton sector means that neutrino oscillation probabilities are different than for antineutrino.

Parameter describing CP violation is  $\delta_{CP}$ .

Neutrino CP violation can be three magnitudes larger than in the quark sector.

Studying this effect has potential to answer the question of why there is more matter than antimatter in the Universe.



**Jarlskog Invariant** in general

$$J = \frac{1}{8} \text{Im} [U_{23}U_{12}U_{22}^*U_{13}^*]$$

**Jarlskog Invariant** In lepton sector

$$J_{CP,l} = 0.033 \sin(\delta_{CP})$$

**Jarlskog Invariant** In quark sector

$$J_{CP,q} = 3 \times 10^{-5}$$

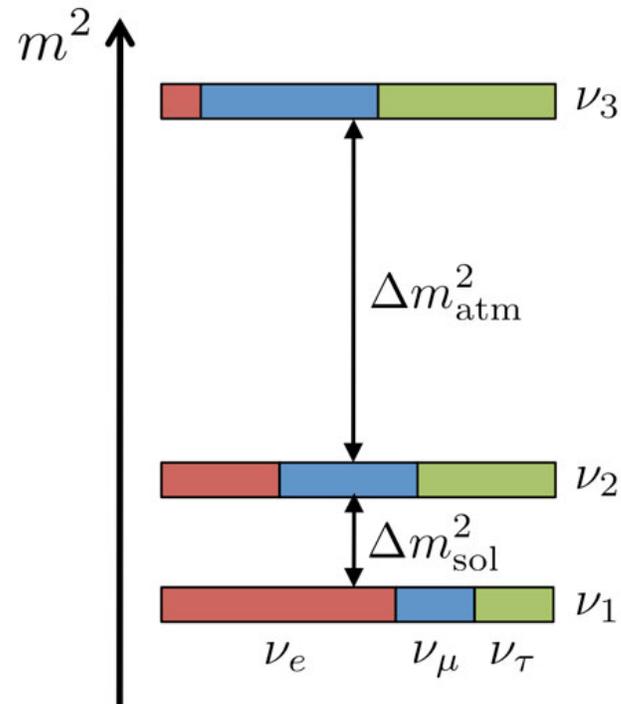
# Mass Ordering

We do know neutrinos have mass.

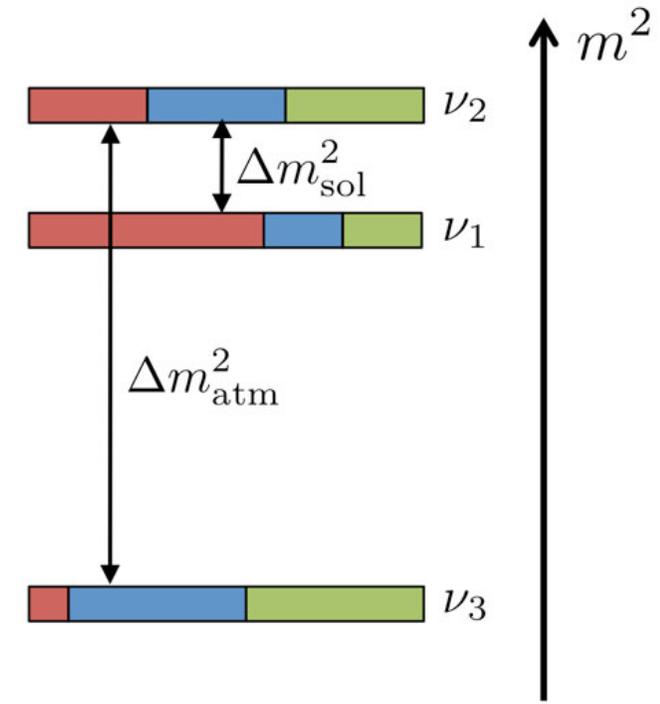
However, we do not know if 3rd eigenstate is largest or smallest

This is what we call mass ordering.

Normal Ordering (NO)



Inverted Ordering (IO)

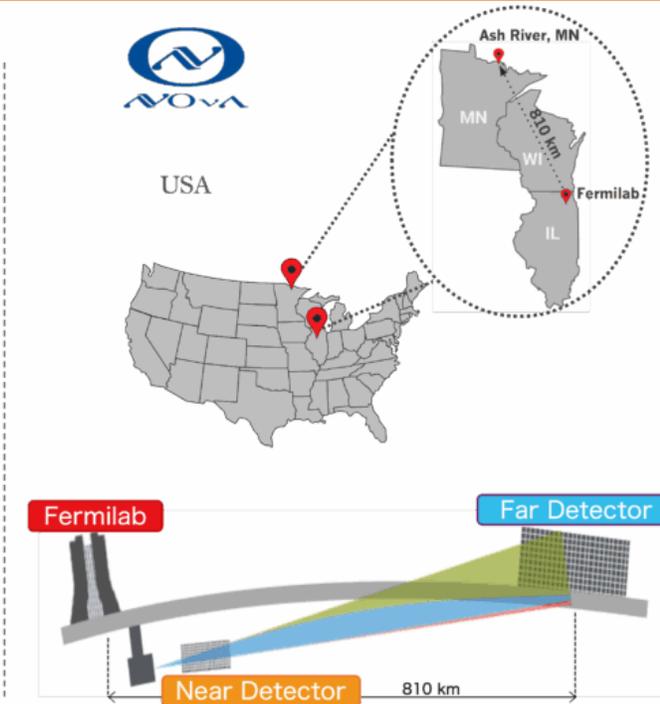
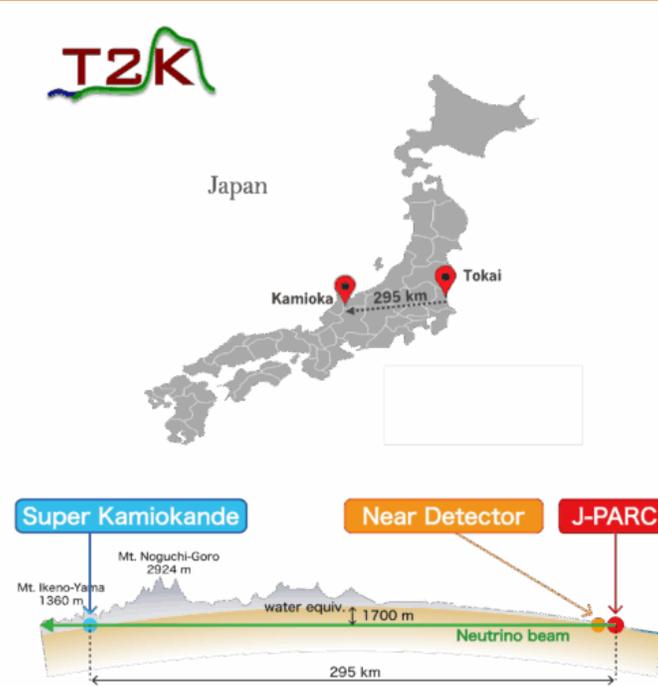


# Long Baseline Neutrino Experiments

Two Long Baseline Neutrino experiment T2K and NOvA

Scheme:

1. Produce neutrino
2. Measure in Near Detector where oscillations are negligible
3. Measure in Far detector after oscillations.



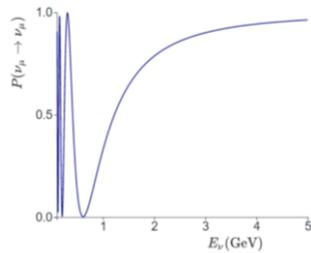
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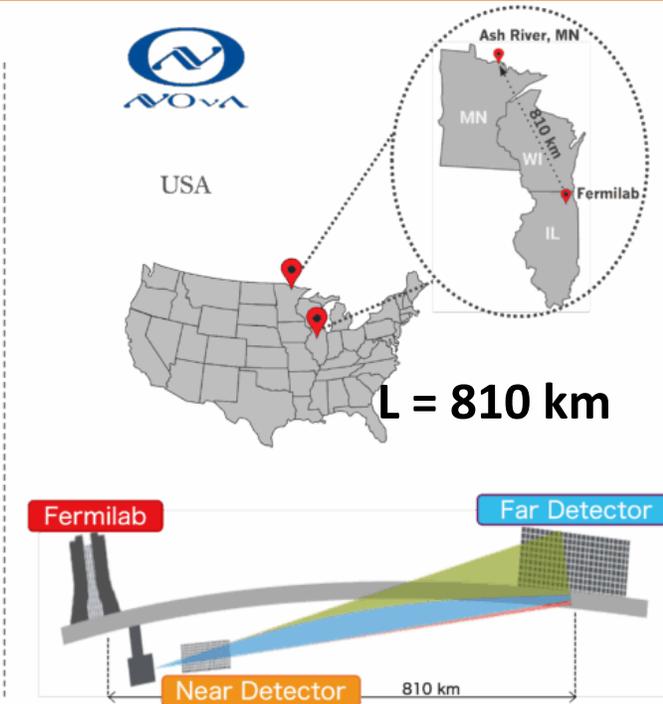
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2. Measure in Near Detector where oscillations are negligible
3. Measure in Far detector after oscillations.

To measure neutrino oscillation probabilities, one simply need to measure **ONLY NEUTRINO ENERGY**



Appearance channel

$$\begin{aligned}
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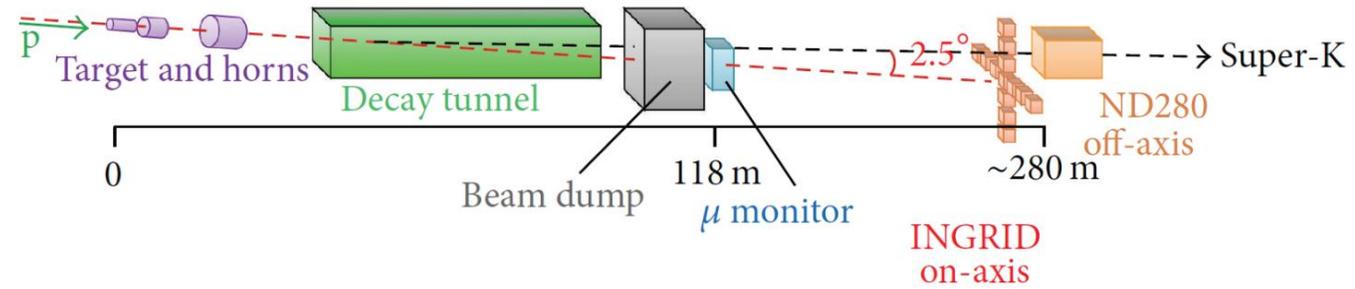
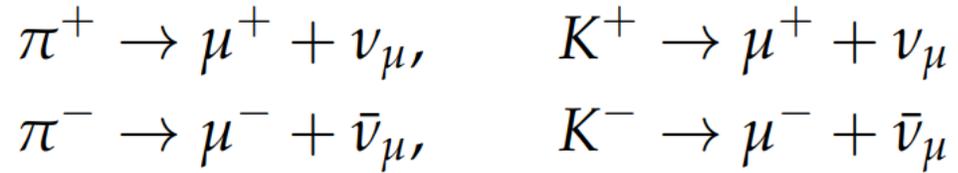
**One doesn't simply**

**Measure neutrino energy**

# Chapter I: Measuring Energy

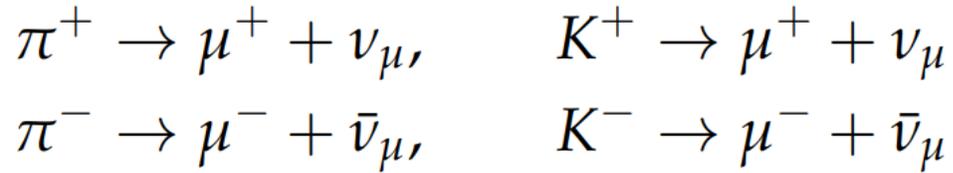
# Neutrino Flux

- Protons hit graphite and hadrons ( $\pi$ ,  $K$ ) which are focused and then decay into neutrinos
- Can select  $\nu/\bar{\nu}$  beam mode based on horn polarity

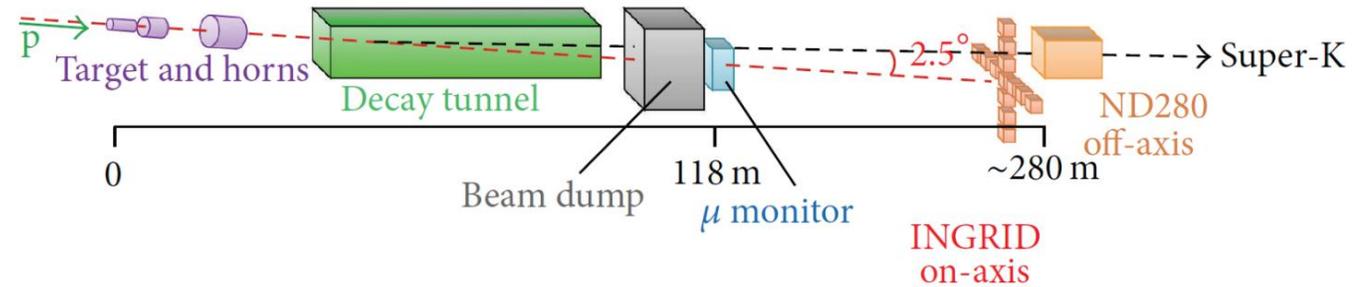


# Neutrino Flux

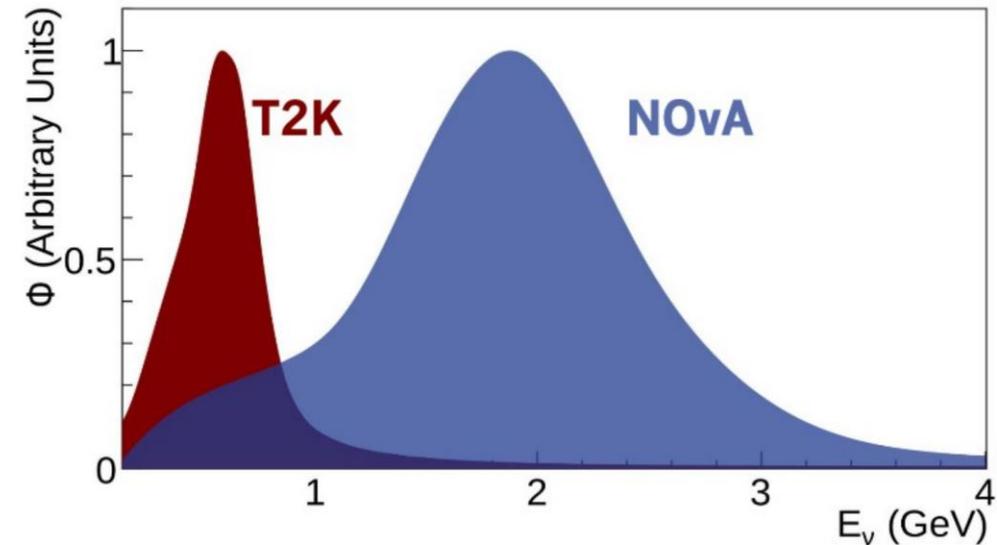
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Therefore, we don't know Energy of incoming neutrino we have spectrum/flux!!!



neutrino spectrum



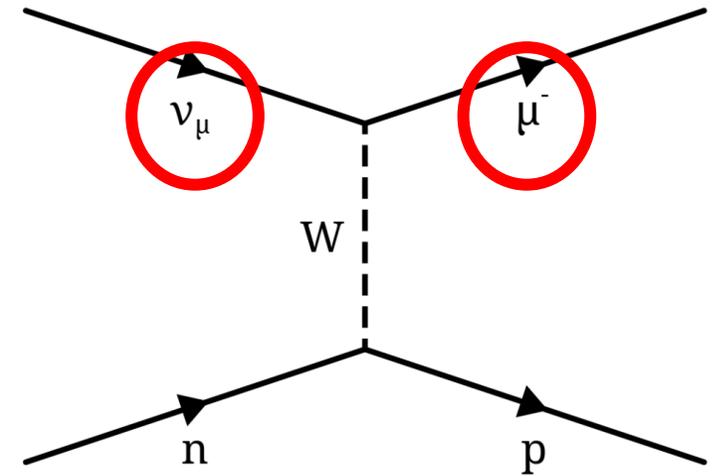
# Neutrino Interaction

We can't measure neutrino itself as they interact only weakly.

In neutrino interaction of **Charged Current** charged lepton is produced.

We have to try to measure neutrino Energy using product of interaction.

If we observe **muon** (**electron**) this means **muon** (**electron**) **neutrino** interacted.

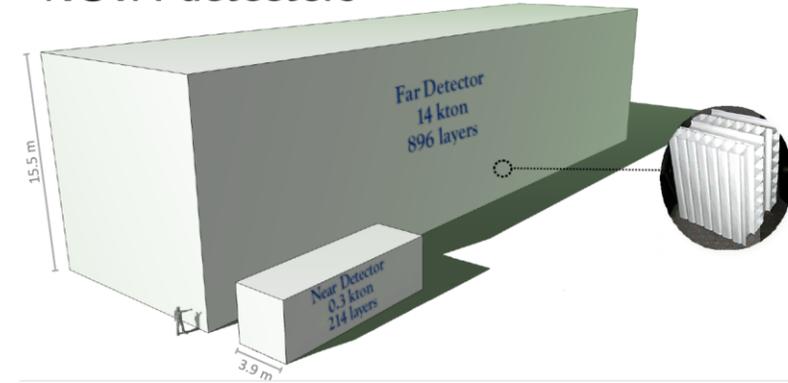


# Reconstructing Neutrino Energy - NOvA

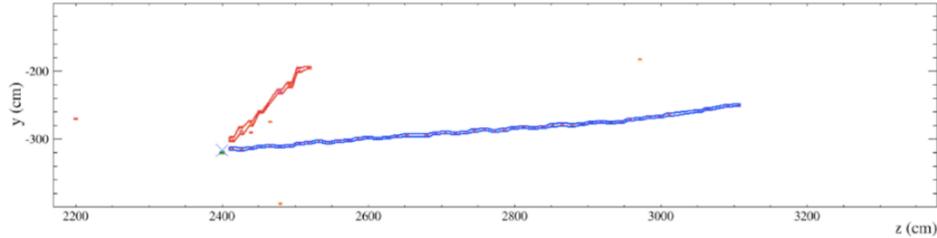
## NOvA detector

- Consist of extruded plastic cells with alternating vertical and horizontal orientation for 3D reconstruction of neutrino interactions

## NOvA detectors

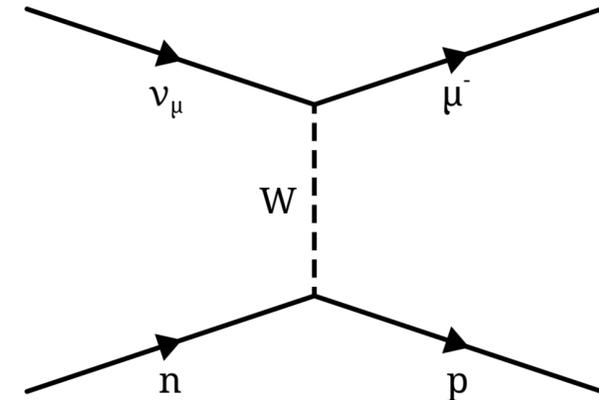


## $\nu_\mu$ energy



$$E_{\nu_\mu} = E_\mu + E_{\text{had}}$$

- $\nu_\mu$  energy is a sum of  $\mu$  energy and hadronic part energy
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- Hadronic energy calorimetric reconstruction
- **What about particles not leaving signal in detector**

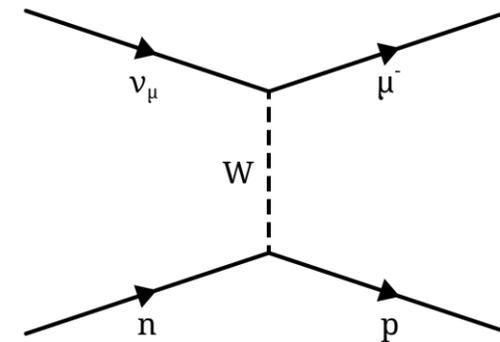
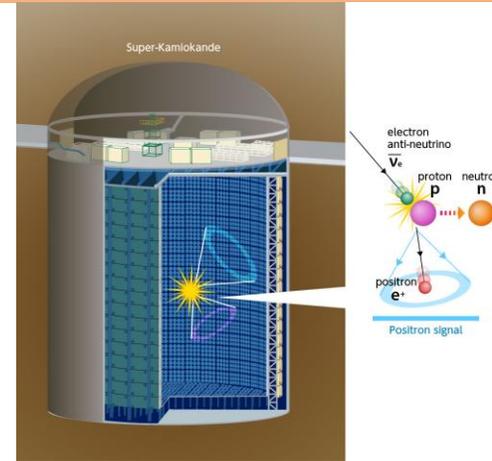
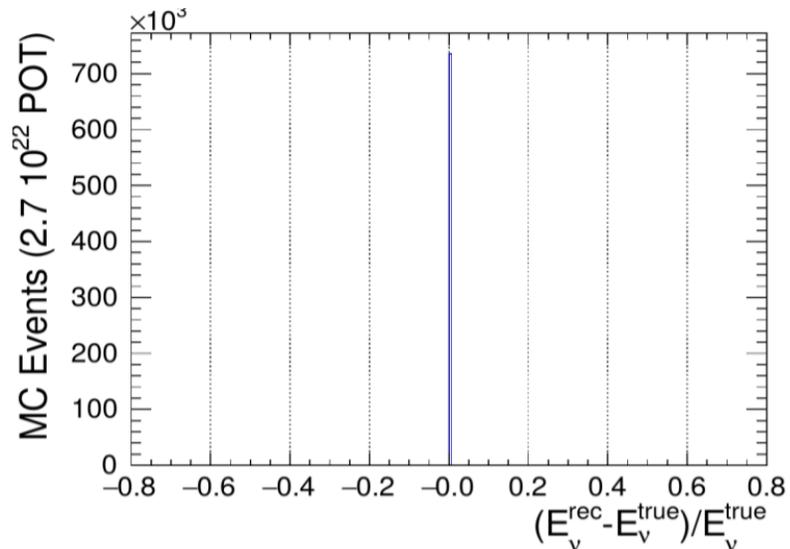


# Reconstructing Neutrino Energy – T2K

Lepton kinematics plays a crucial role in T2K. We may get neutrino energy from the following formula (for two body process):

$$E_{\nu}^{rec} = \frac{m_p^2 - (m_n - E_B)^2 - m_e^2 + (m_n - E_B)E_l}{2(m_n - E_B - E_l + p_l \cos\theta_l)}$$

Only uses **particle masses**, **lepton kinematics** and **nuclear model**.



In ideal situation reconstructed should equal true.

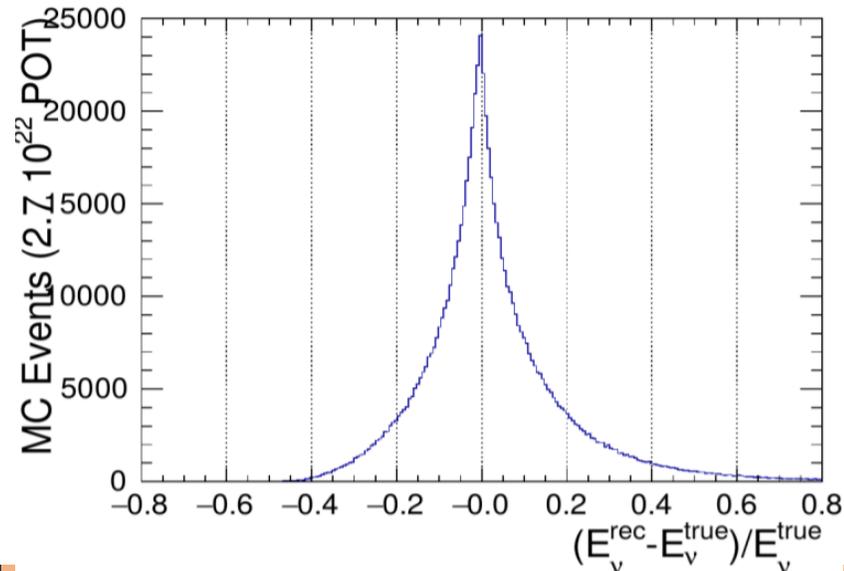
# Reconstructing Neutrino Energy – T2K

T2K far detector is water Cherenkov detector which do not see low energetic proton. Cannot use calorimetric measurement like NOvA

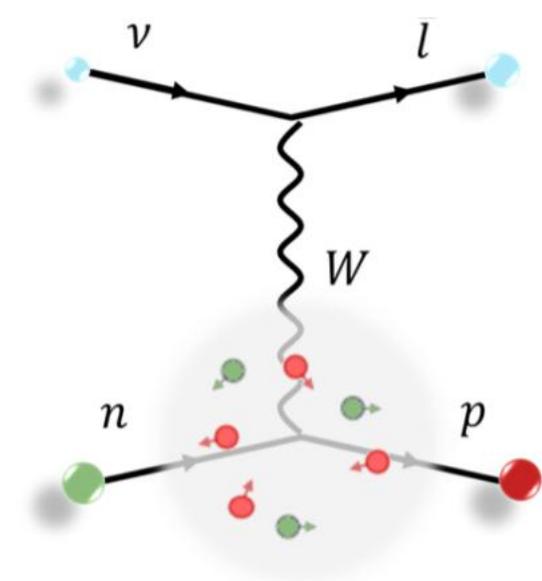
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Neutrino interacts with nucleons in nuclei which smears reconstructed energy due to binding energy and nucleon momentum in nuclei.

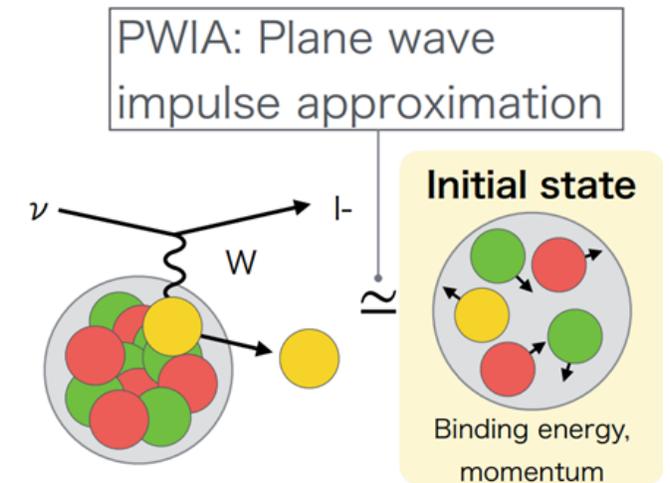
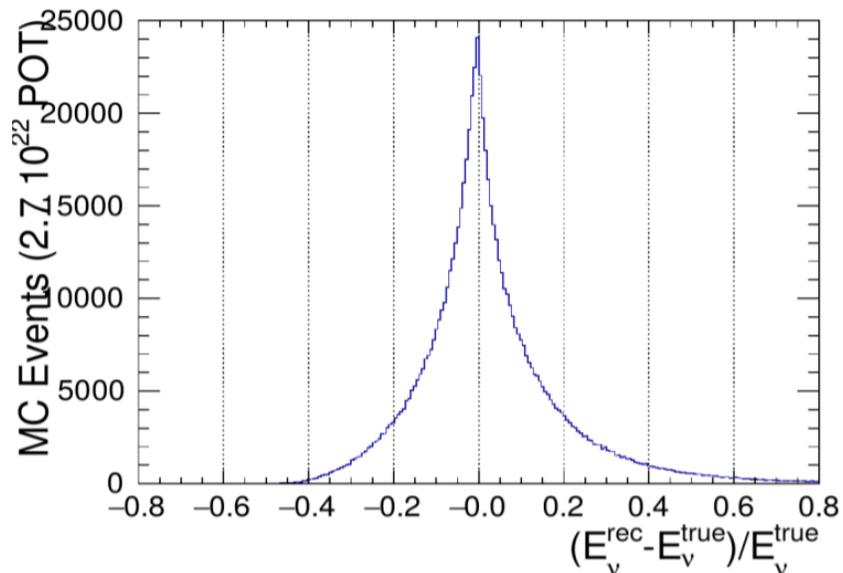
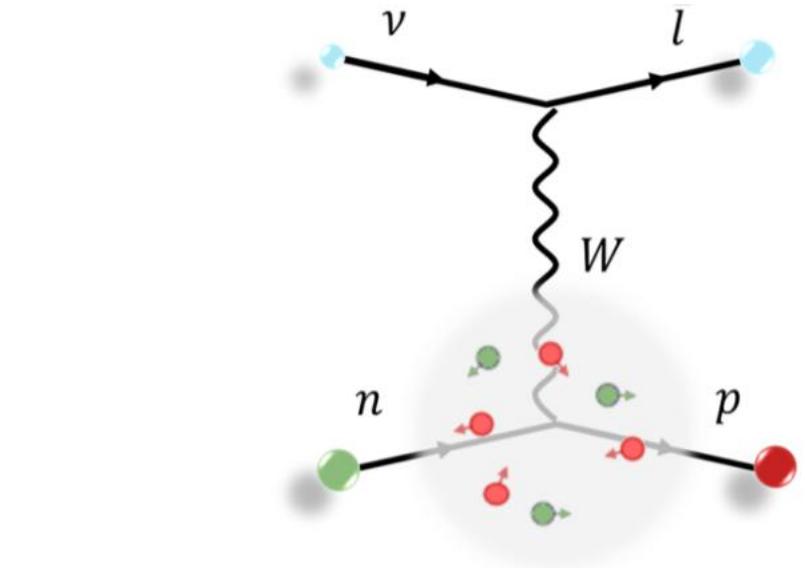


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**One doesn't simply**

**Measure neutrino energy**

# Chapter II: Modelling of Interactions

## Summary

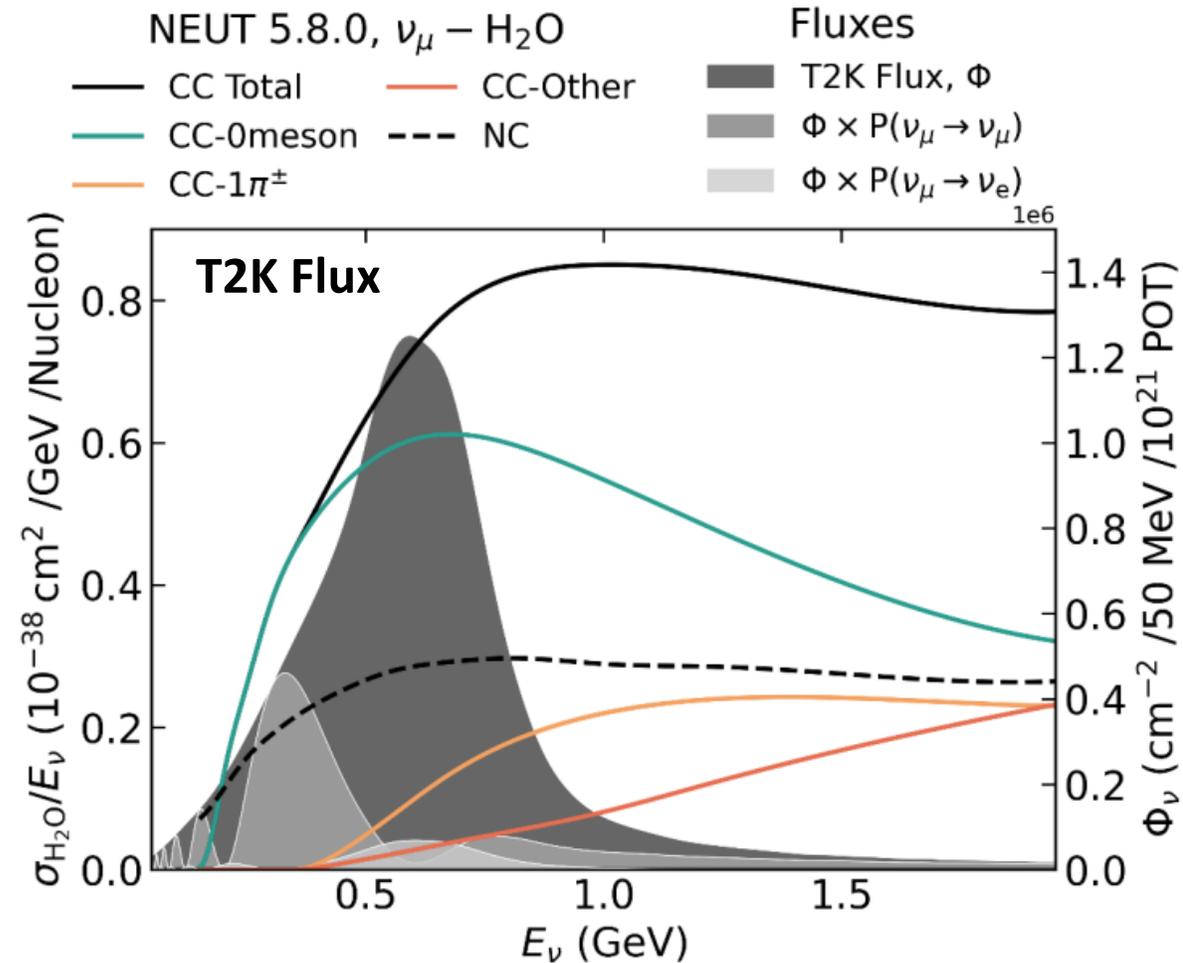
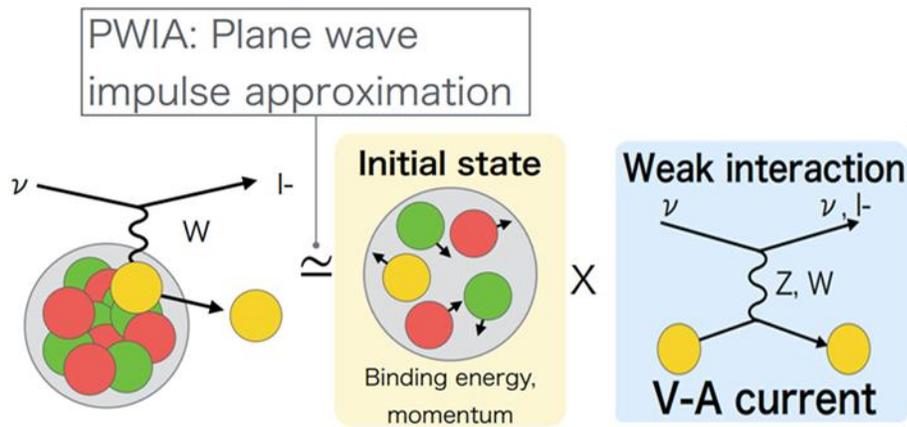
- To measure  $\nu$  oscillation one need only energy
- We can measure Energy using products of  $\nu$  interaction

# Reconstruct Neutrino Energy

Neutrino can undergo several different reactions.

Each reactions use

- Slightly different model
- Different set of uncertainties
- Different challenges

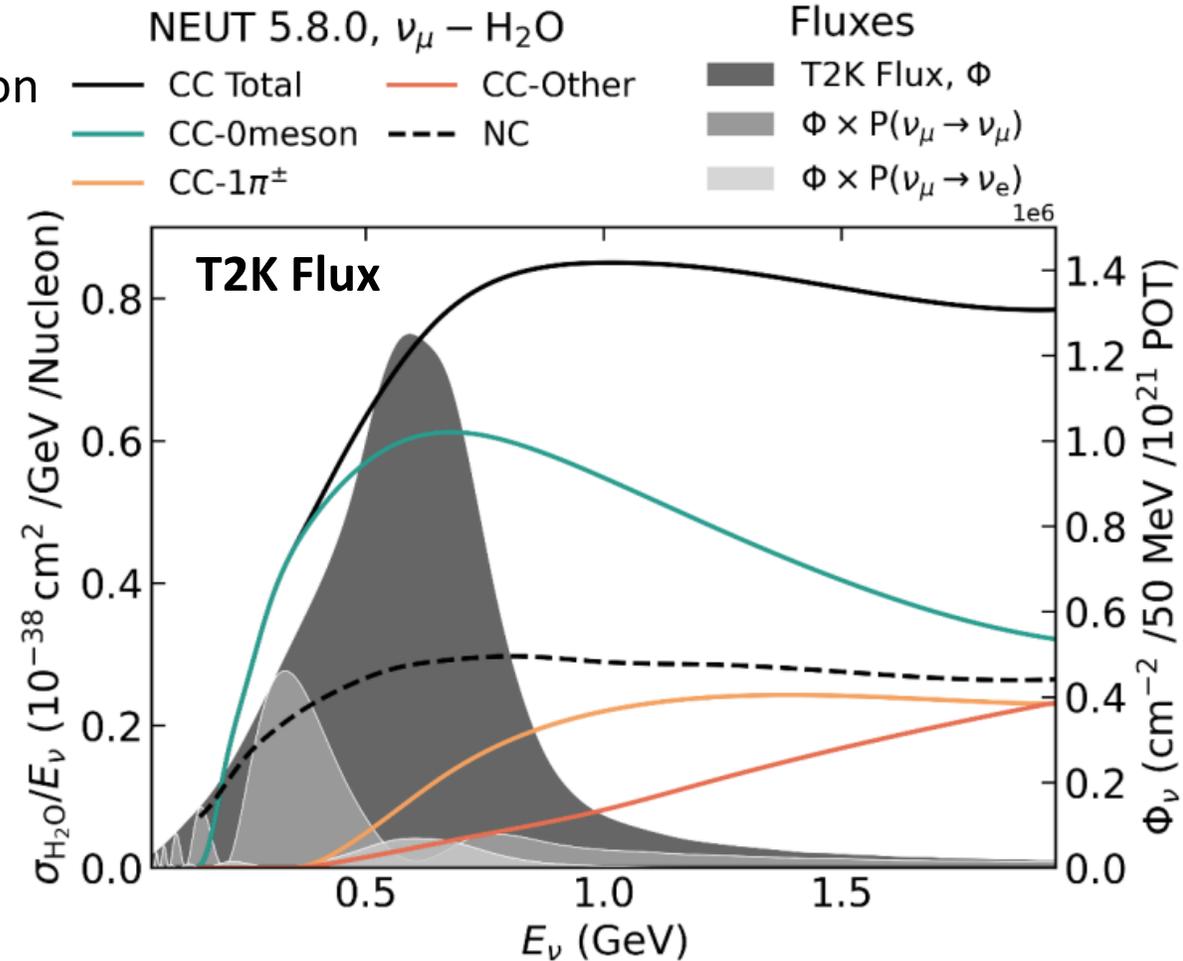
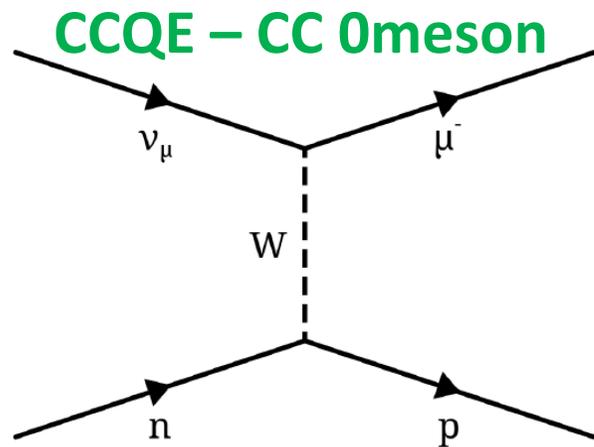
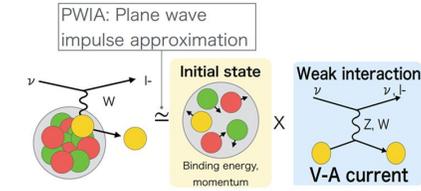


Plot from L. Pickering

# Reconstruct Neutrino Energy

CCQE or CC 0meson.

- Simple topology
- Main signal for T2K and important for energy reconstruction method.

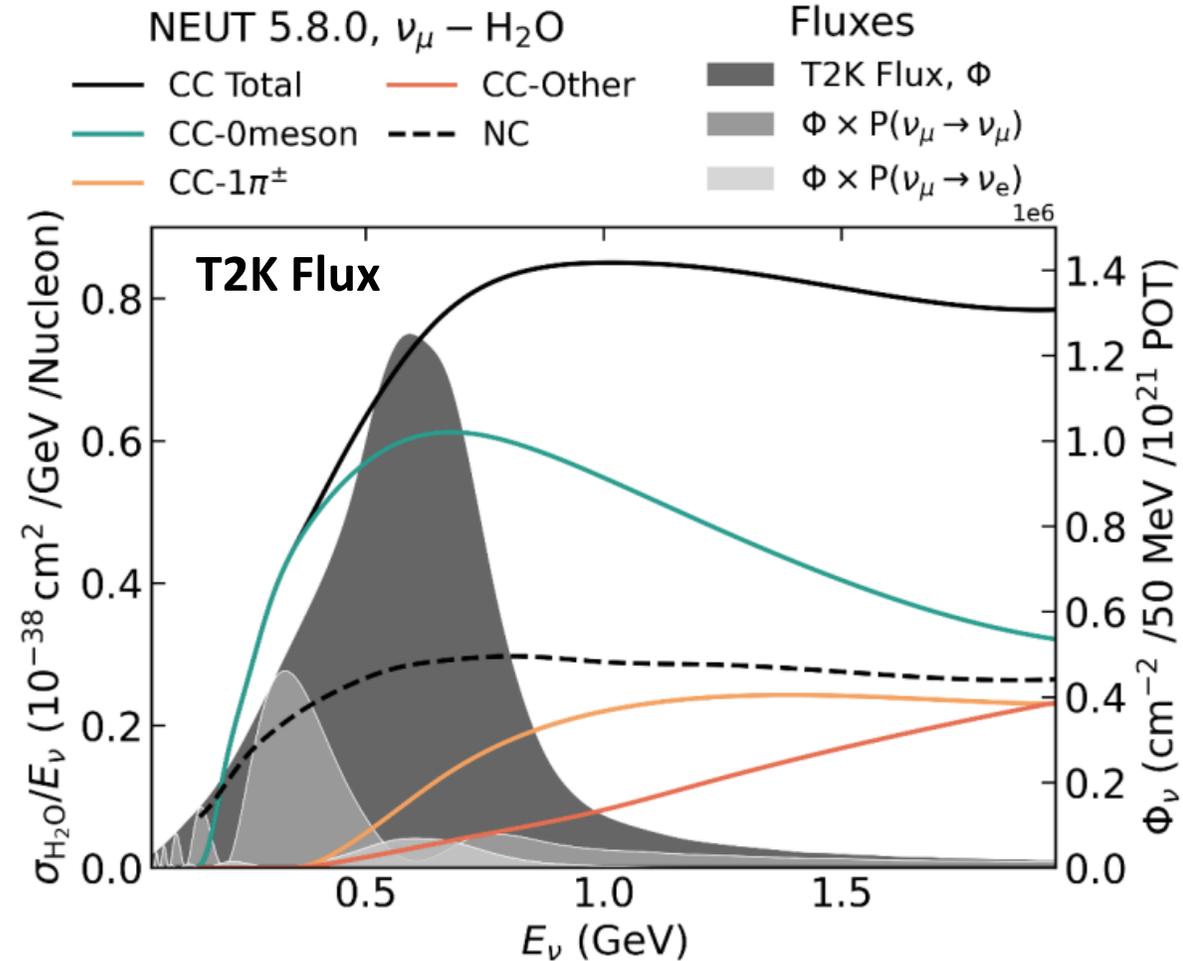
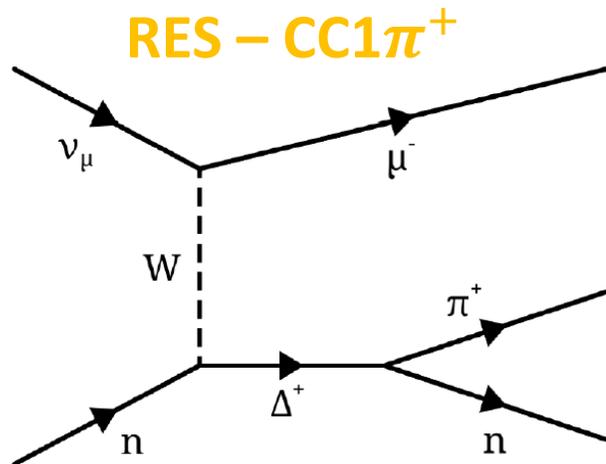
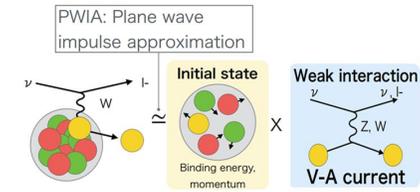


Plot from L. Pickering

# Reconstruct Neutrino Energy

**CC1 $\pi^+$**  - mostly coming through resonance decay.

- Much more difficult due to numerous resonances.
- T2K dominated by very well-known delta resonance.

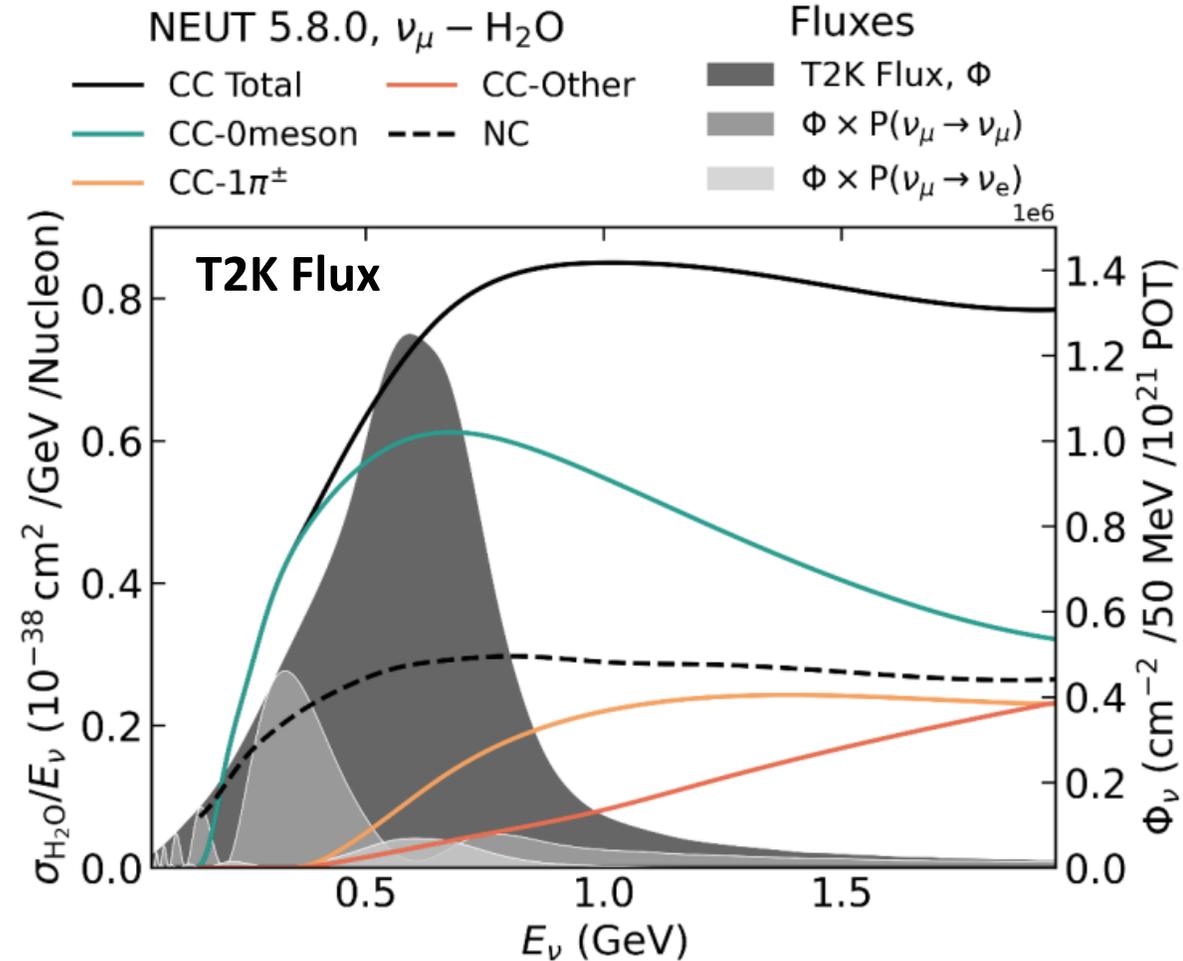
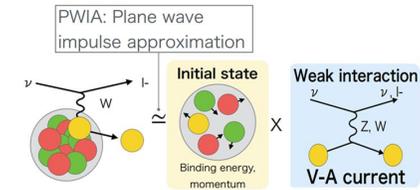
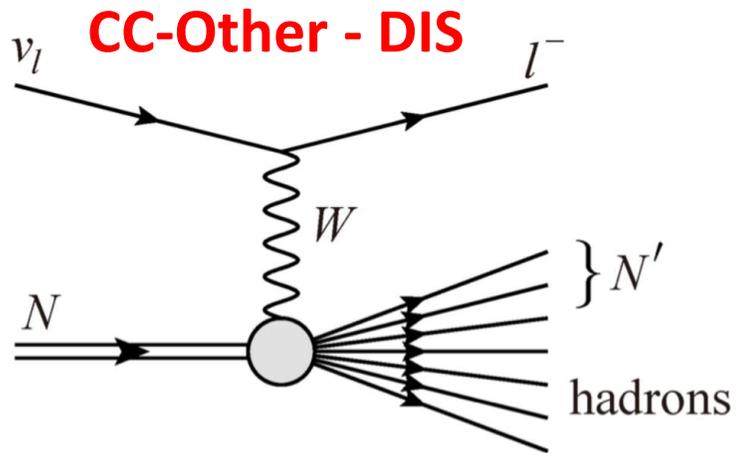


Plot from L. Pickering

# Reconstruct Neutrino Energy

## Shallow and Deep-Inelastic Scattering

- Background for both experiments.
- Very diverse final state.



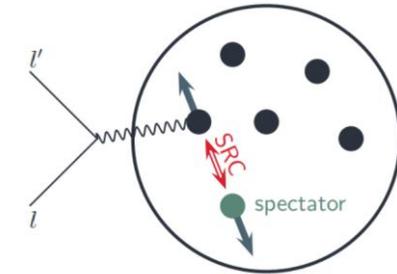
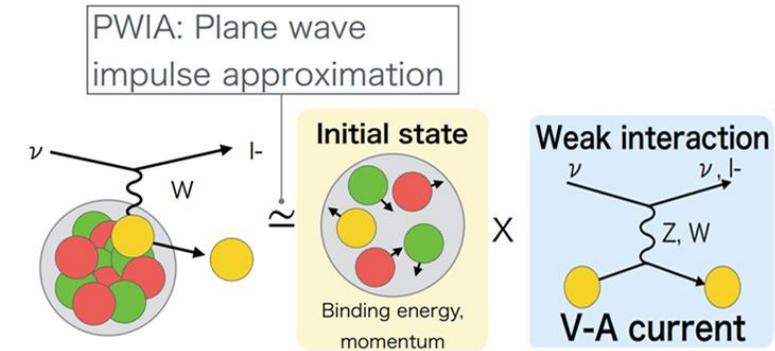
Plot from L. Pickering

# Correlations

Because interaction is happening inside nucleus there can be some inner nucleon correlations.

Then neutrino is interacting with two nucleons and two nucleons are ejected.

Often refers as two particles two holes (**2p2p**).



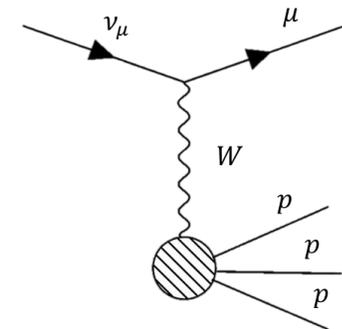
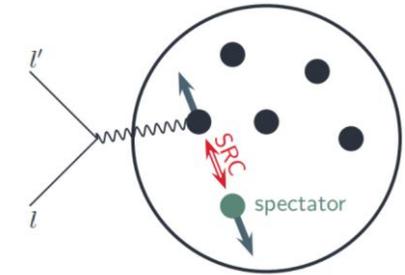
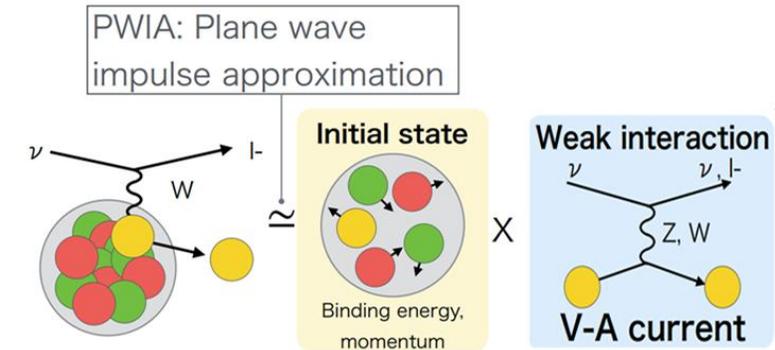
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There can be more correlation resulting in even **3p3h**



# Final State Interactions - Cascade

Up to this point we discussed „initial interaction”

After initial interaction particles have to „leave” nucleus.

We assume billiard ball like interactions often call it cascade

Due to cascade for example pion can be absorbed.

In other words, this means CC1pi+ interaction can be „seen” as CC0pi ☹️

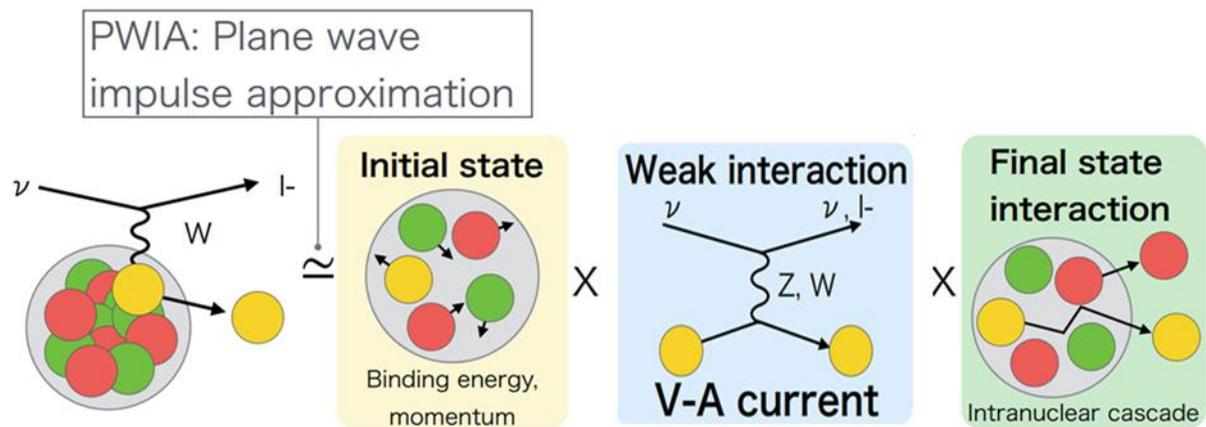
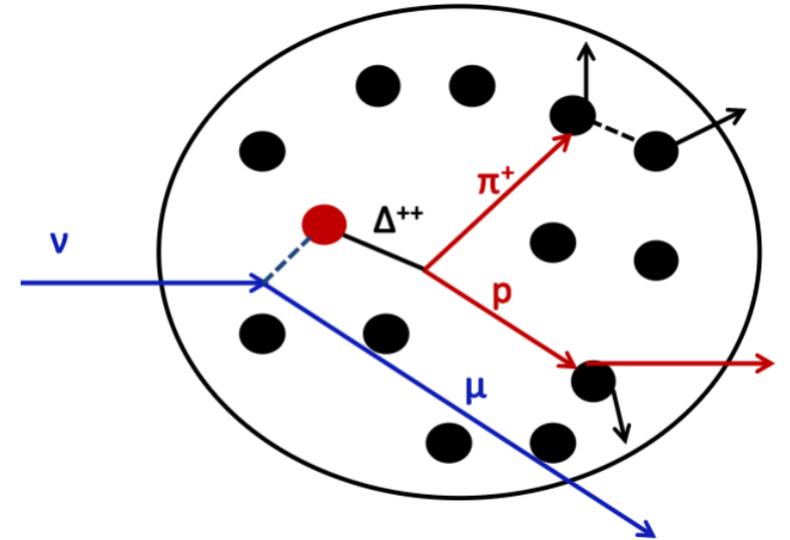


Figure from Seisho

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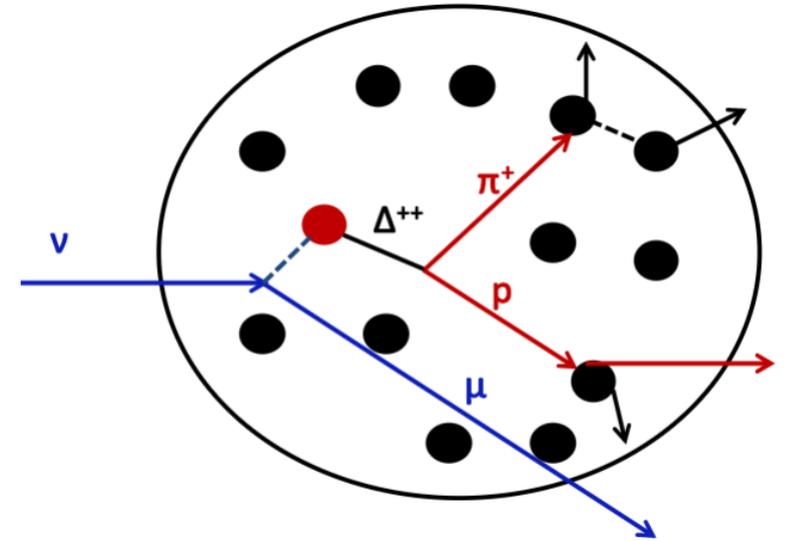
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There is also deexcitation but less important for T2K and NOvA but it becomes more relevant.

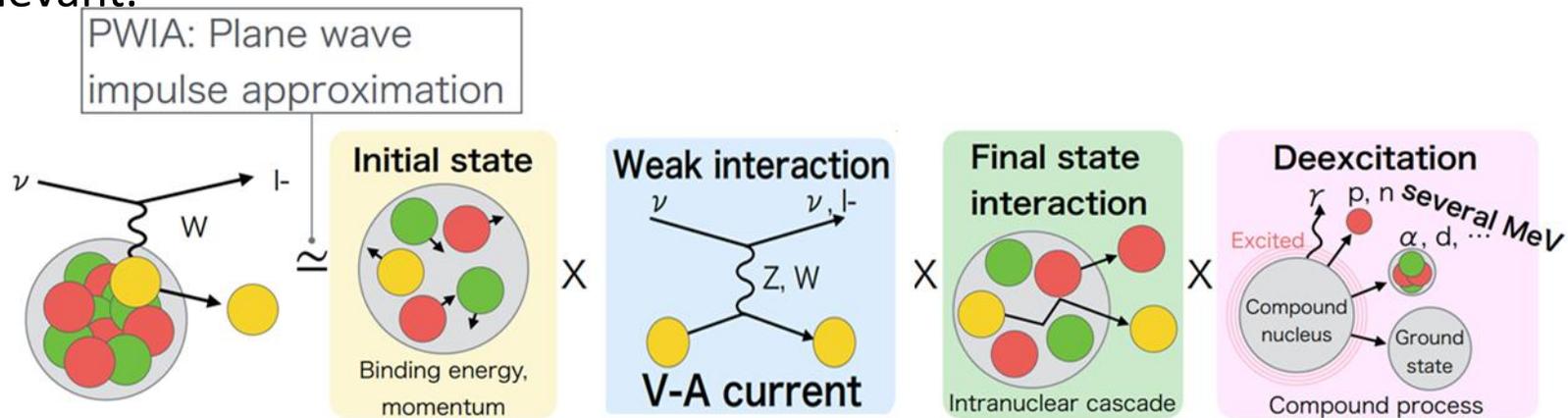
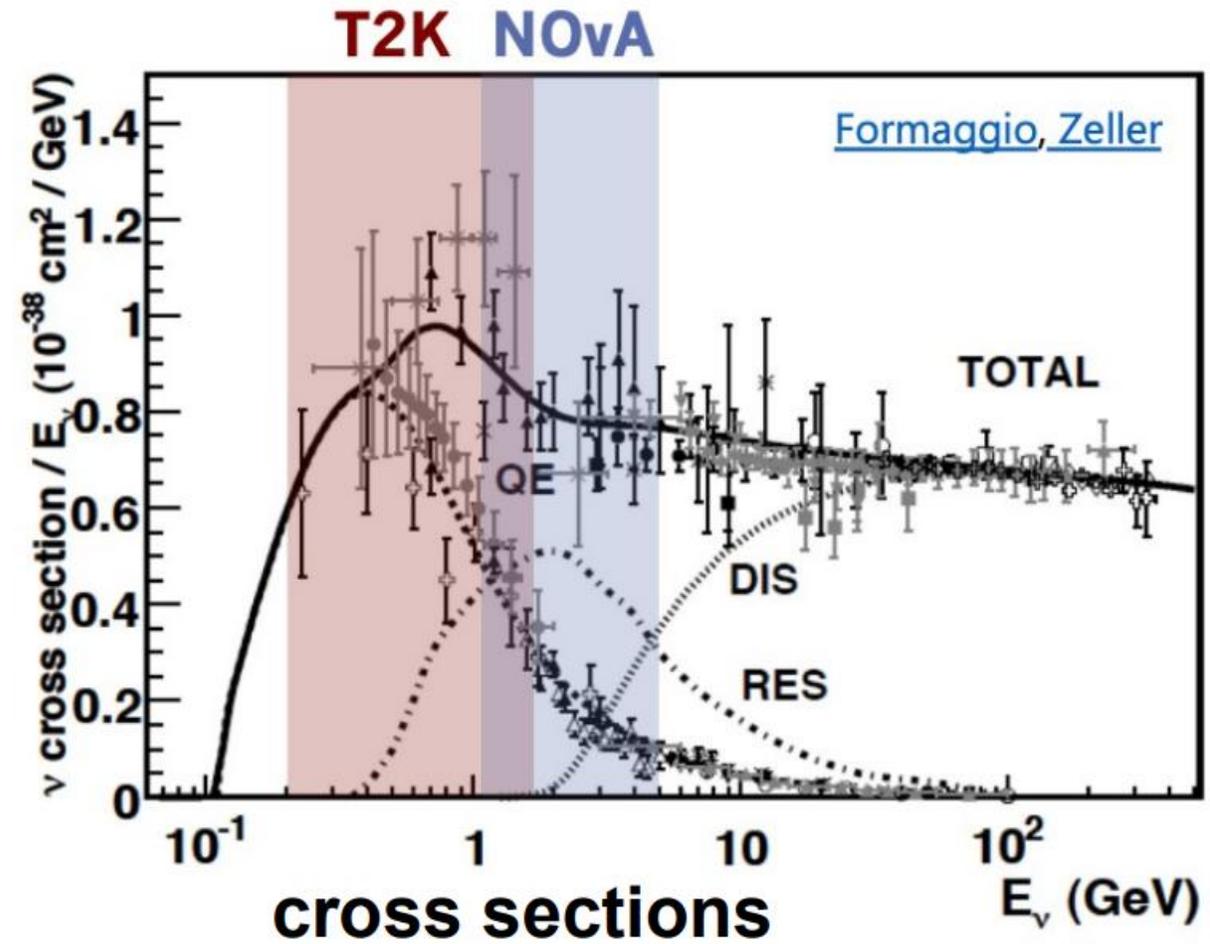


Figure from Seisho

# T2K + NOvA

Due to different neutrino flux, importance of different reaction reactions varies between T2K and NOvA.



# T2K + NOvA

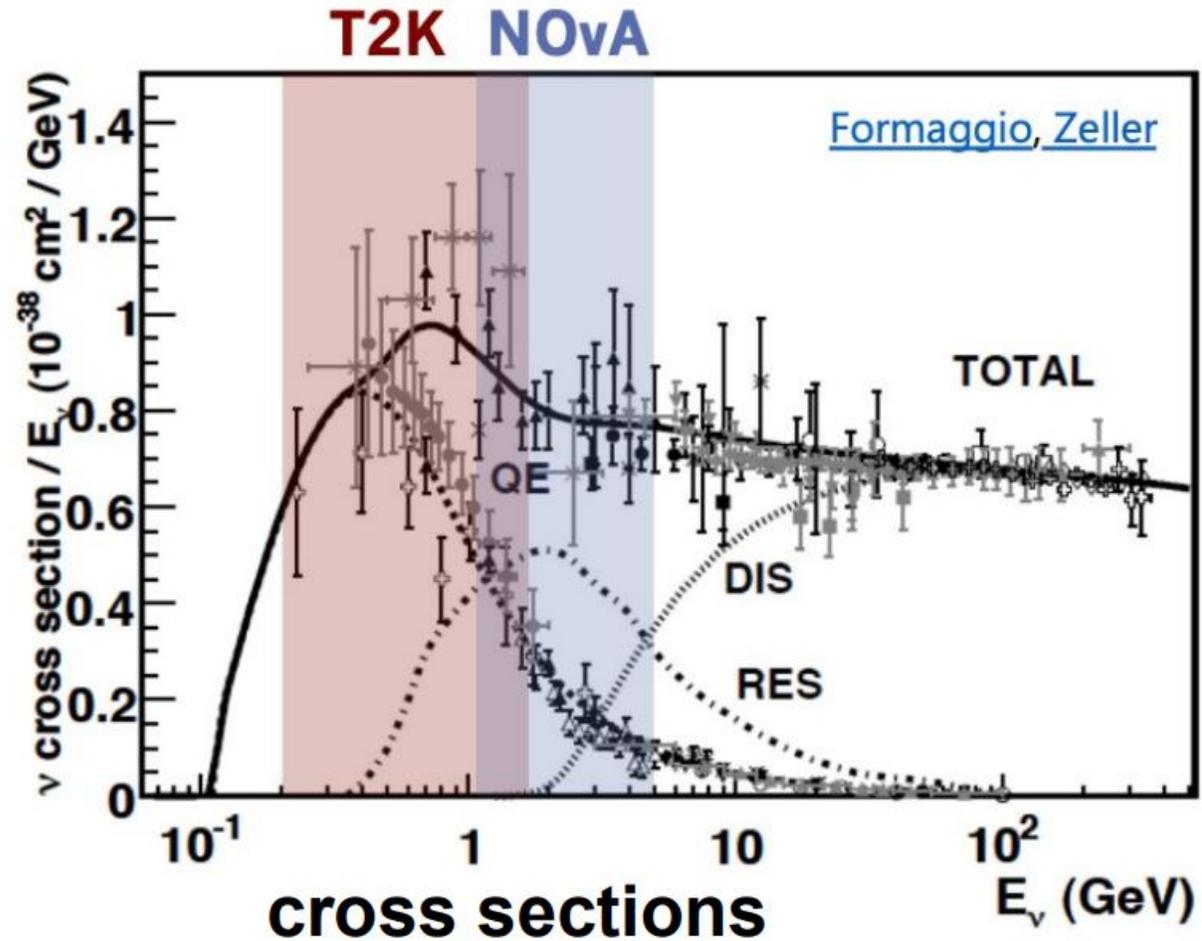
Due to different neutrino flux, importance of different reaction reactions varies between T2K and NOvA.

T2K is much more dominated by CCQE.

This is why T2K can effectively use Erec formula

$$E_{\nu}^{rec} = \frac{m_p^2 - (m_n - E_B)^2 - m_e^2 + (m_n - E_B)E_l}{2(m_n - E_B - E_l + p_l \cos\theta_l)}$$

Only uses **particle masses**, **lepton kinematics** and **nuclear model**.



# Different Neutrino Generators

Neutrino generator have access to different models and vary how consistently modelled are implemented.



NEUT used by **T2K** and other Japanese based experiments

- Development driven by needs of these experiments
- Wide range of processes



GENIE used by **NOvA** and other USA based experiments

- Developed experimentalists and theorists
- Wide range of processes

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Generators have access to different models and vary how consistently modelled are implemented.

In neutrino physics we have wide range access to generators

Allow exploring impact of different effects and analysis biases



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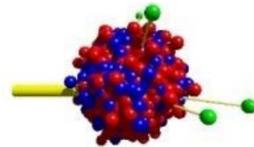
GENIE used by **NOvA** and other USA based experiments

- Developed experimentalists and theorists
- Wide range of processes



NuWro

- Mainly developed by theorists
- Wide range of processes



GiBUU

- Mainly developed by theorists
- Consistent theoretical framework for physics processes



ACHILLES

- Development driven by theorists
- New generator

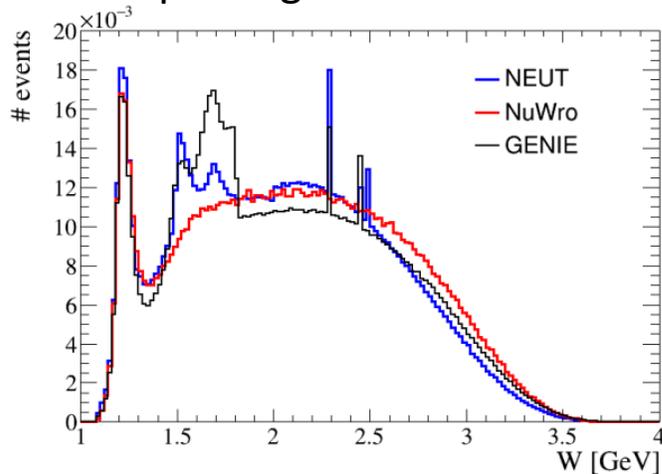
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Example of generator differences



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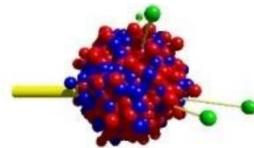
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- Mainly developed by theorists
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- Mainly developed by theorists
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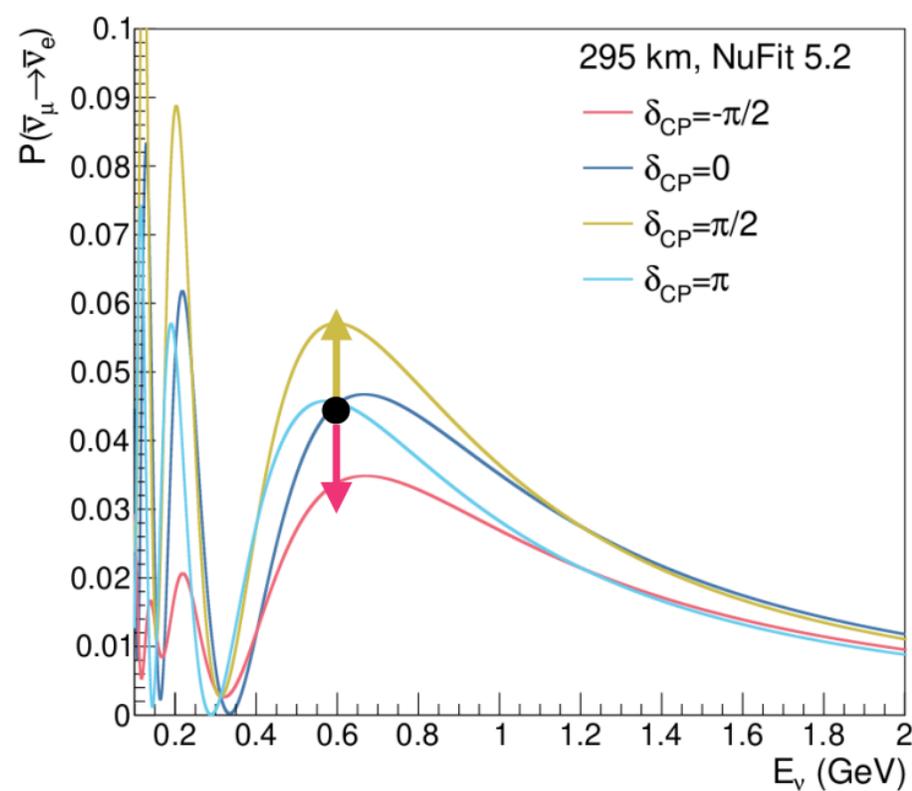
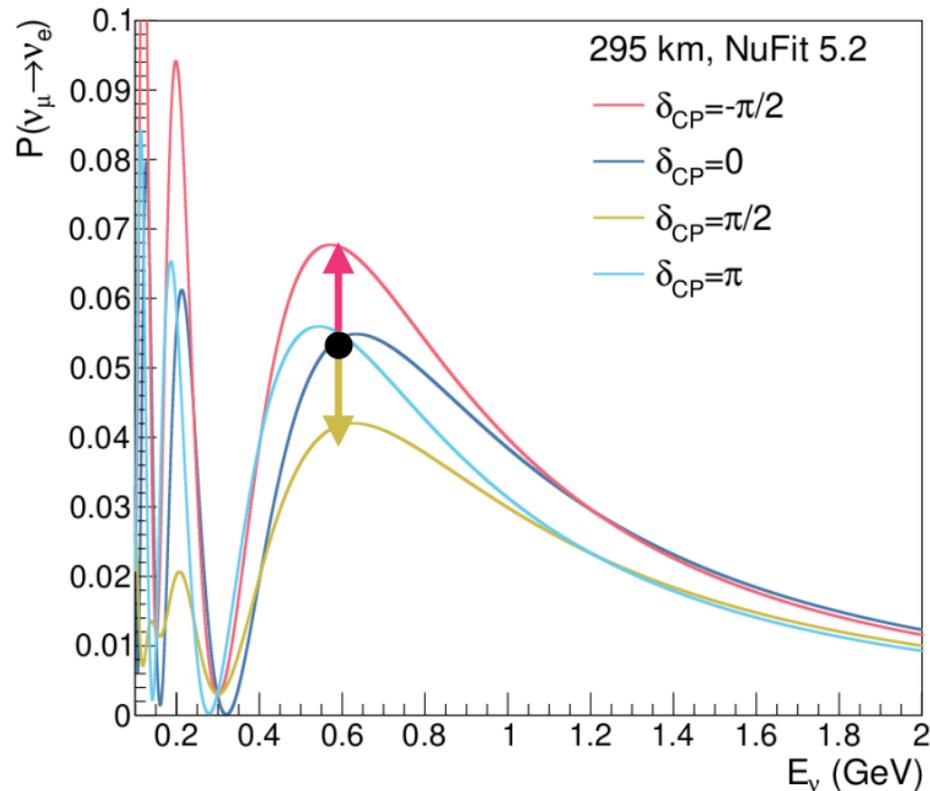


ACHILLES

- Development driven by theorists
- New generator

# Example of mismodeling

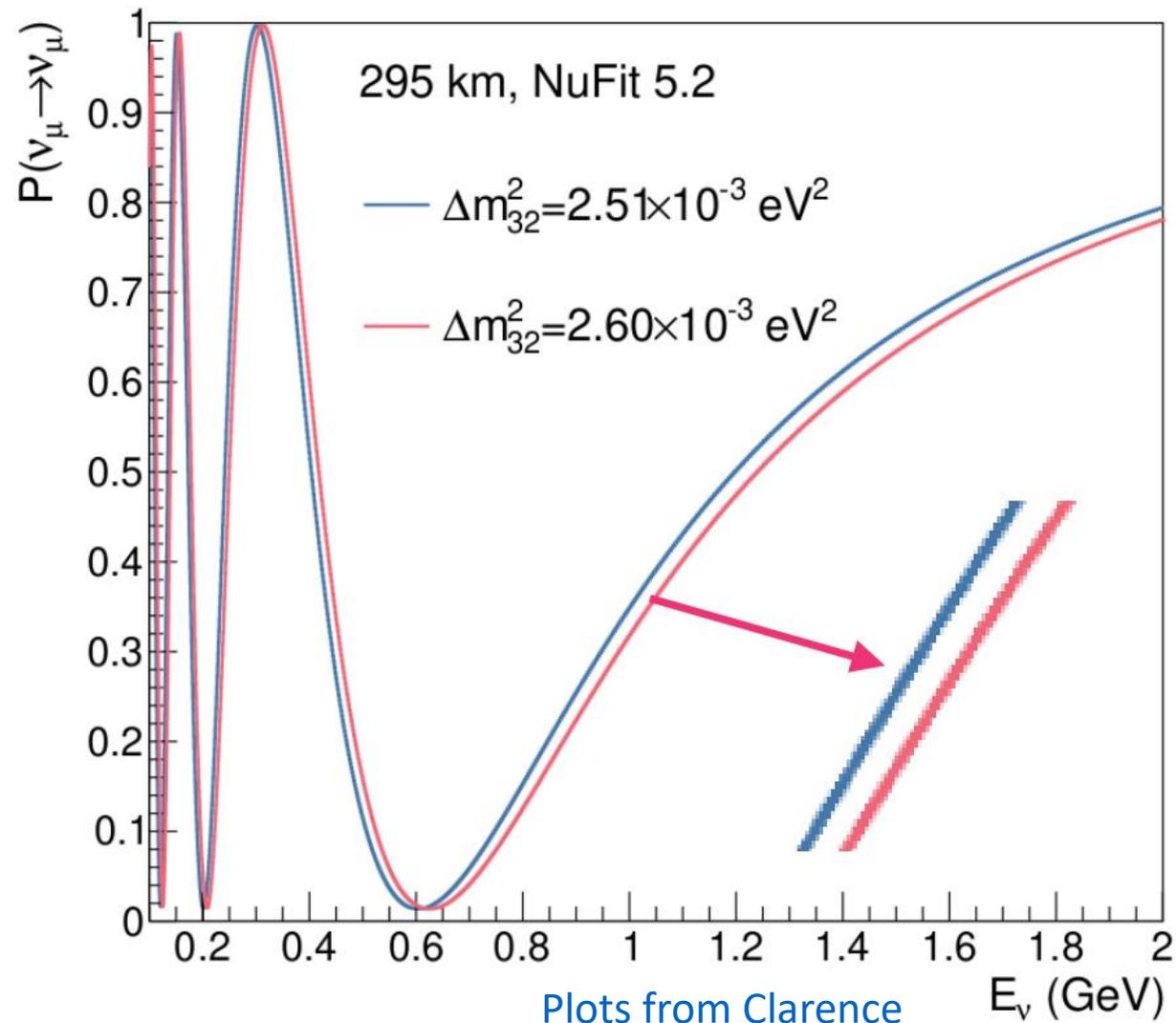
Is the increased rate of CC1e from oscillations?  
Is it a poorly modelled NC1 $\pi^0$  background?  
Is NC1 $\pi^\pm$  mistaken for CC1 $\mu$ ?



[Plots from Clarence](#)

# Example of mismodeling

Is the frequency of the oscillation due to  $\Delta m_{32}^2$ , or biases in neutrino energy reconstruction from mismodelling?



# Chapter III: Electron Scattering

## Summary

- To measure  $\nu$  oscillation one need only energy
- We can measure Energy using products of  $\nu$  interaction
  - Modelling of interactions is difficult 😞

# Electron Scattering - Introduction

- Electron scattering, we have very good control of incoming and outgoing angle and momentum
- Both neutrino and electron scatterings can be simulated using the same nuclear model.
- **A lot of old electron scattering data**

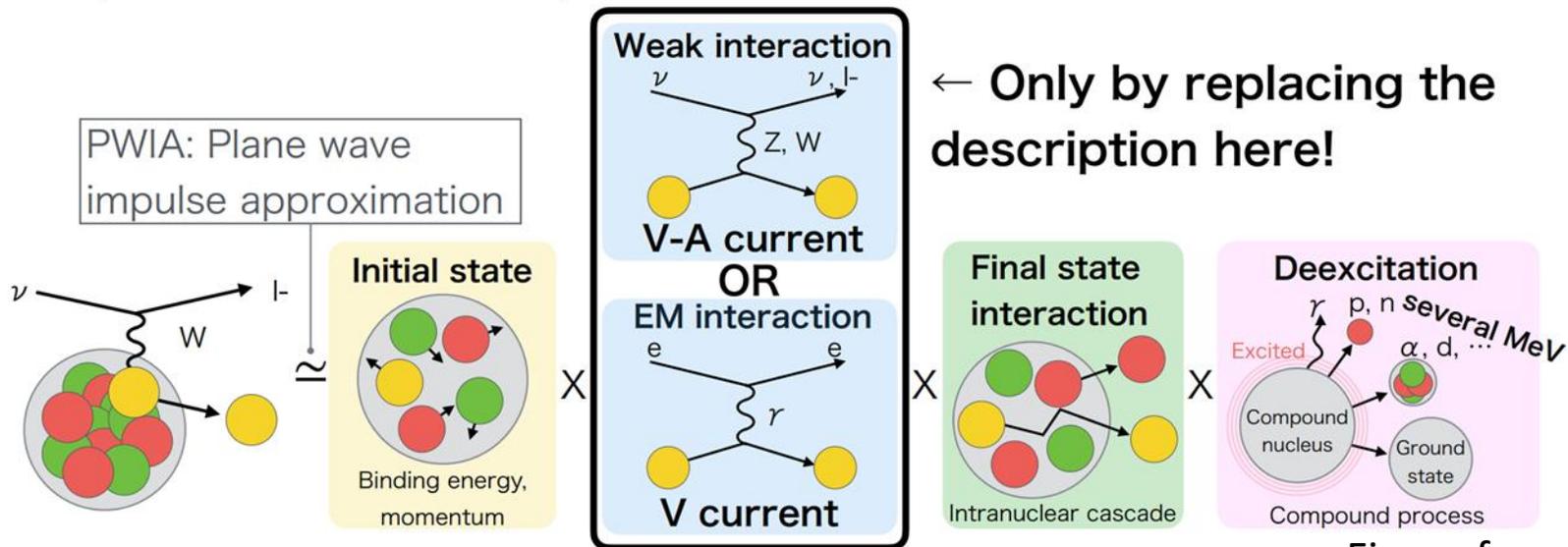
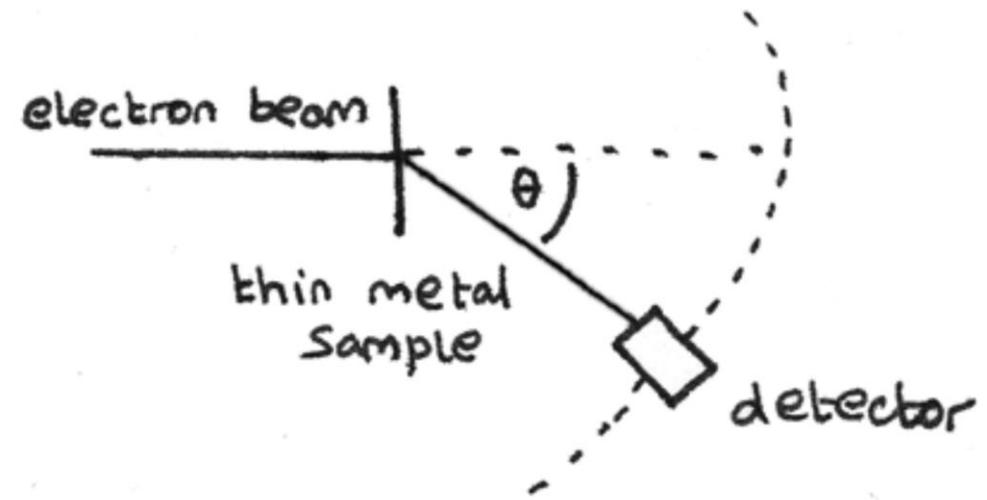
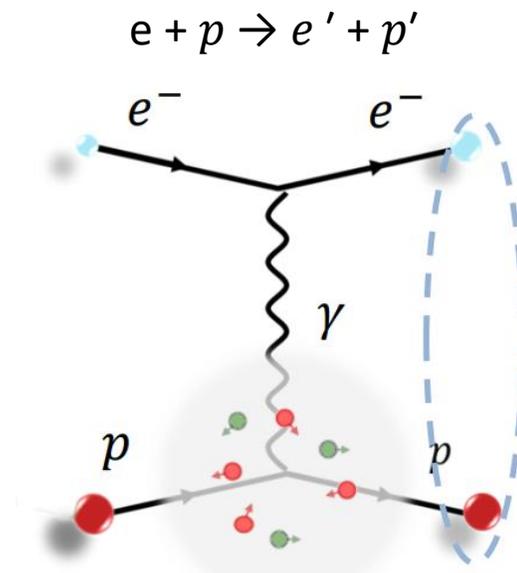
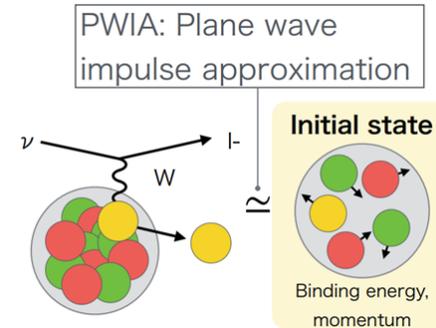
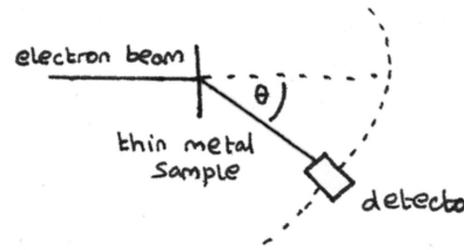


Figure from Seisho

# Improving Initial State Description

We can measure initial state with electron scattering

We know the incoming  $e^-$  – energy / momentum in e-scattering experiments!

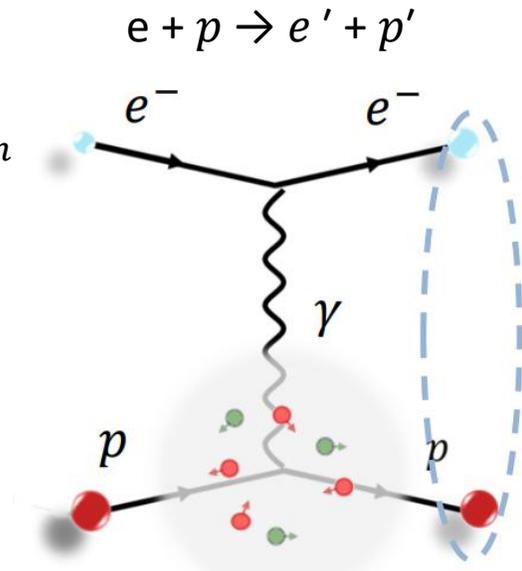
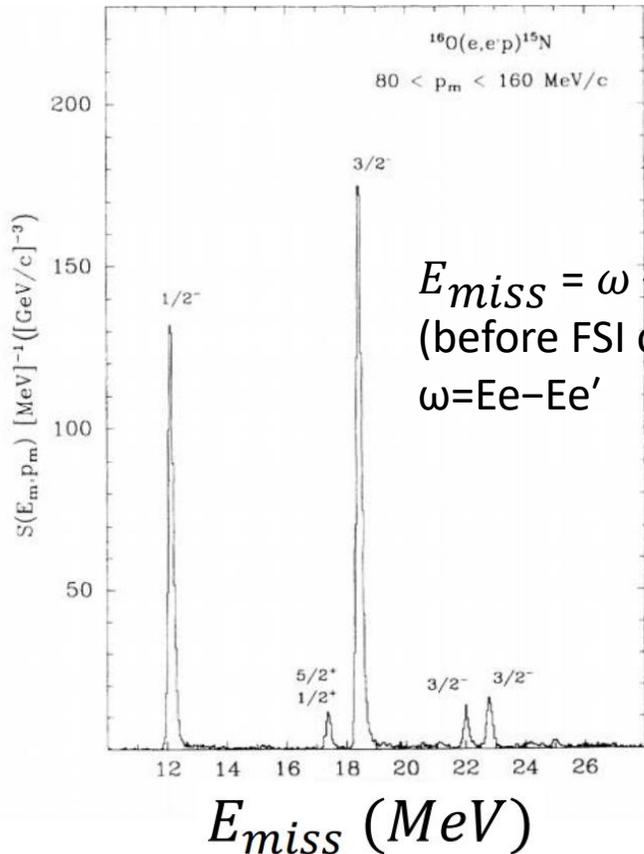
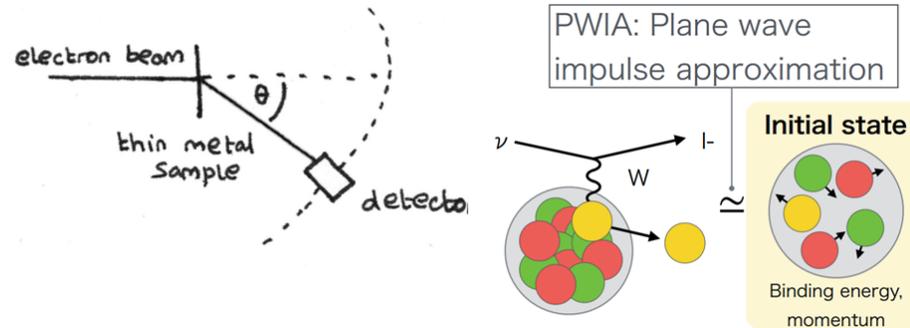


Phys Rev C, **49**, 2 (1994)  
(M. Leuschner et al.)

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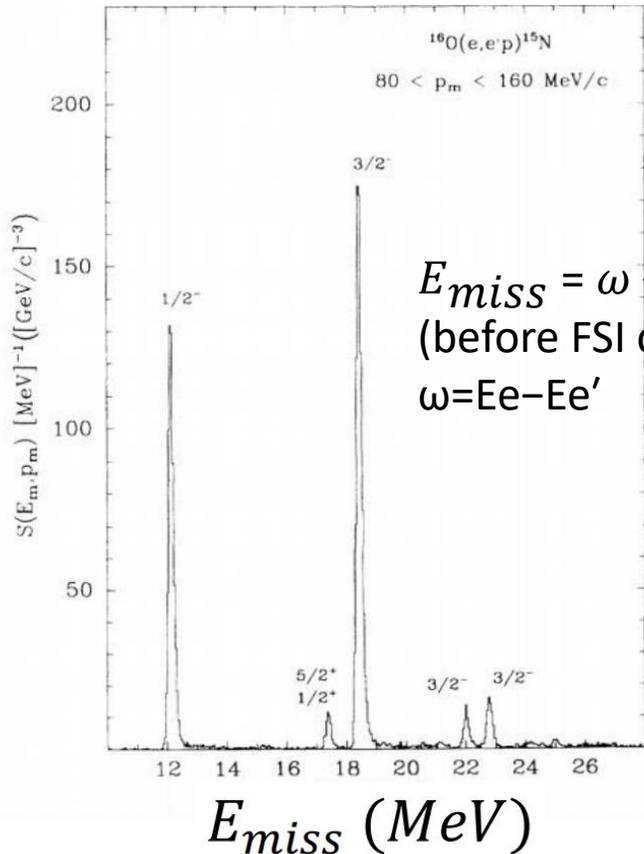
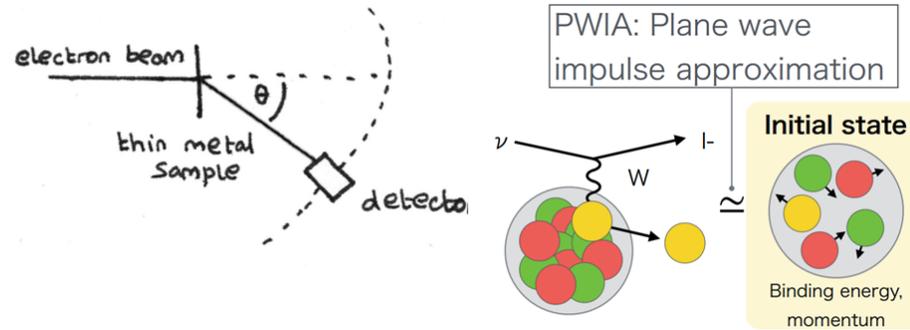
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Based on  
[Stephen's](#)

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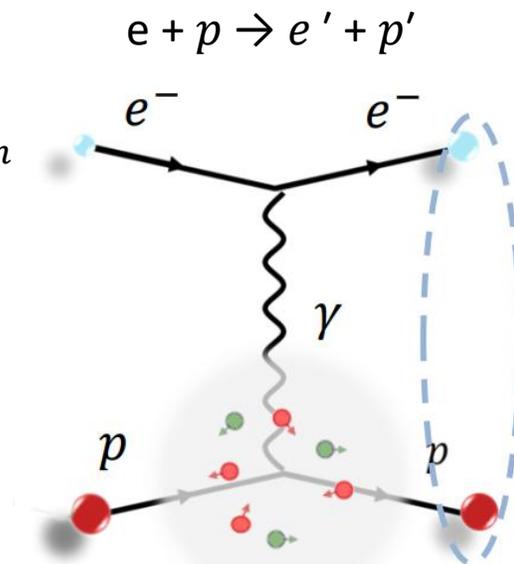
We know the incoming  $e^-$  – energy / momentum in e-scattering experiments!



$$E_{miss} = \omega - T_{p'} - T_{rem}$$

(before FSI corrections)

$$\omega = E_e - E_{e'}$$

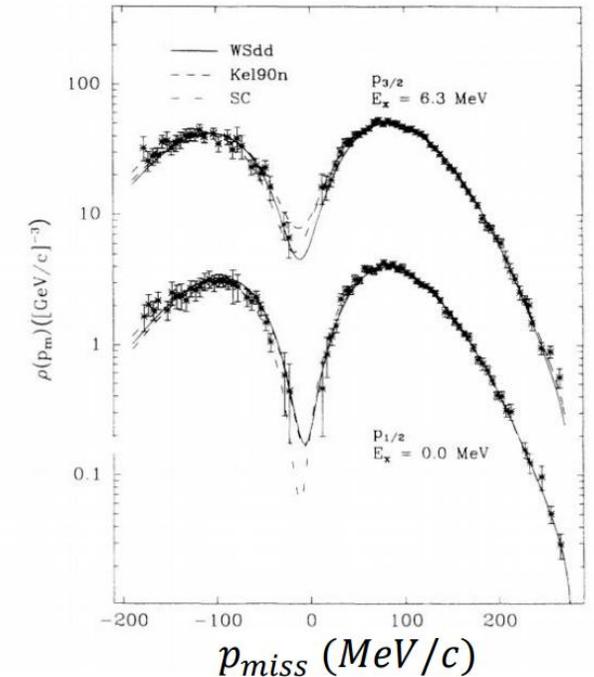


Can get initial state nucleon momentum:

$$p_{miss} = p_e - p_{e'} - p_{p'}$$

Can get initial state nucleon momentum:

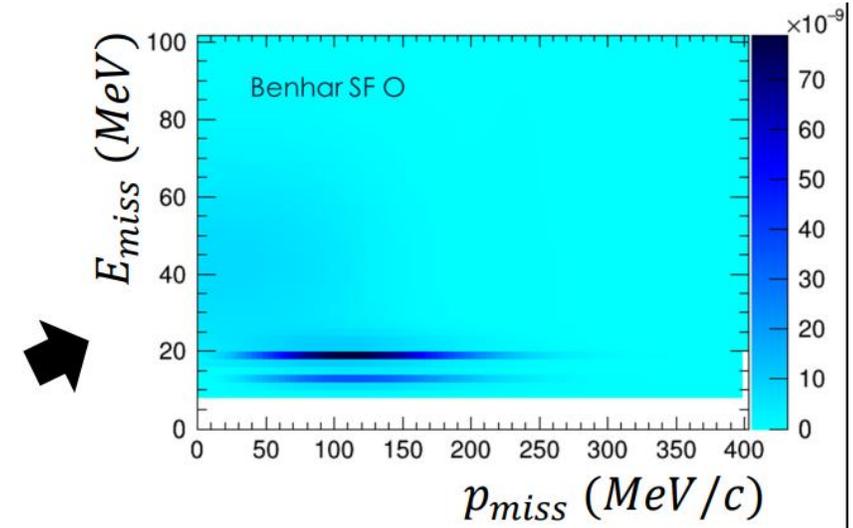
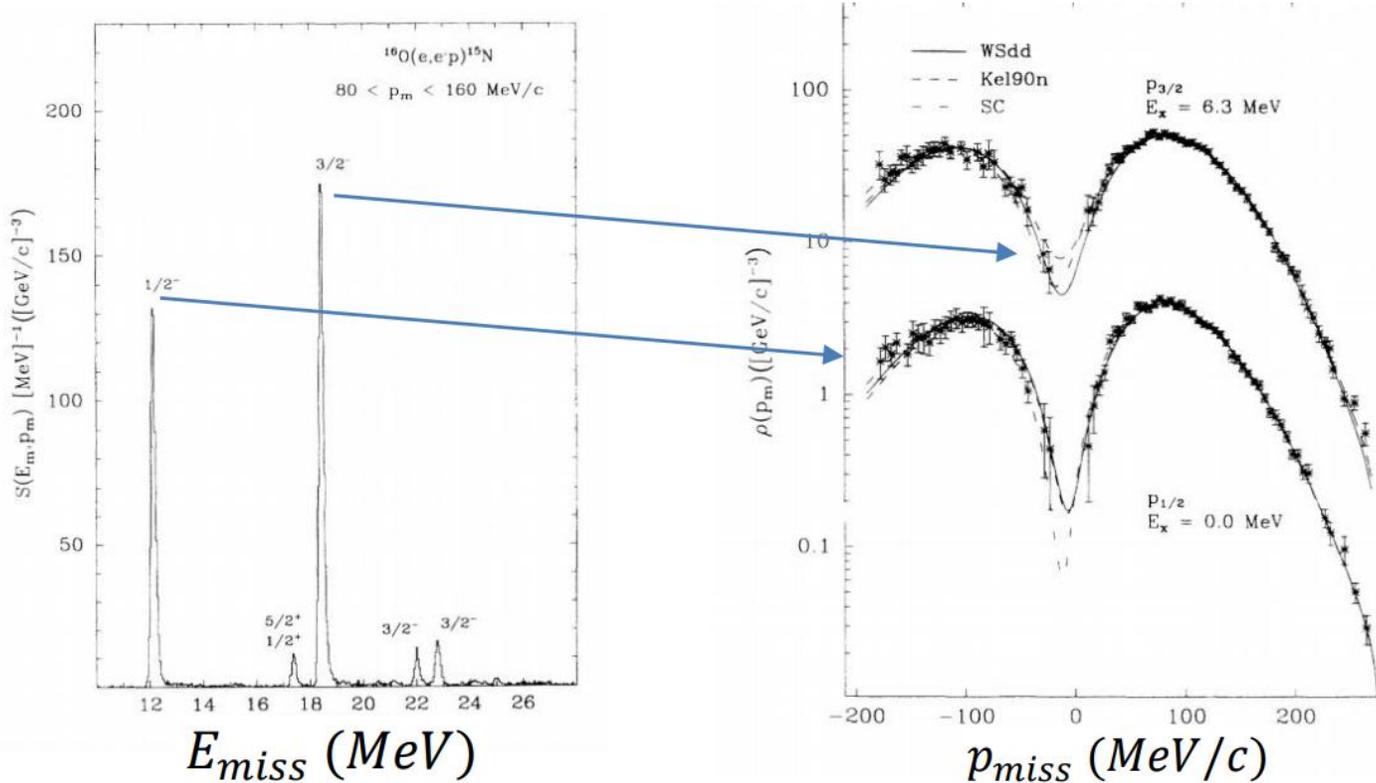
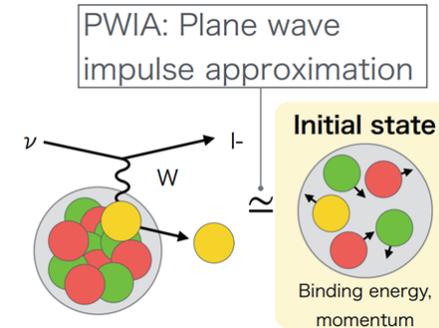
$$p_{miss} = p_e - p_{e'} - p_{p'}$$



Based on [Stephen's](#)

# Improving Initial State Description

Scan through  $E_{miss}$  and measure  $p_{miss}$  (or vice-versa) to build probability of what initial state is.

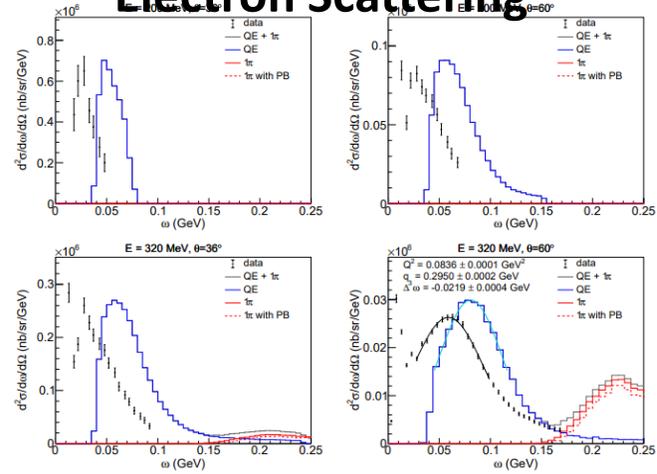


Phys Rev C, **49**, 2 (1994)  
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Based on  
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# Electron Scattering - PWIA

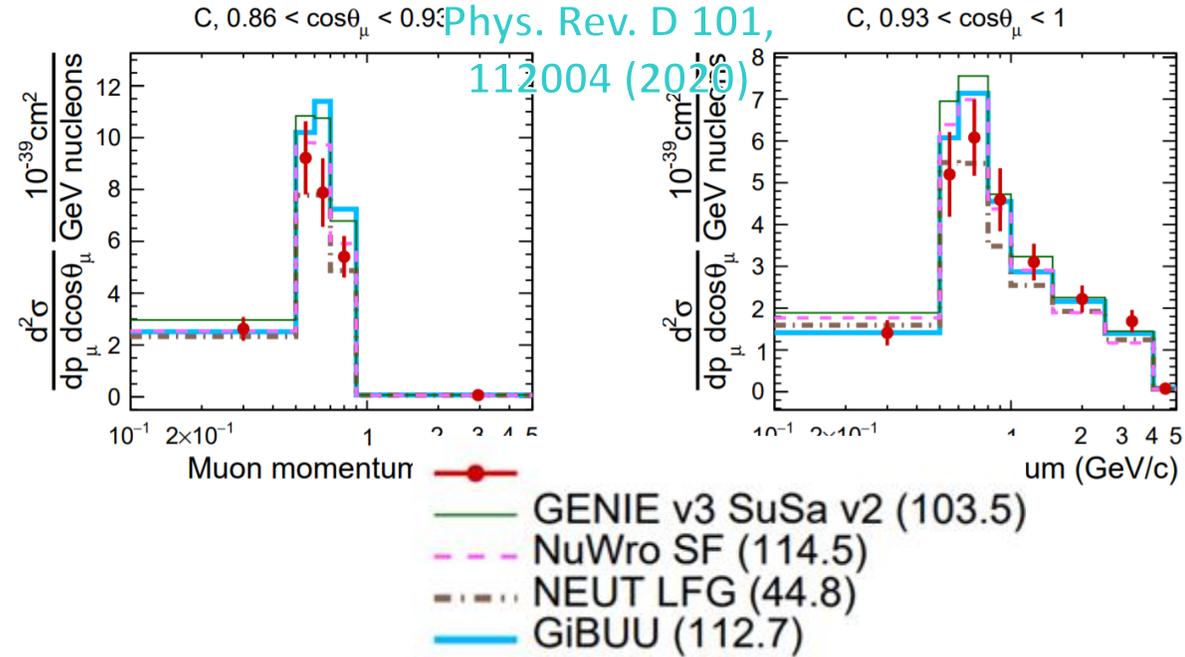
## Electron Scattering



We generally observe large discrepancy using same model between electron and neutrino scattering.

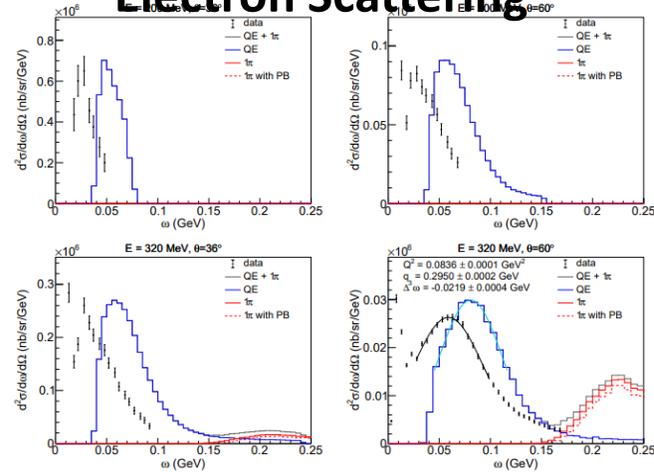
Due to nature of neutrino interactions, we cannot make measurement as precise as electron scattering

## Neutrino Scattering



# Electron Scattering - PWIA

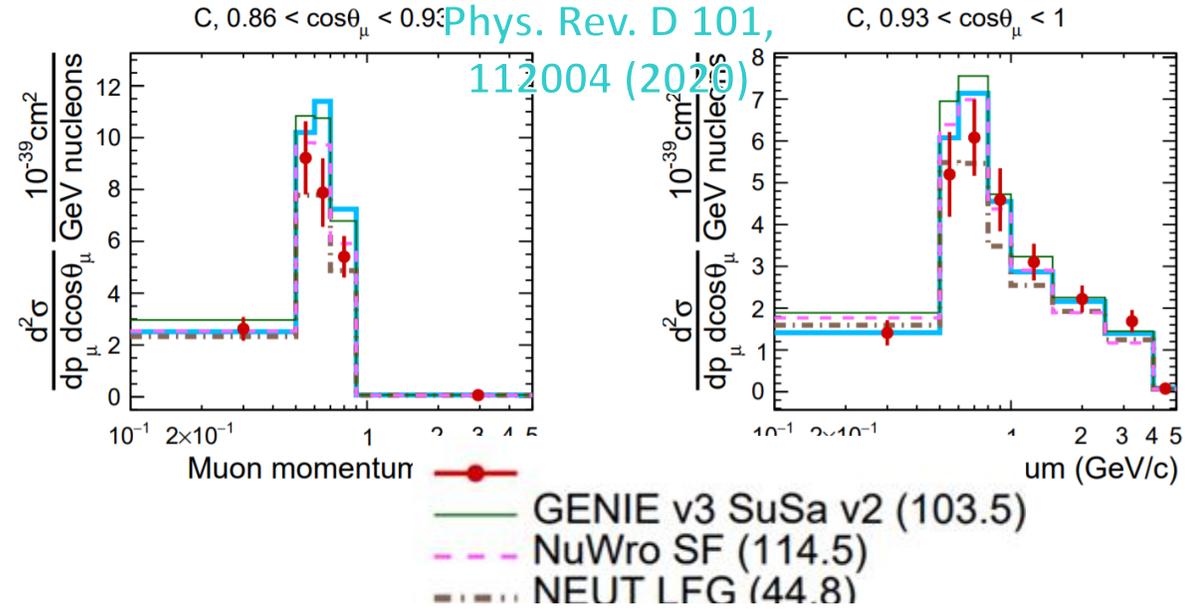
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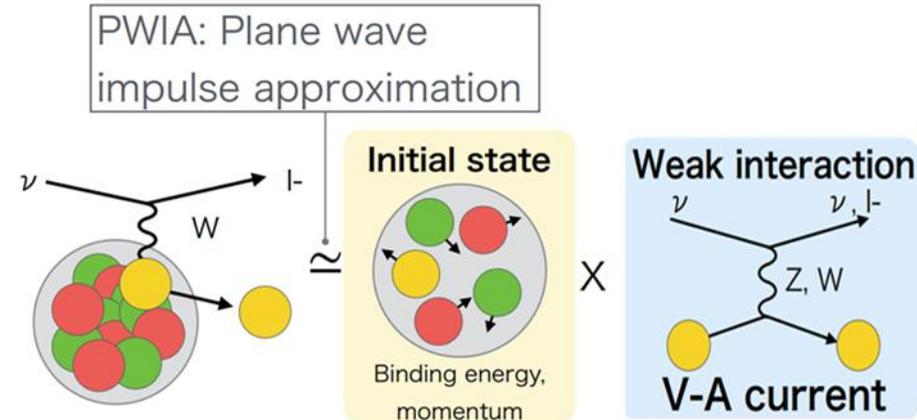
## Neutrino Scattering



Main problem is we used model with Plane Wave Impulse approximation.

Because lepton is travelling through nucleus there are quantum mechanical effects „DISTORTING” wave.

They are very important for low Energy transfer phase-space



# Electron Scattering - DWIA

When accounting for distorted wave and including elastic FSI we can recover mismatch with electron scattering.

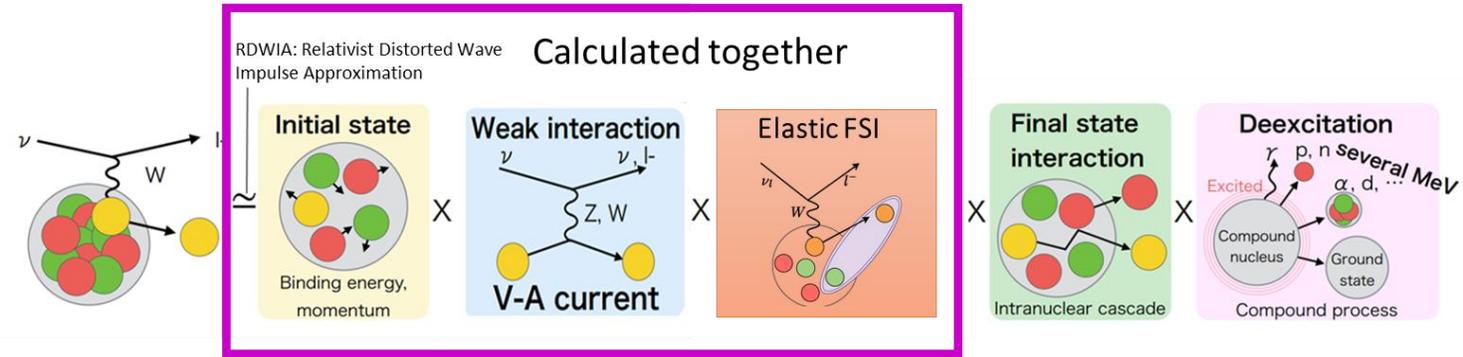
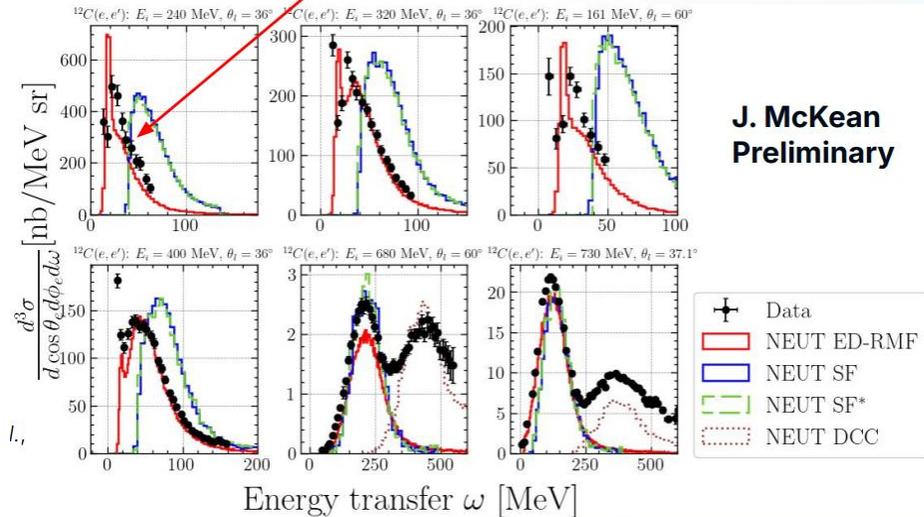


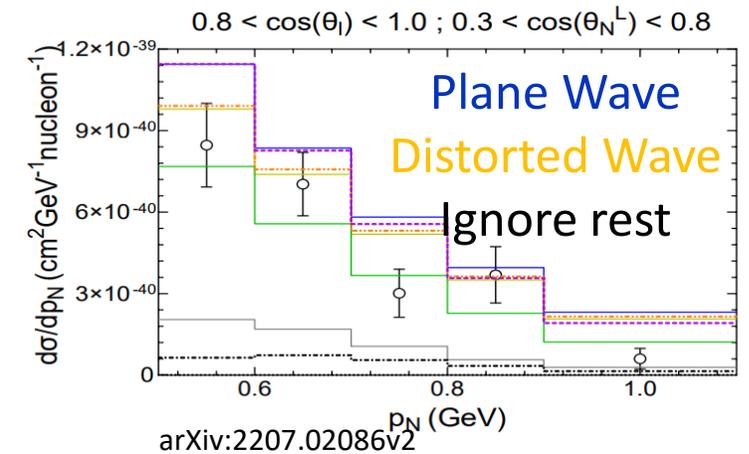
Figure adapted from S. Abe and Jake

## Electron Scattering

Low "q0" mismatch is recovered



## Neutrino Scattering



# Electron Scattering – Summary

- Some data is old from 60/70 errors not understood and hand scanning plots ☹️
- Not every model has ability to switch to electron scattering like popular 2p2h Nieves model ☹️
- Perfect agreement with electron scattering doesn't guarantee great agreement for neutrino ☹️

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- Not every model has ability to switch to electron scattering like popular 2p2h Nieves model ☹️
- Perfect agreement with electron scattering doesn't guarantee great agreement for neutrino ☹️

However

- More and more generators and model have ability to use electron scattering 😊
- There are new collaboration build on providing electron scattering for neutrino measurements 😊
- If model doesn't agree with electron scattering it is very unlikely it will ever agree with neutrino 😊



# Chapter IV: Neutrino Scattering

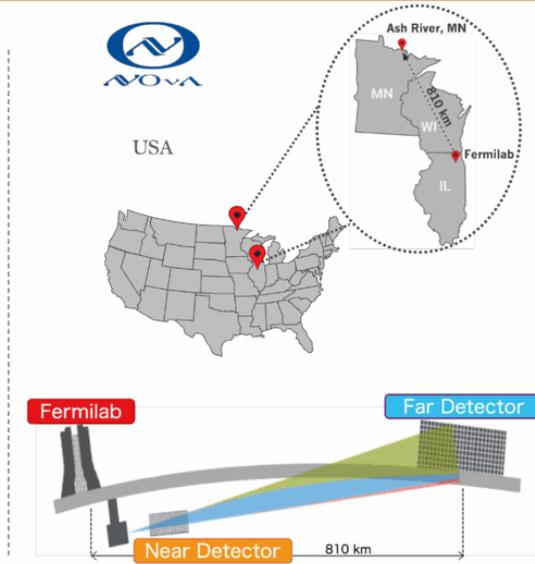
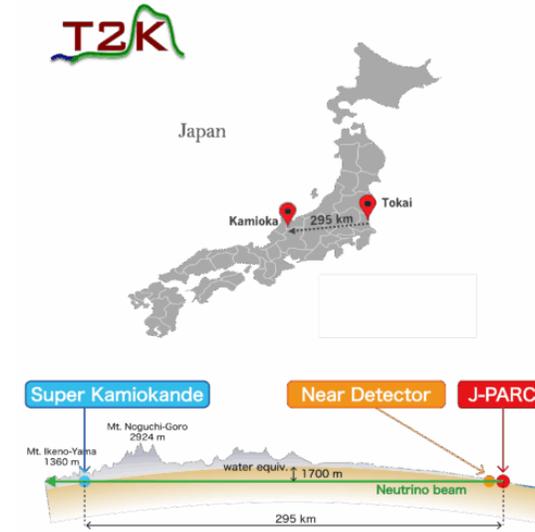
## Summary

- To measure  $\nu$  oscillation one need only energy
- We can measure Energy using products of  $\nu$  interaction
  - Modelling of interactions is difficult 😞
- Using electron scattering to develop better models

# Near Detectors

Both T2K and NOvA have near detector

- Oscillations are negligible (due to small  $L$ )
- Relatively high number of events, order of hundred thousands vs hundreds in Far Detector
- Measure neutrino cross-section
- Constrain fit parameters

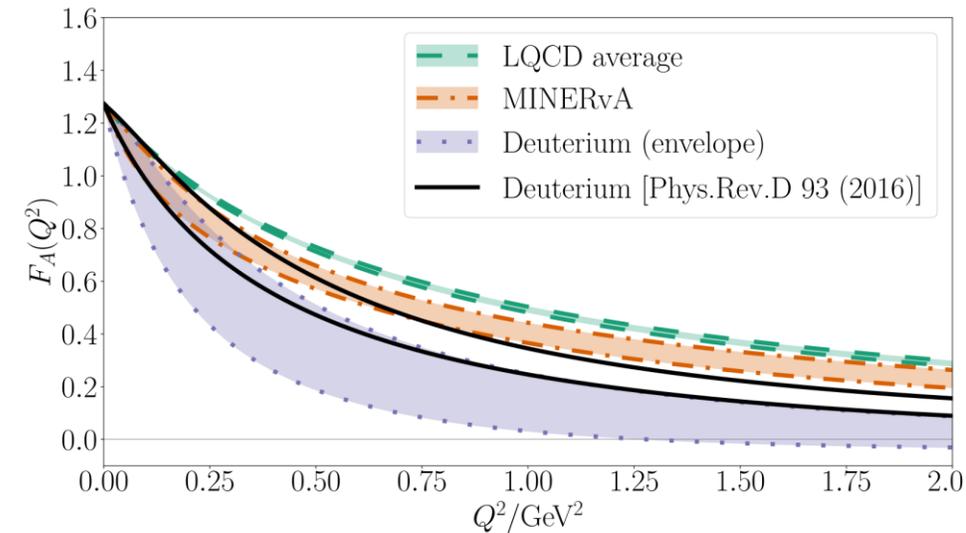
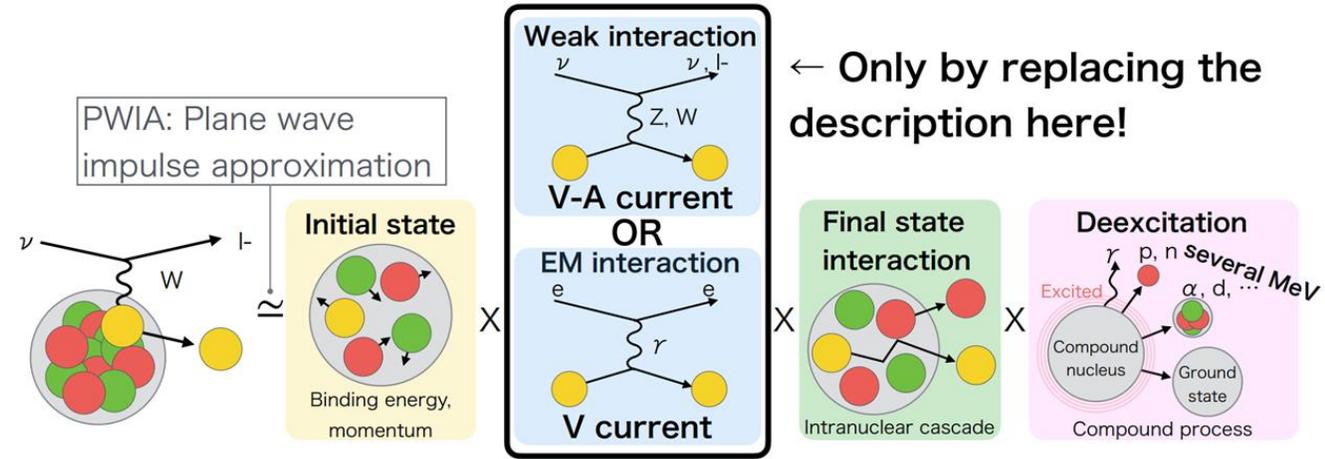


# Neutrino Scattering

Axial form factors are property of weak interactions

Need neutrino data.

Using neutrino scattering allows us to measure parameters like „axial mass” necessary to describe form factors.

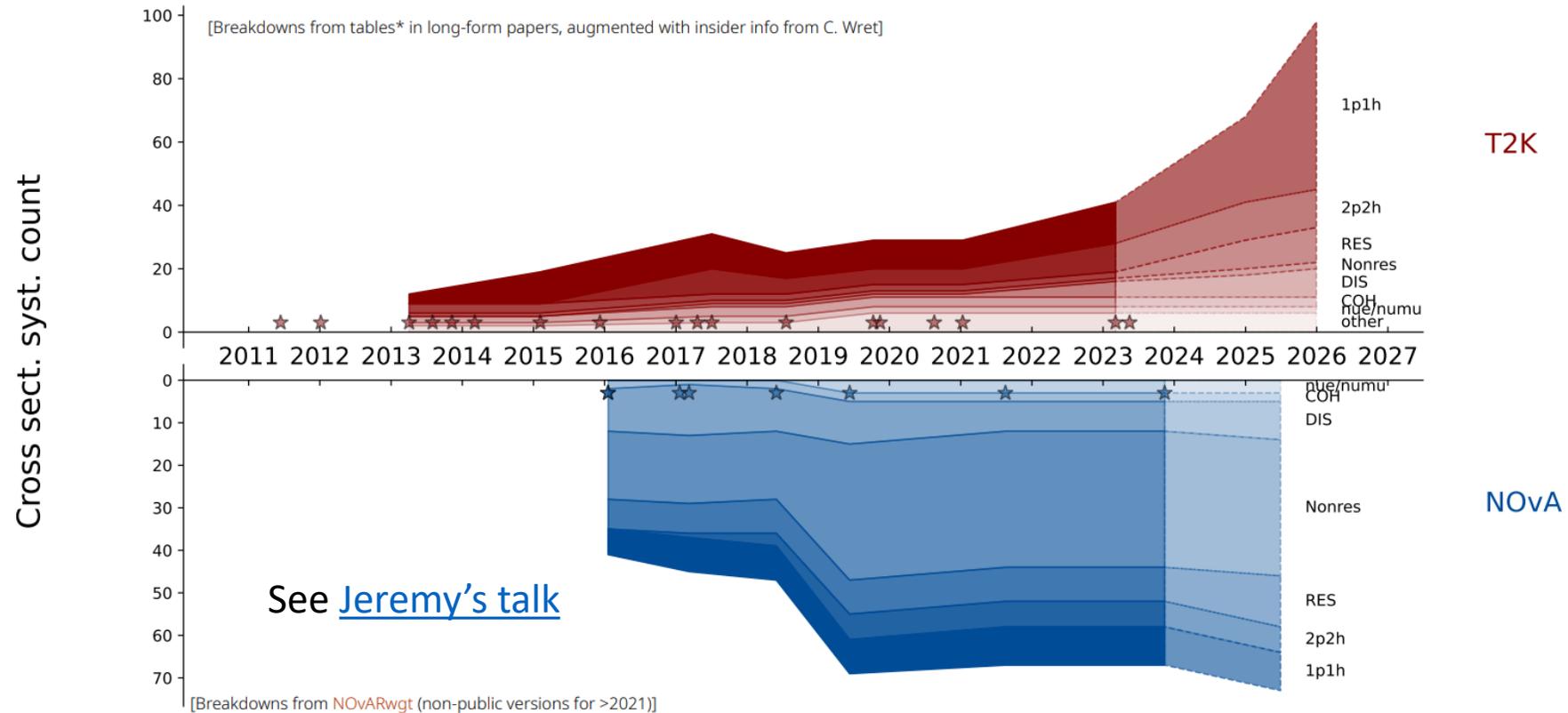


# T2K+NOvA

There has been impressive progress of theory inputs.

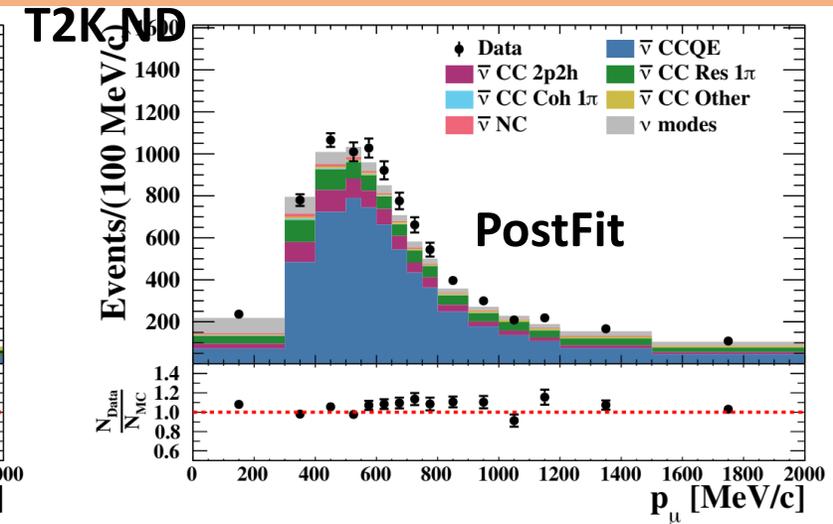
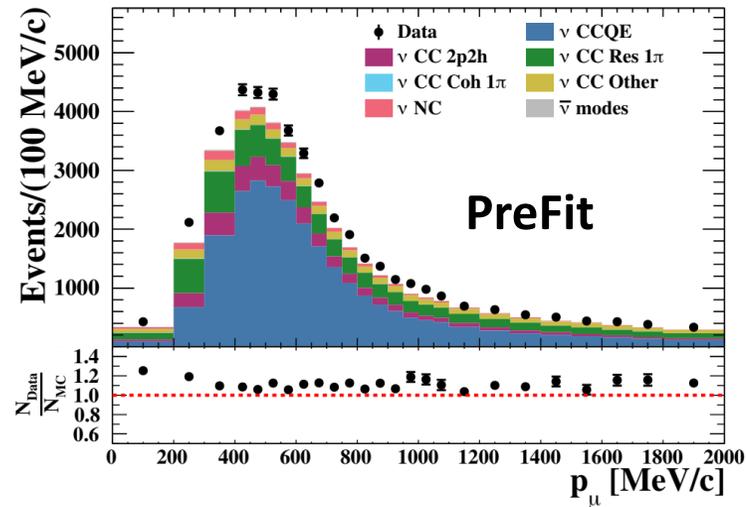
Allowing to get better models and more realistic uncertainties describing reactions like CCQE, RES FSI etc.

Near detectors are becoming more significant as the number of uncertainties rises.



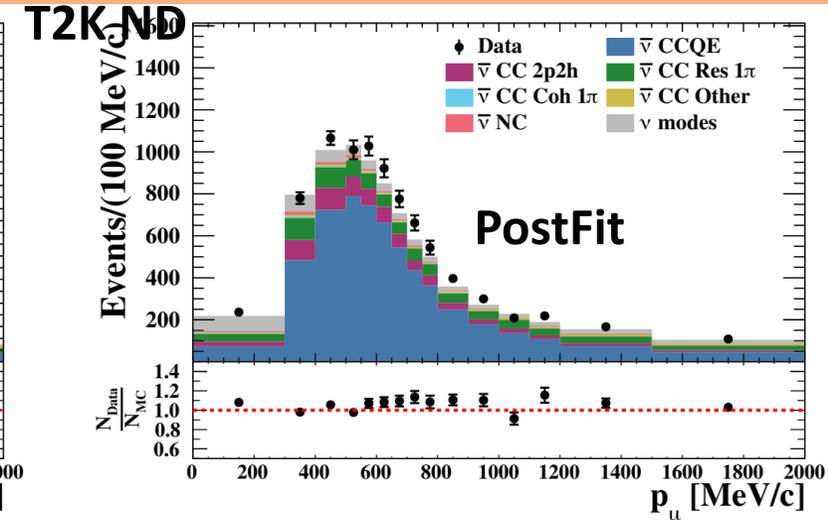
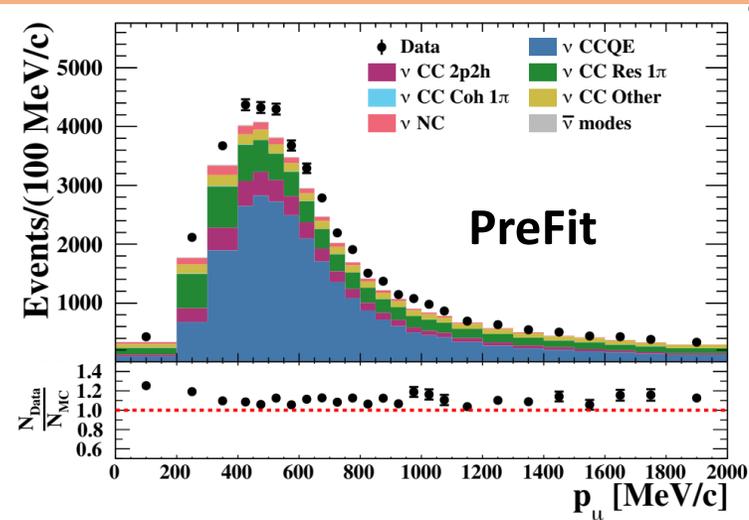
# Impact of near detectors

Near Detector allows to improve data MC agreement significantly

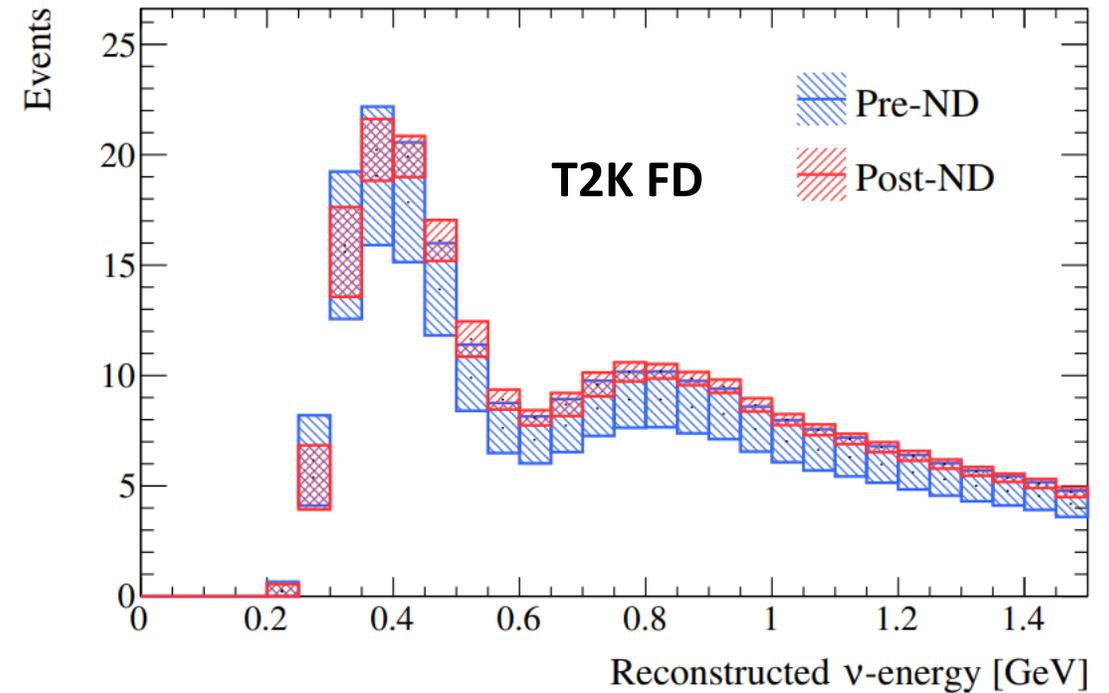


# Impact of near detectors

Near Detector allows to improve data MC agreement significantly



But also, significantly reduces uncertainty on predictions in far detector.

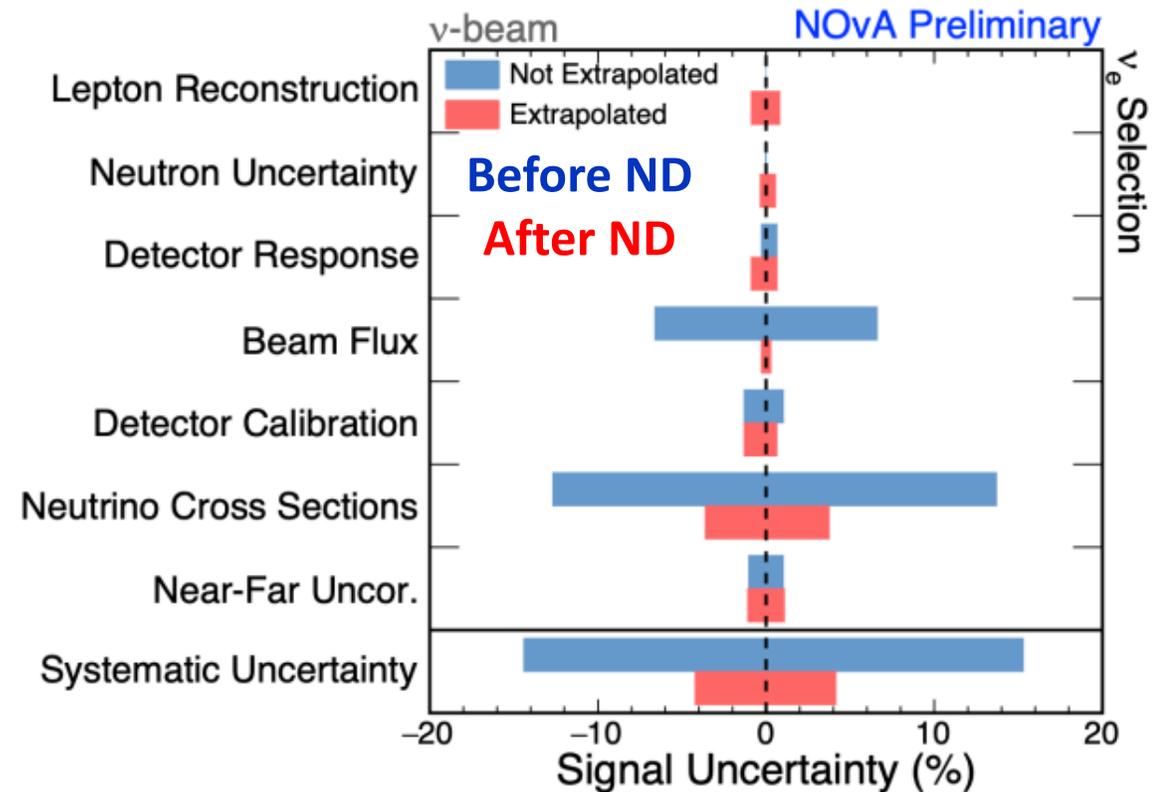


Notice scale of events observed at ND and FD

# Impact of near detectors

We can see for NOvA ND also allows to significantly reduce uncertainties.

Especially one related to modelling of neutrino interactions.



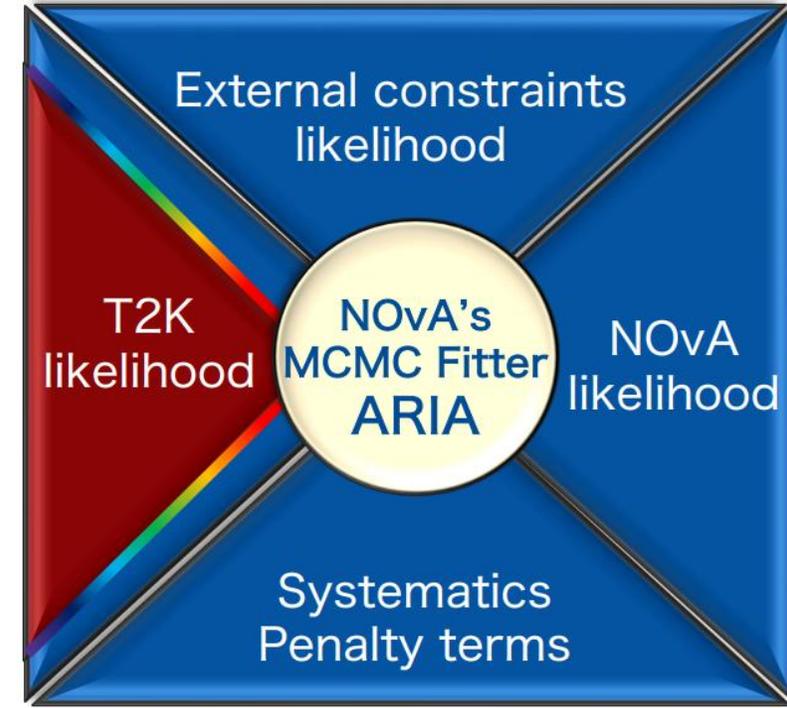
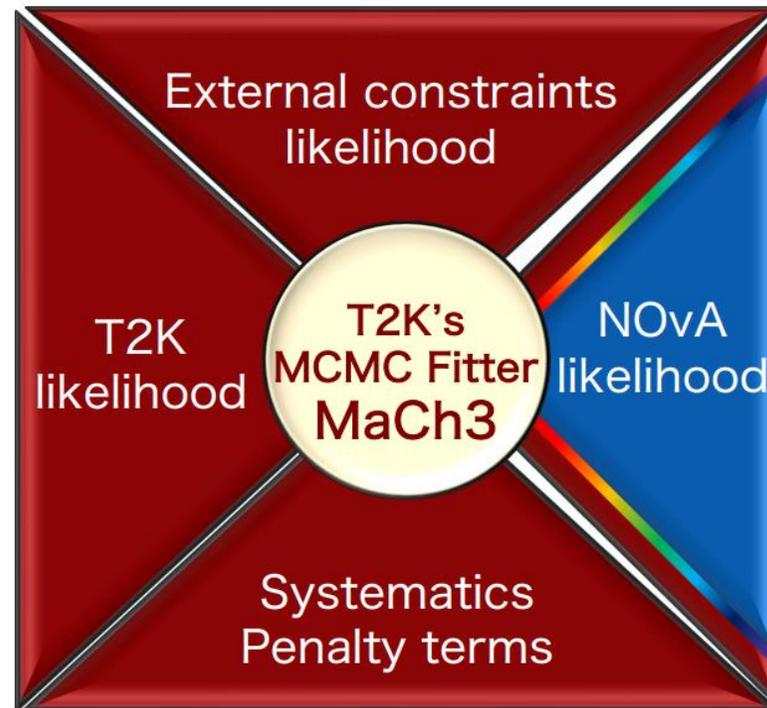
# Chapter V: T2K+NOvA Methodology

## Summary

- To measure  $\nu$  oscillation one need only energy
- We can measure Energy using products of  $\nu$  interaction
  - Modelling of interactions is difficult ☹️
  - Using e/ $\nu$  scattering to develop better models
- Near detectors are used for  $\nu$  scattering and error reduction

# T2K+NOvA

- Both T2K and NOvA have used their Bayesian Markov Chain Monte Carlo (MCMC) fitters.
- Both produce same output format: Posterior densities and credible intervals for parameters-of-interest.
- Independent implementation of the framework provided rigorous validation of the joint fit.



Red represents T2K codebase & blue shows NOvA codebase.

# Simulated Data Studies

We have plethora of generators with multiple models available

We can run data fit with only one models configuration.

Uncertainties are built for single configuration

We know uncertainties can't cover all effects.

**How to treat such unknown uncertainty?**

**Different Neutrino Generators**

Generator have access to different models and vary how consistently modelled are implemented.	 NEUT used by T2K and other Japanese based experiments	<ul style="list-style-type: none"><li>• Development driven by needs of these experiments</li><li>• Wide range of processes</li></ul>
neutrino physics we have wide range access to generators	 GENIE used by NOvA and other USA based experiments	<ul style="list-style-type: none"><li>• Developed experimentalists and theorists</li><li>• Wide range of processes</li></ul>
Now exploring impact of different effects and analysis biases	 NuWro	<ul style="list-style-type: none"><li>• Mainly developed by theorists</li><li>• Wide range of processes</li></ul>
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Kamil Skwarczyński 32

# Simulated Data Studies

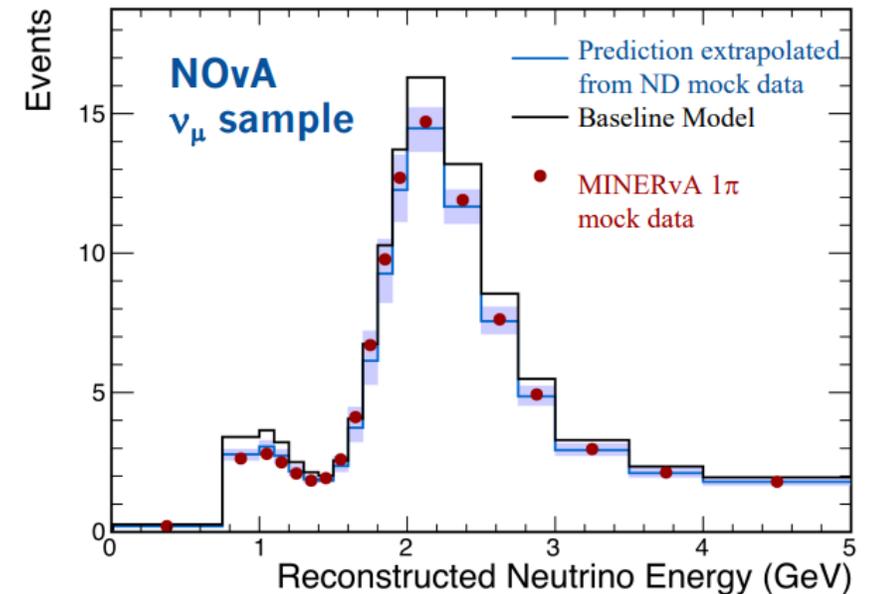
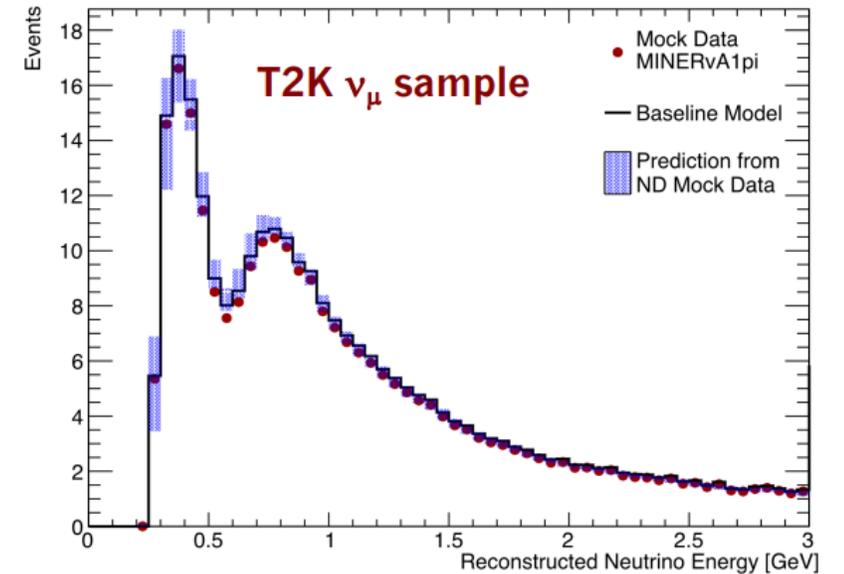
## How to treat such unknown uncertainty?

We use simulated data to evaluate the robustness of the fit against various alternate models

Reweight MC to alternative model and treat it as (simulated) „data”.

Perform fit both for near and far detector

Compare with default fit



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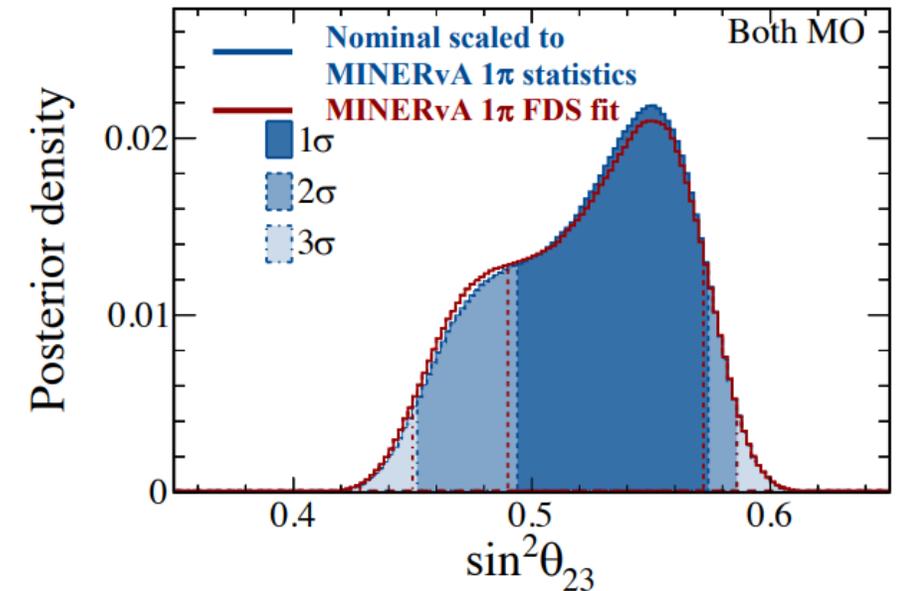
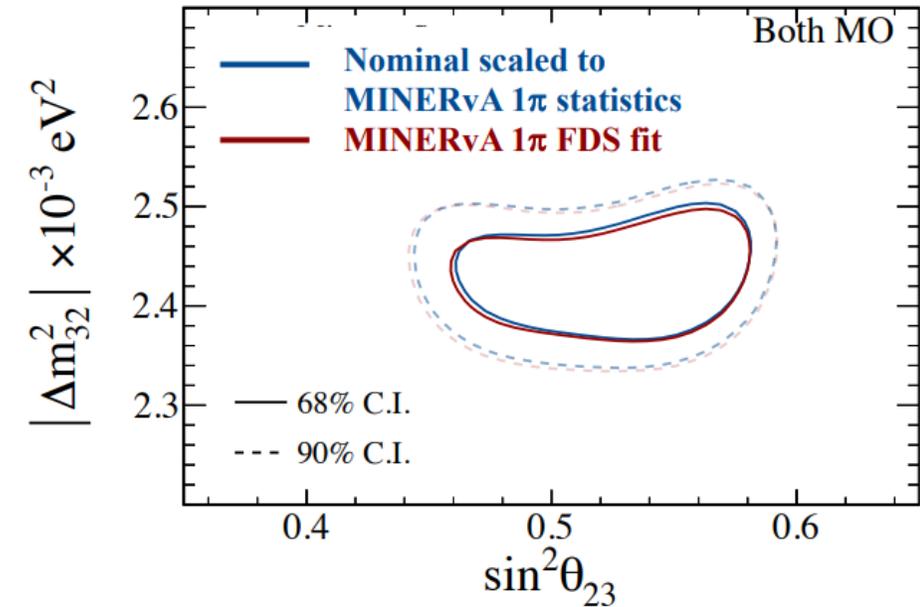
Perform fit both for near and far detector

Compare with default fit

Run fit and analyse.

All simulated data were below set criterion

No need to inflate error due to out of model effects



# Impact of Correlations – Nightmare Studies

T2K and NOvA uses different neutrino generators and different models and interaction uncertainties.

Direct correlation of models impossible ☹️

Exception  $\nu_\mu/\nu_e$  and  $\bar{\nu}_\mu/\bar{\nu}_e$  cross-section uncertainties, treatment is identical (large  $\delta_{CP}$  impact)

**Different Neutrino Generators**

Generator have access to different models and vary how consistently modelled are implemented.		<b>NEUT</b> used by T2K and other Japanese based experiments <ul style="list-style-type: none"><li>• Development driven by needs of these experiments</li><li>• Wide range of processes</li></ul>
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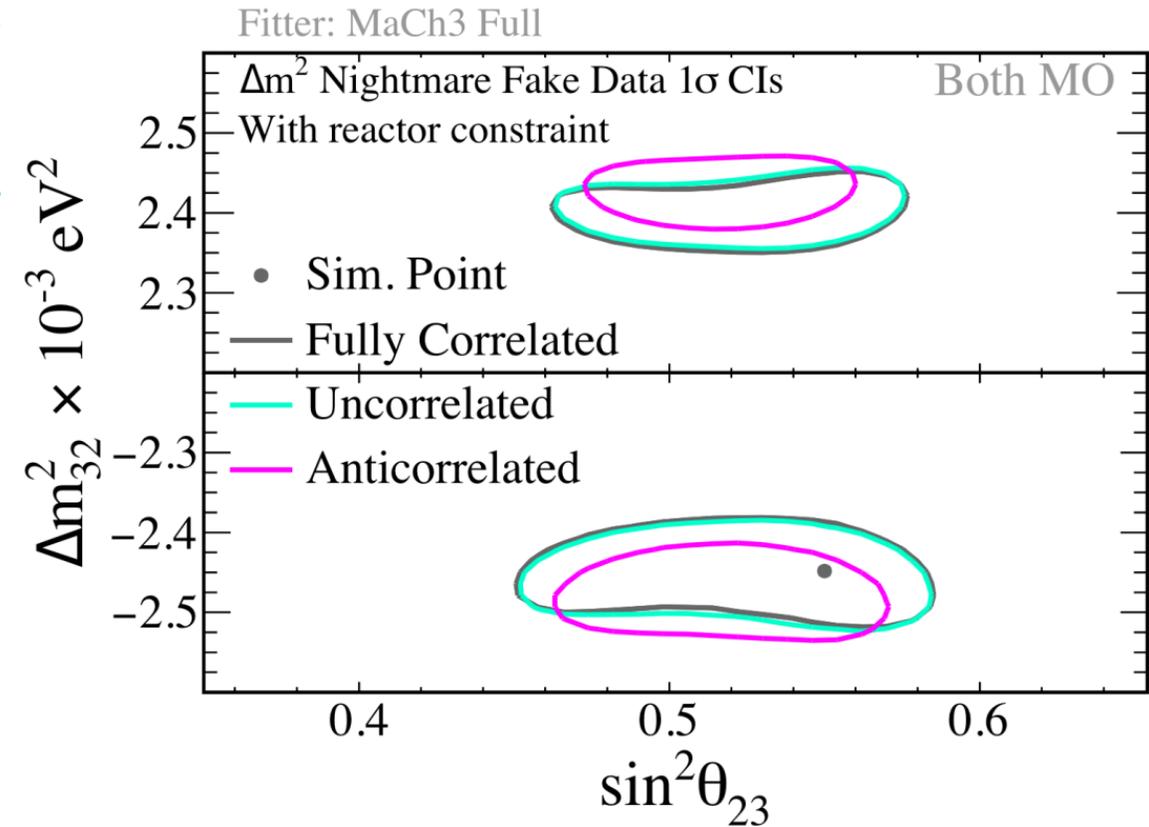
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Exception  $\nu_\mu/\nu_e$  and  $\bar{\nu}_\mu/\bar{\nu}_e$  cross-section uncertainties, treatment is identical (large  $\delta_{CP}$  impact)

Fabricated parameters for each experiment to simulate a fully correlated bias for  $\Delta m^2_{32}$  or  $\sin^2\theta_{23}$

- Keeping the parameters either fully correlated, uncorrelated, or fully anti-correlated in the fit
- **Uncorrelated and correlated (to follow simulated bias) agree well** while **incorrectly correlating systematics leads to biases**
- Impact of correlations merits further investigation for future analyses with increased statistics

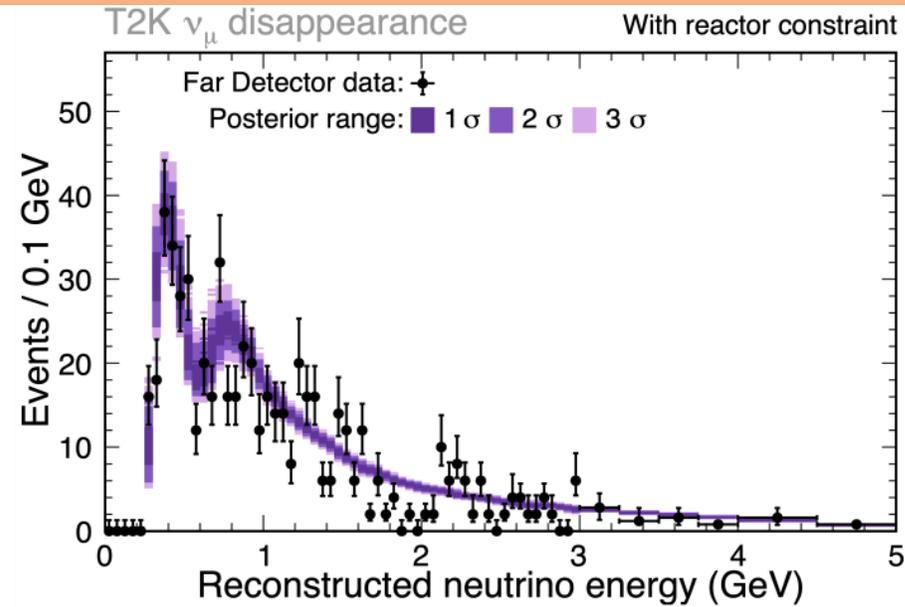


# Epilogue: All Comes Together

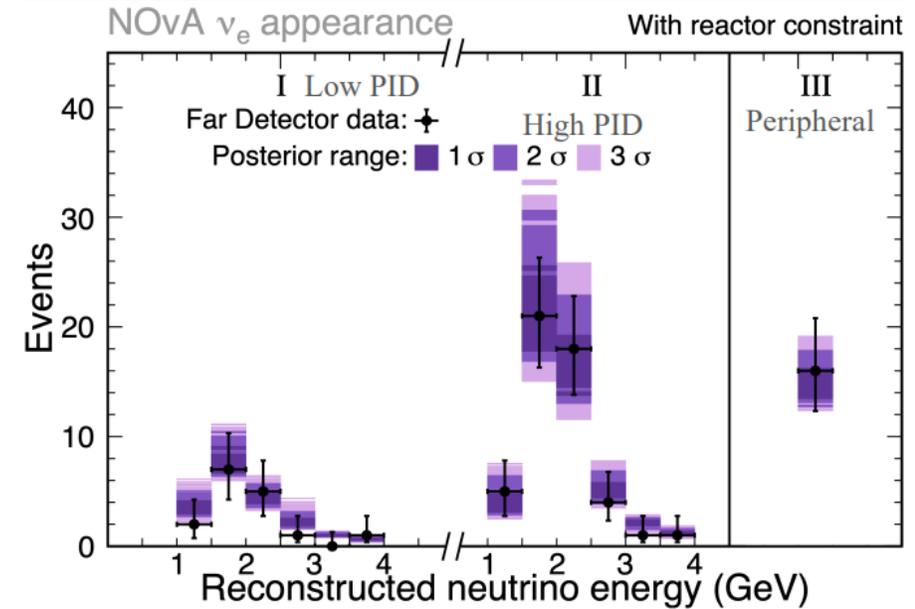
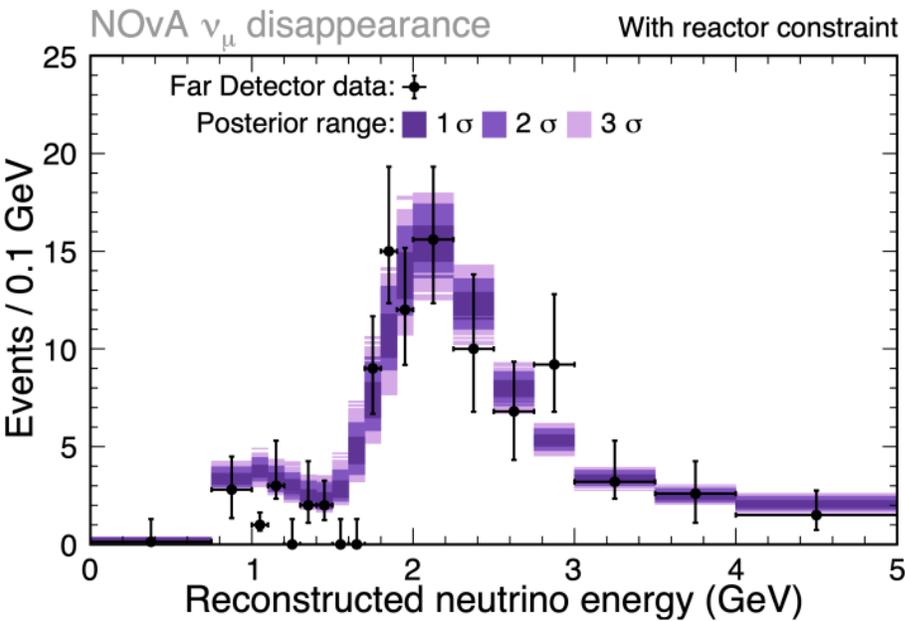
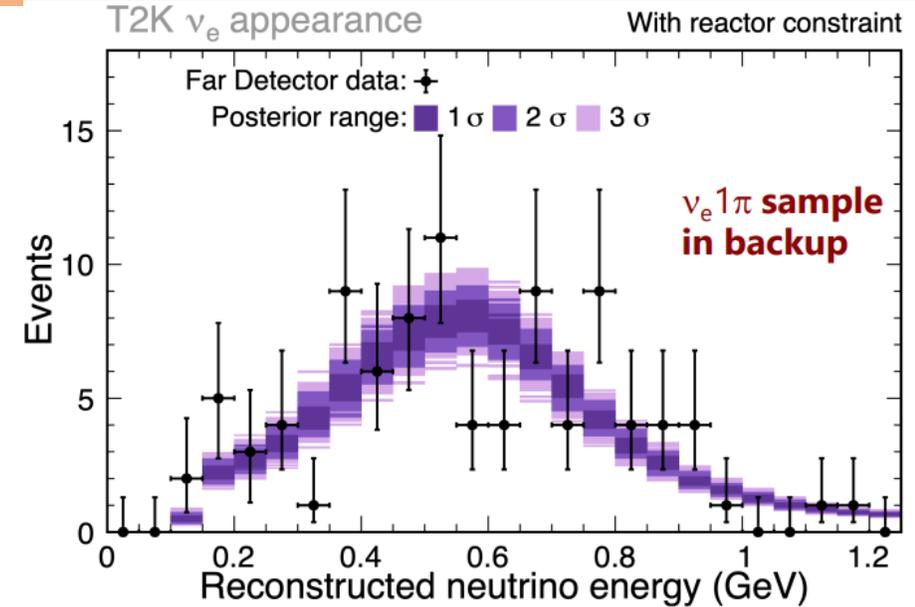
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- Near detectors are used for  $\nu$  scattering and error reduction
- T2K+NOvA performer several simulated data studies all successful below threshold

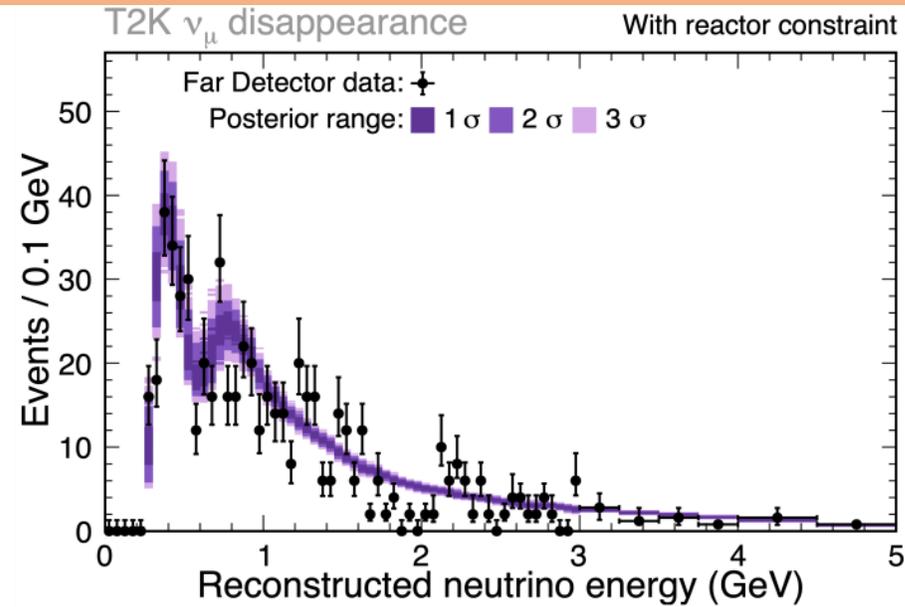
# FD Data Samples



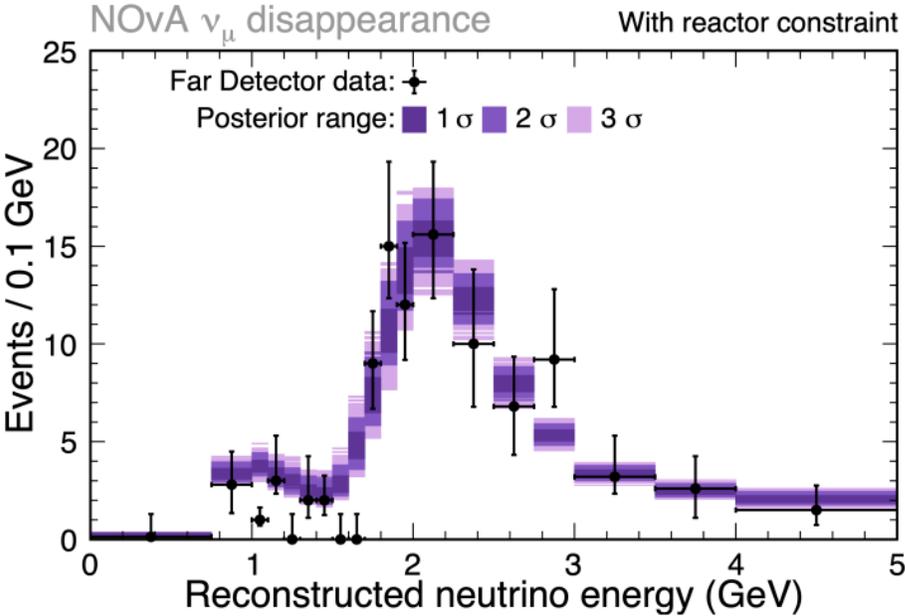
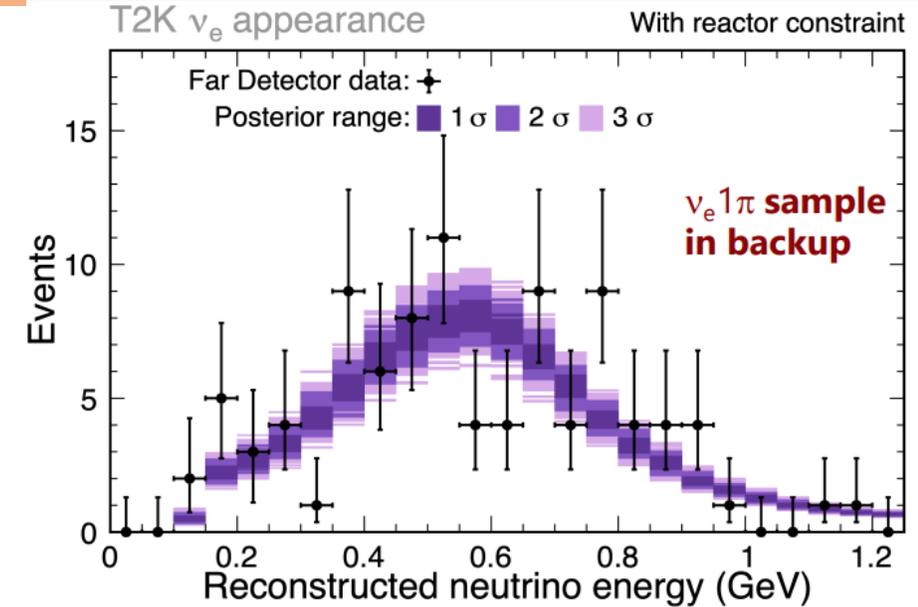
Good agreement between data and MC for FD samples at T2K and NOvA



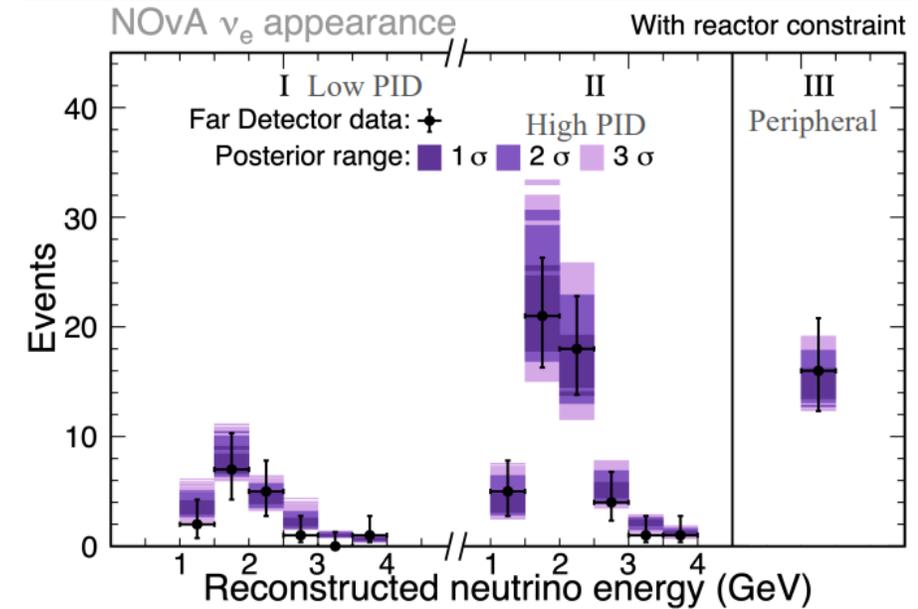
# FD Data Samples



Good agreement between data and MC for FD samples at T2K and NOvA



Channel	NOvA	T2K	Total
$\nu_e$	82	$94_{(\nu_e)}$	<b>190</b>
$\bar{\nu}_e$	33	$14_{(\nu_e 1\pi)}$	<b>49</b>
$\nu_\mu$	211	318	<b>529</b>
$\bar{\nu}_\mu$	105	137	<b>242</b>



# Jarlskog and CP Violation

Appearance channel

$$\frac{P(\nu_\mu \rightarrow \nu_e)}{P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)} \approx \sin^2(2\theta_{13}) \sin^2(\theta_{23}) \sin^2\left(\frac{1.27\Delta m_{32}^2 L}{E}\right) \mp \frac{1.27\Delta m_{21}^2 L}{E} 8J_{CP} \sin^2\left(\frac{1.27\Delta m_{32}^2 L}{E}\right)$$

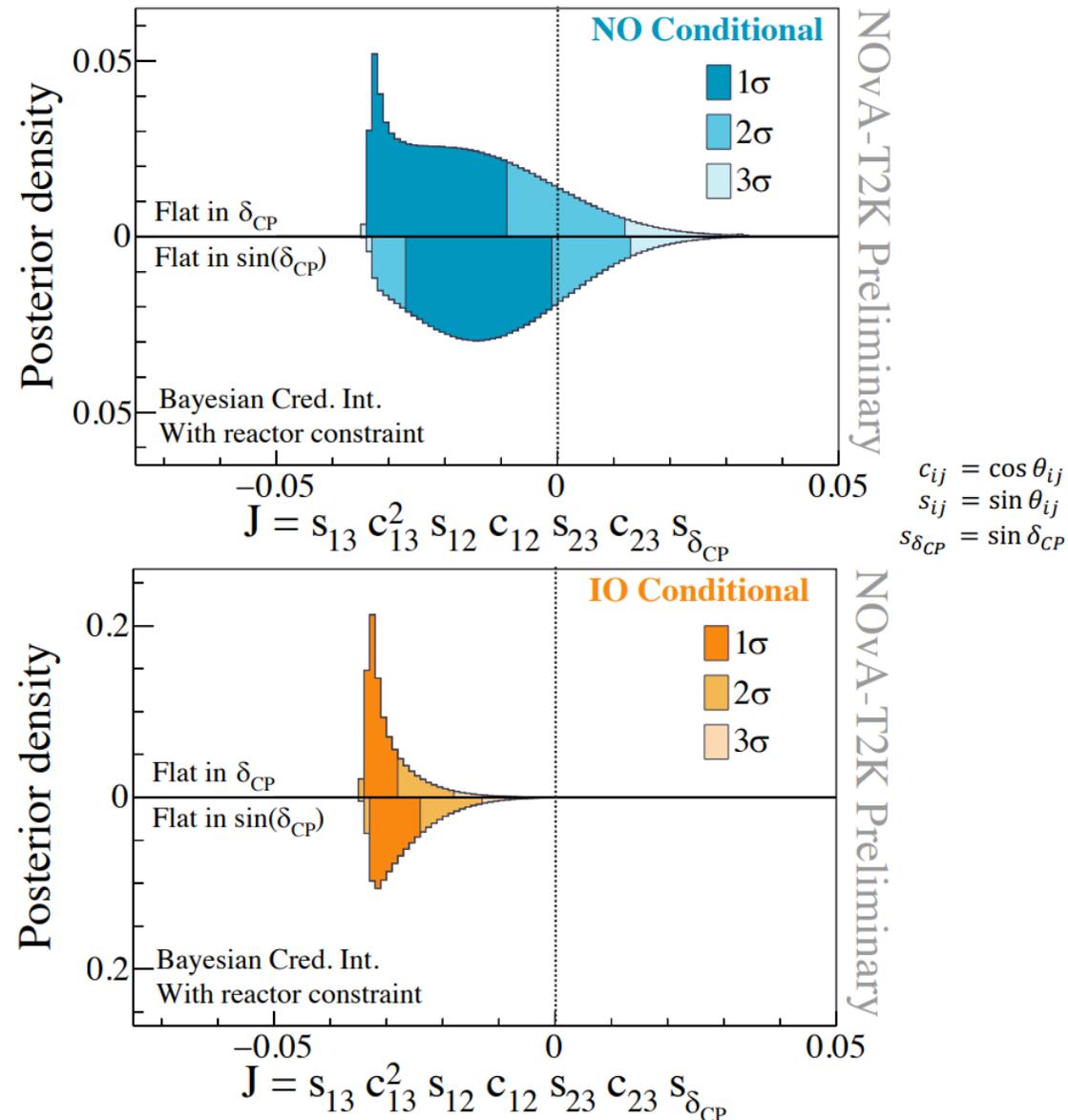
Jarlskog-invariant is a parameterization independent way to measure CP violation.

$J = 0$ : CP-Conservation

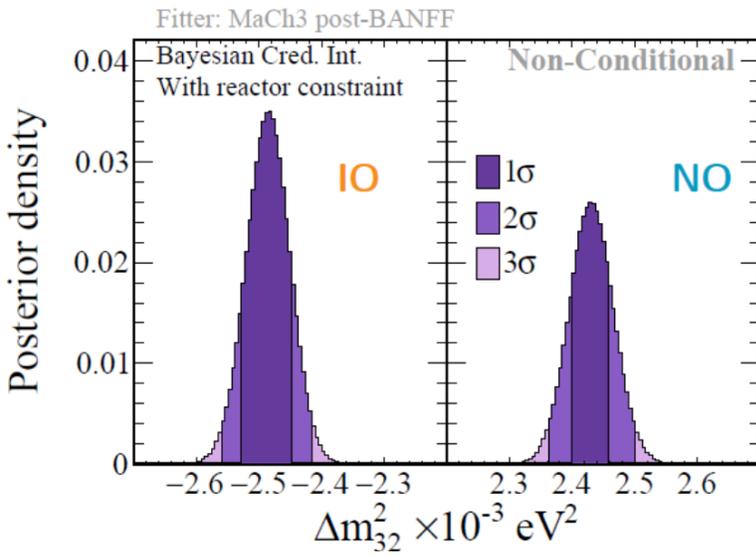
$J \neq 0$ : CP-Violation

For Normal Ordering, a considerably wider range of probable values for  $J$

$J = 0$  lies outside the 3sigma interval for the Inverted Ordering

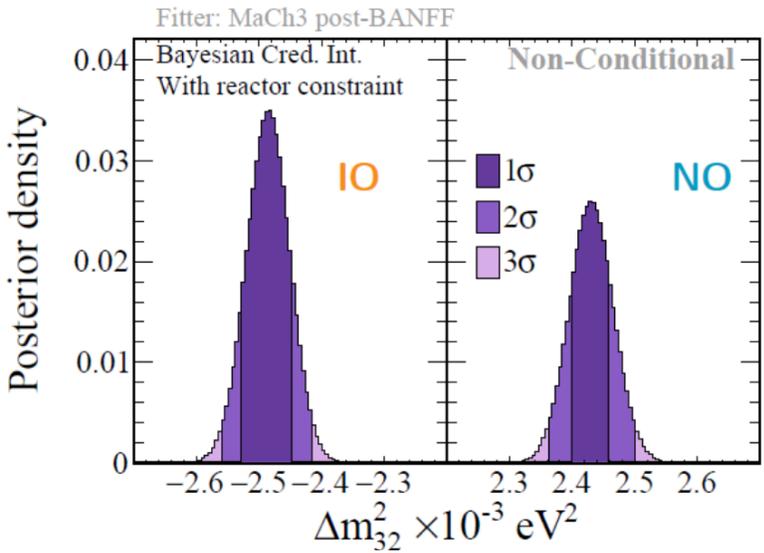


# Results: $\Delta m^2_{32}$



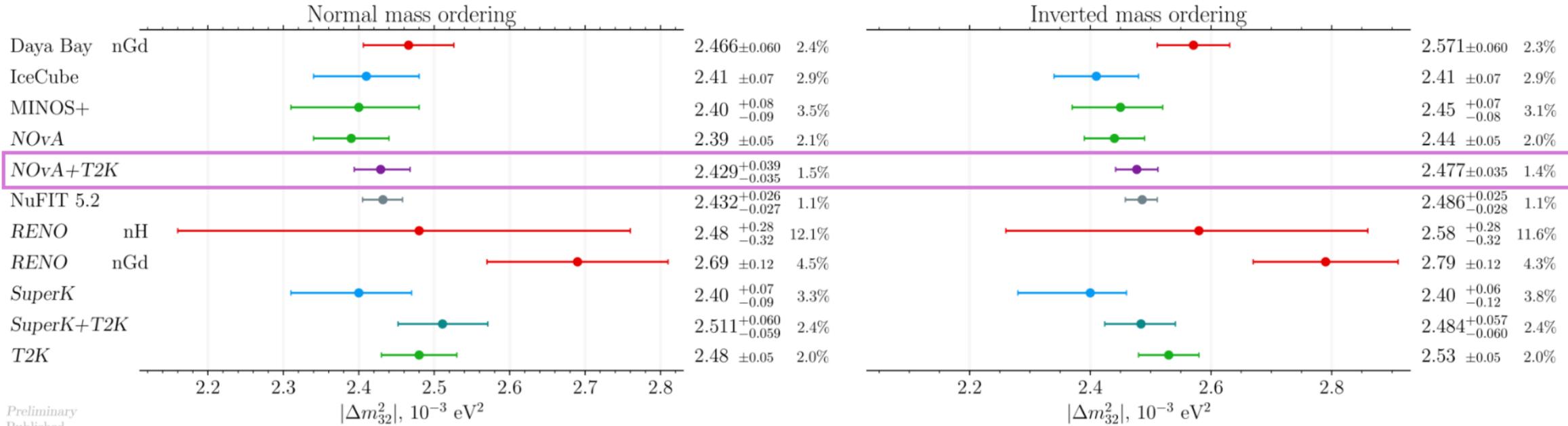
Mild preference for inverted ordering

# Results: $\Delta m_{32}^2$



Mild preference for inverted ordering

Smallest uncertainty in  $\Delta m_{32}^2$  32 < 2 %



Preliminary  
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v10 2023.10: git.jim.ruy/mj/osc

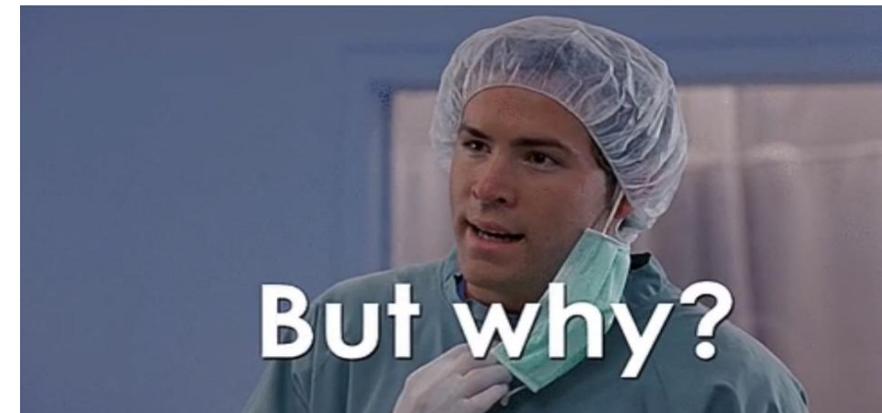
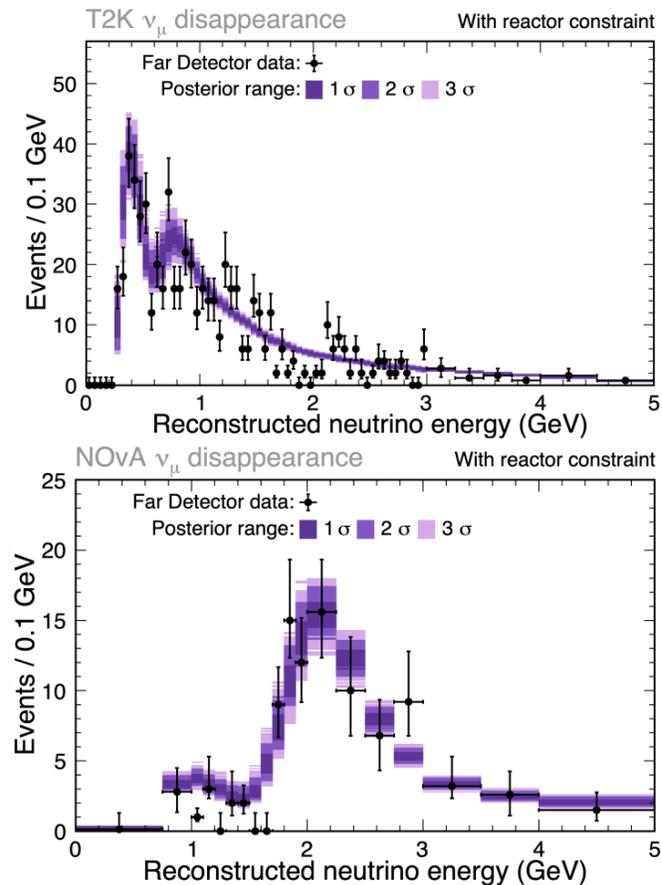
# Bonus: Looking Beyond

## Summary

- To measure  $\nu$  oscillation one need only energy
- We can measure Energy using products of  $\nu$  interaction
  - Modelling of interactions is difficult 😞
  - Using e/ $\nu$  scattering to develop better models
- Near detectors are used for  $\nu$  scattering and error reduction
- T2K+NOvA performed several simulated data studies all successful below threshold
  - T2K+NOvA performed measurement of mass ordering parameter

# One Step Back

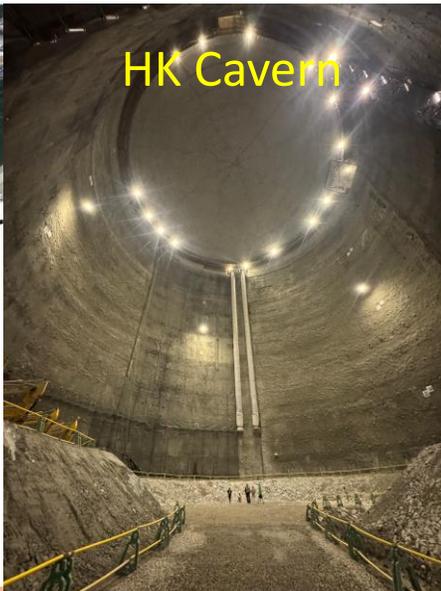
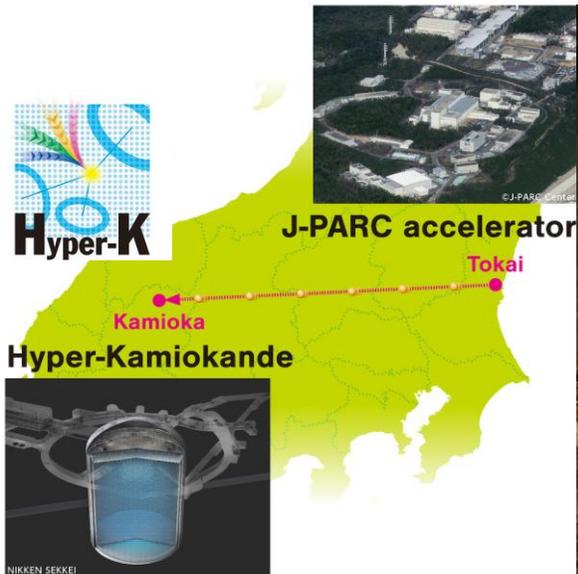
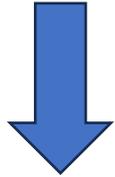
Some may ask why I focused so much on modelling uncertainties if we have huge statistical error.



# Hyper Kamiokande

Current experiment will be replaced with new much larger at scale.

Successor of T2K will be Hyper-Kamiokande (Japan)



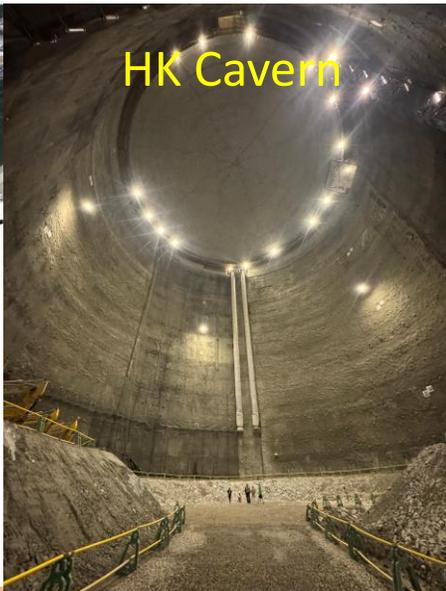
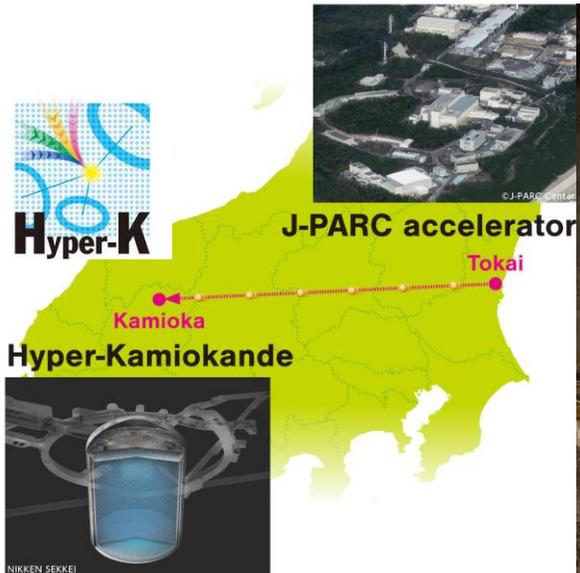
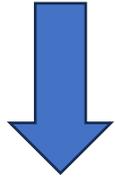
# Hyper Kamiokande and DUNE

Current experiment will be replaced with new much larger at scale.

Successor of T2K will be Hyper-Kamiokande (Japan)

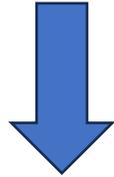
Successor to NOvA will be DUNE (USA).

T2K



NOvA

USA



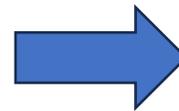
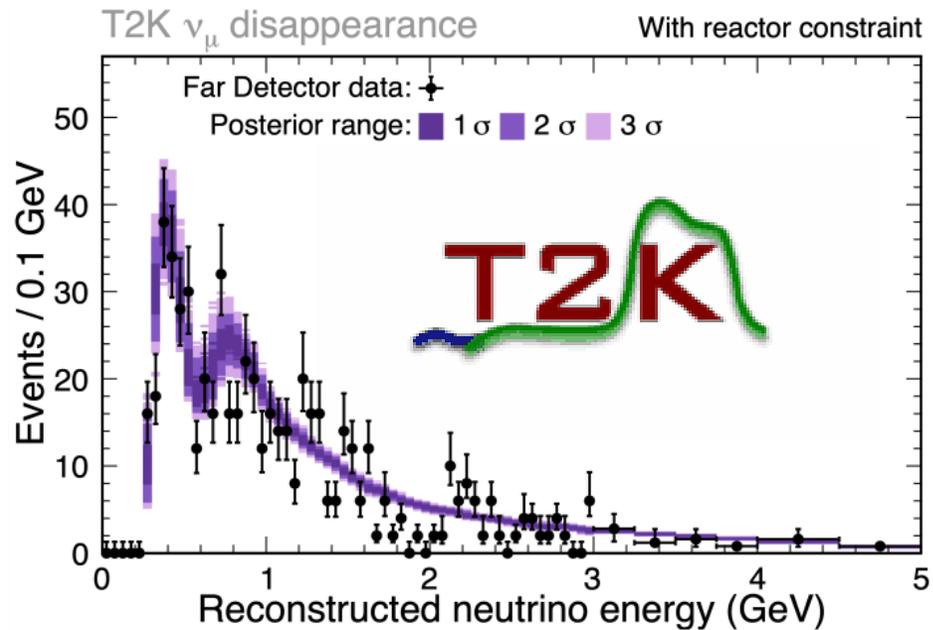
# Precision

New experiment can expect thousand of events.

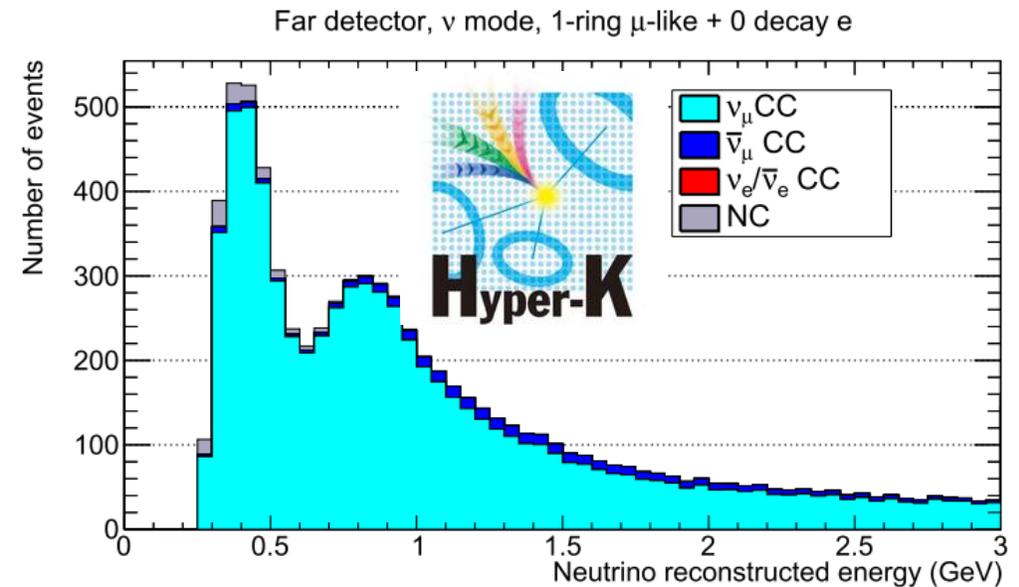
With such high number of events stat error will be much lower.

Thus, progress on modelling done in current experiments will directly transfer to future.

Around 500 events for this sample

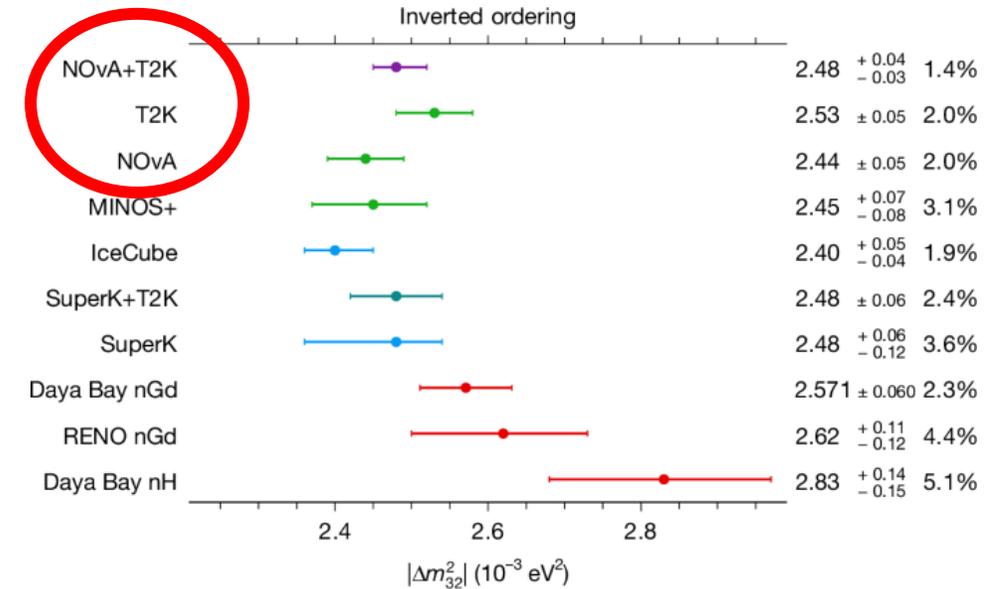


Around 9k events for this sample



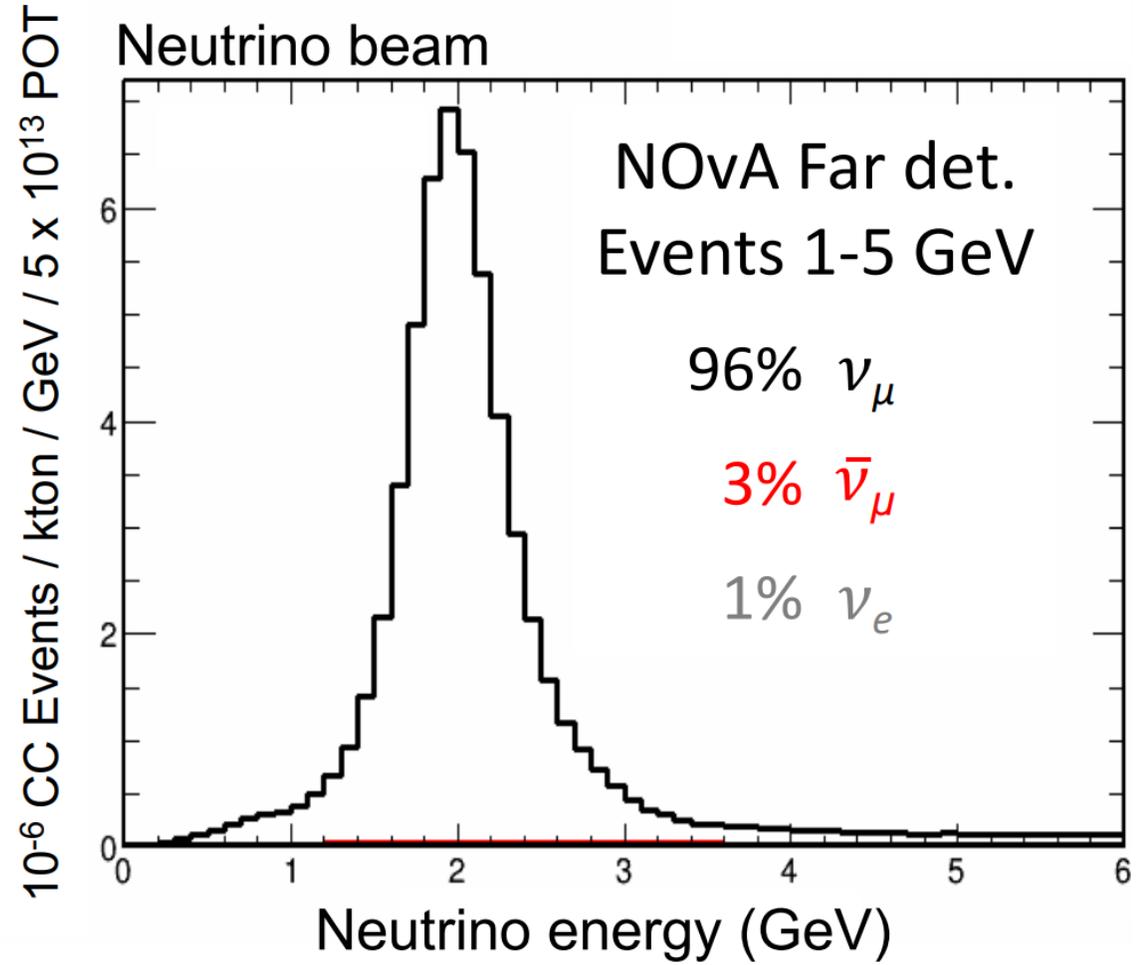
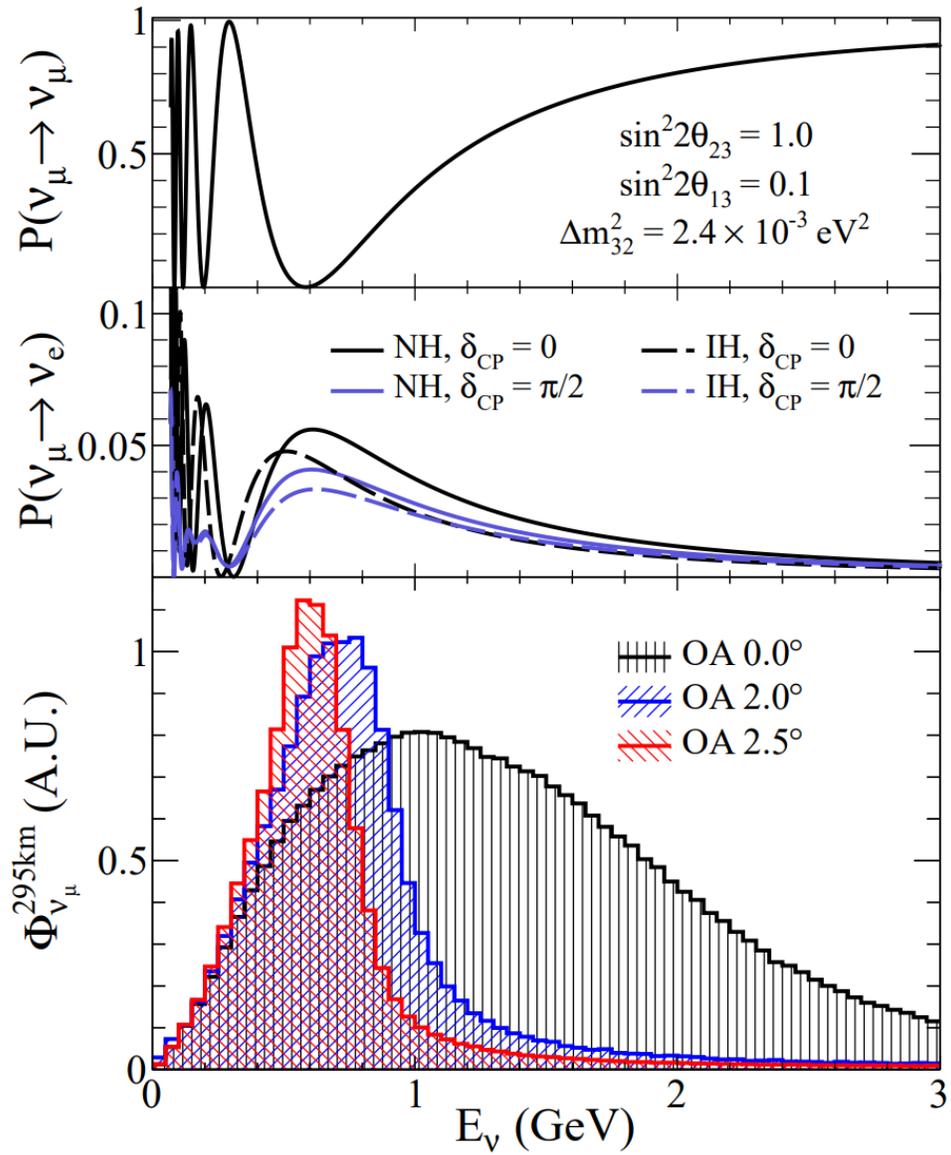
# Summary

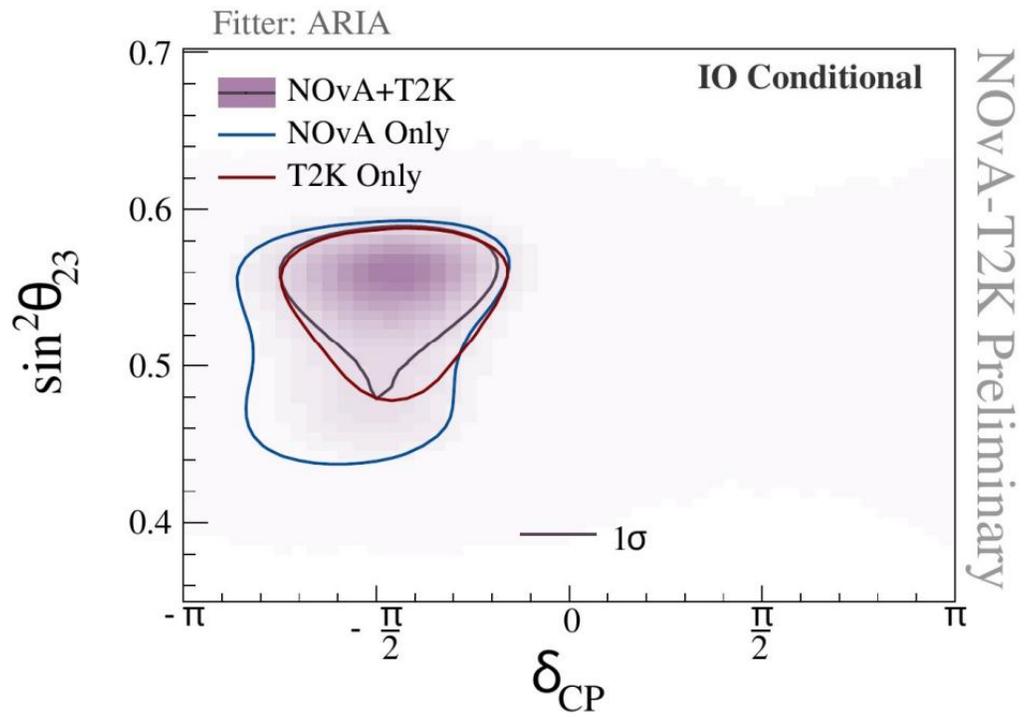
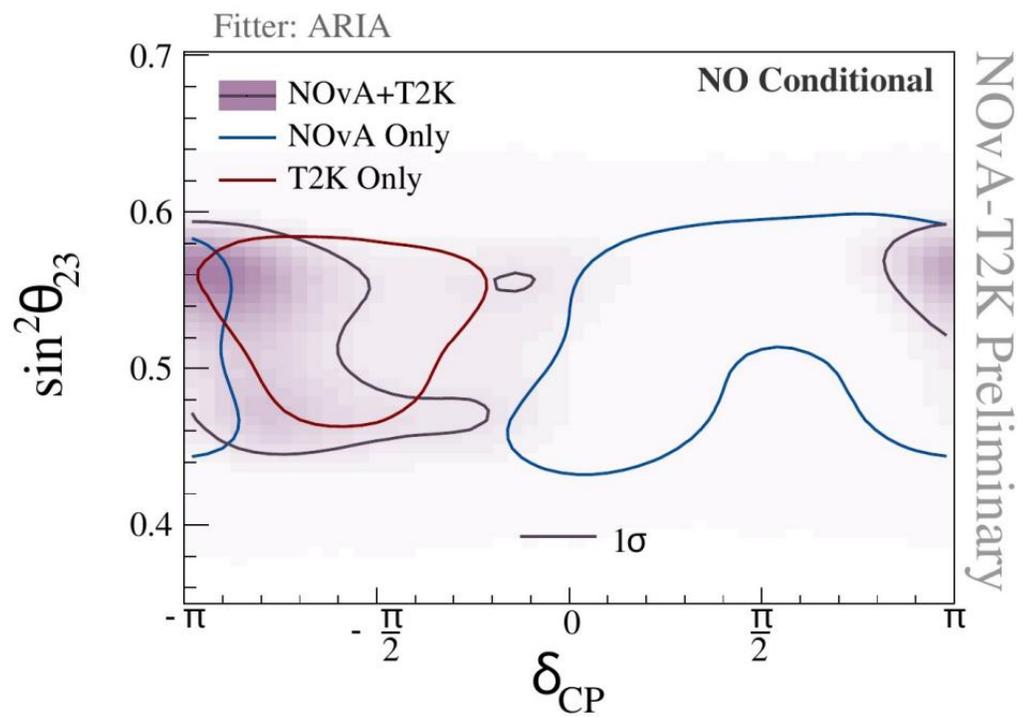
- To measure  $\nu$  oscillation one need only energy
- We can measure Energy using products of  $\nu$  interaction
- Modelling of interactions is difficult ☹️
- Using  $e/\nu$  scattering to develop better models
- Near detectors are used for  $\nu$  scattering and error reduction
- T2K+NOvA performed several simulated data studies all successful below threshold
- T2K+NOvA performed measurement of mass ordering parameter
- Future Experiments like HK and DUNE will require more sophisticate modelling

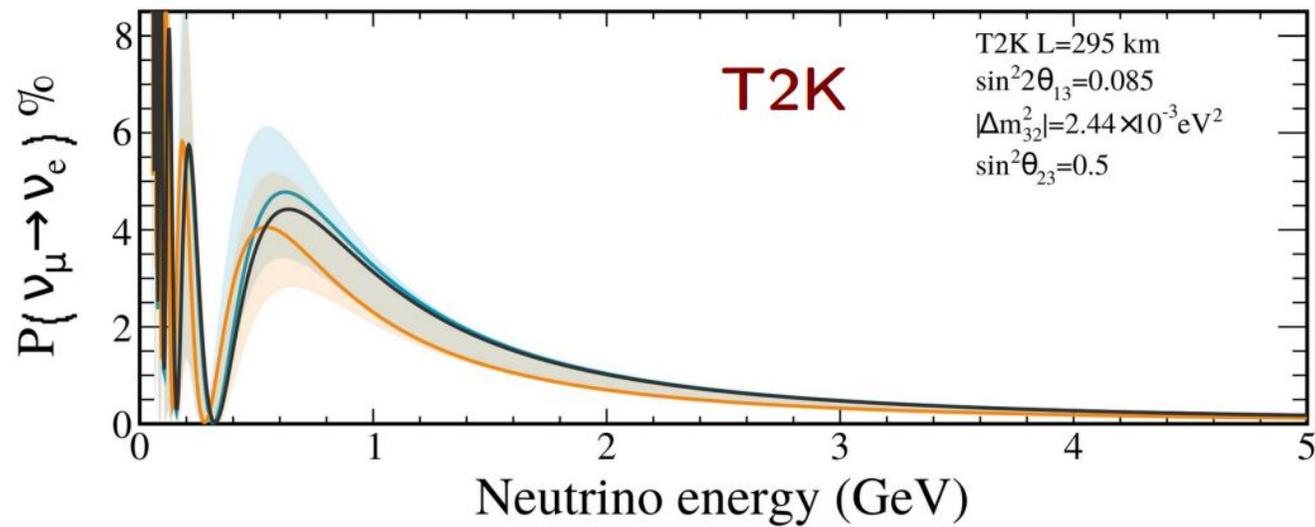
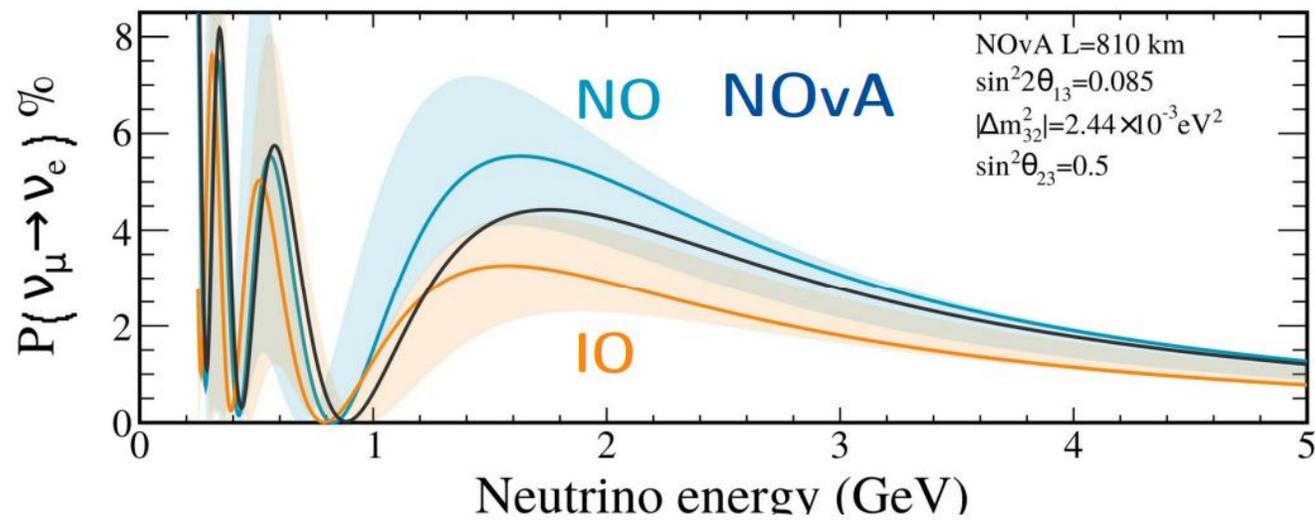


# Backup

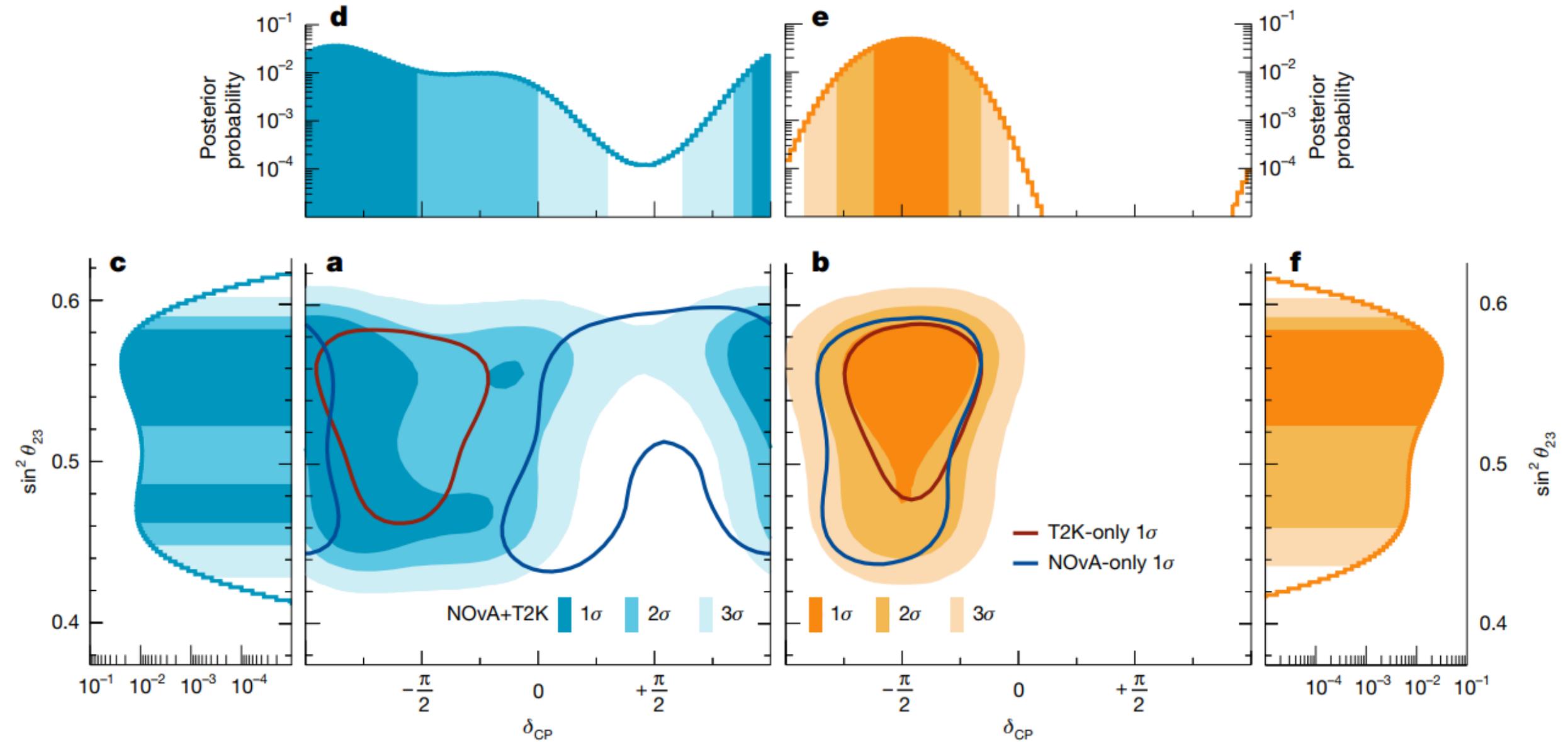
# Flux







# Joint Distribution

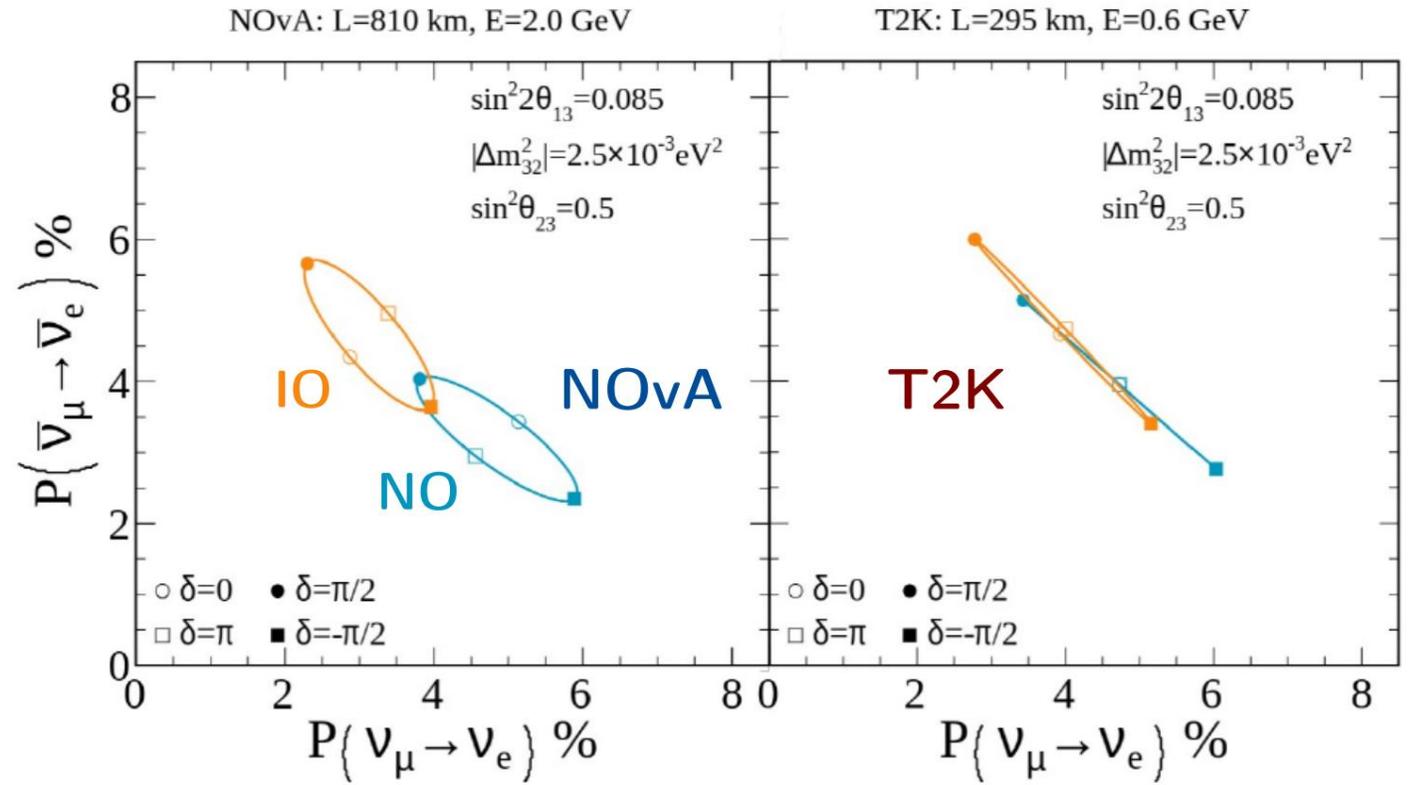


## NOvA:

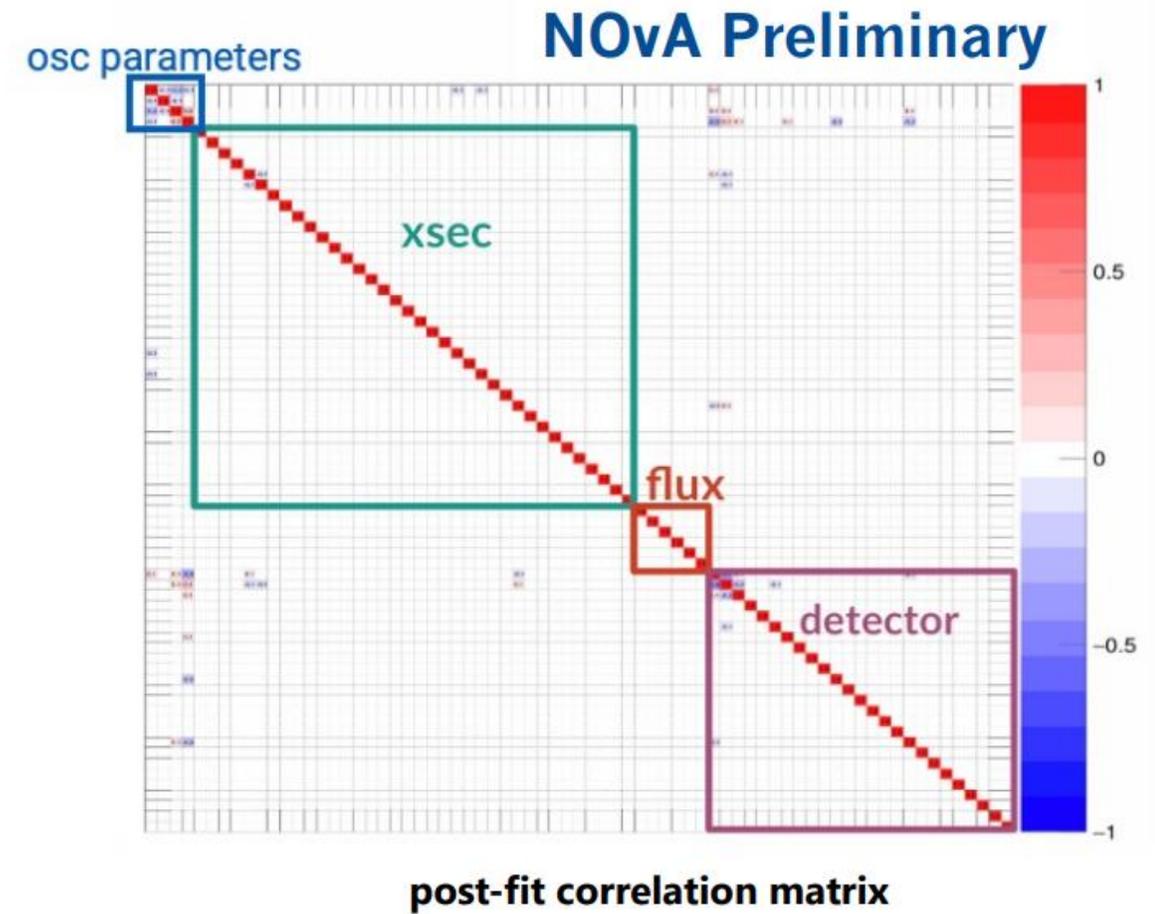
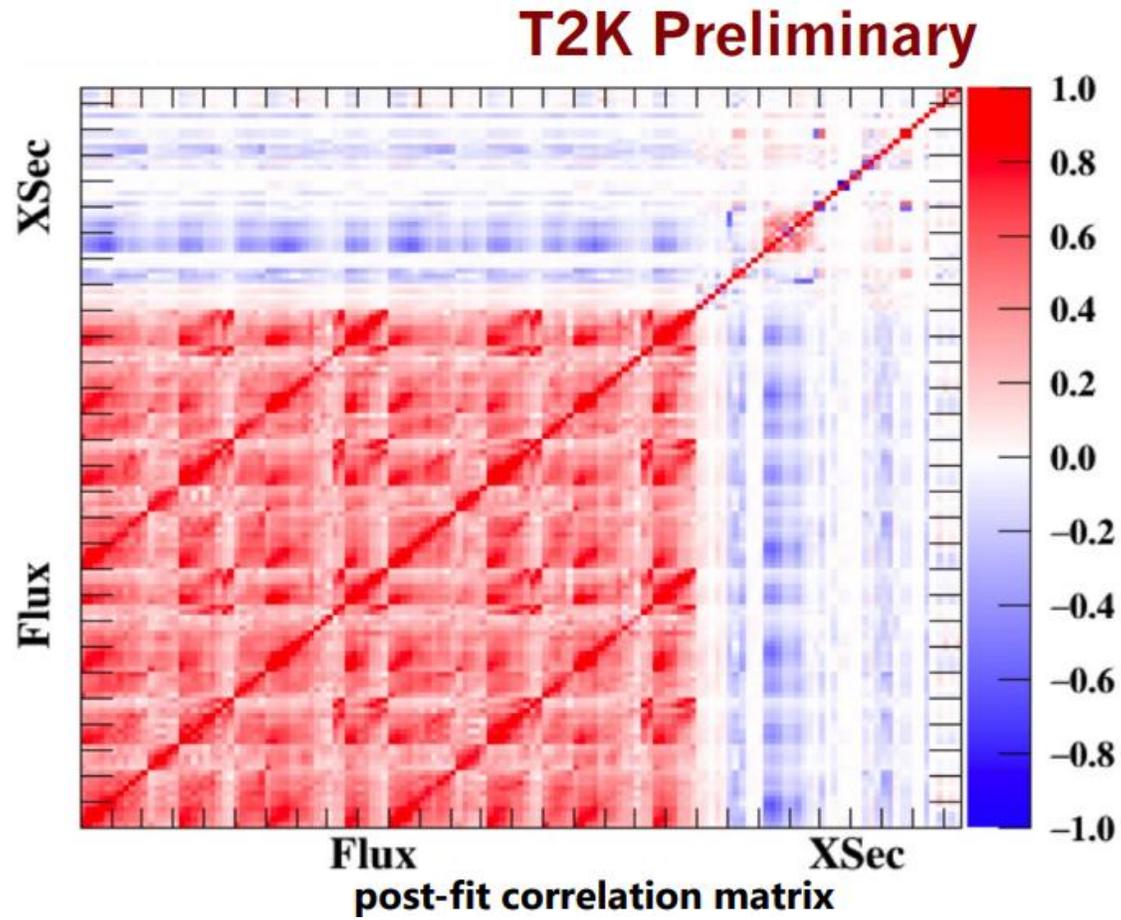
- Better mass ordering sensitivity
- Degenerate for around  $\delta_{CP} = \pi/2$  and  $-\pi/2$  (CPV)

## T2K:

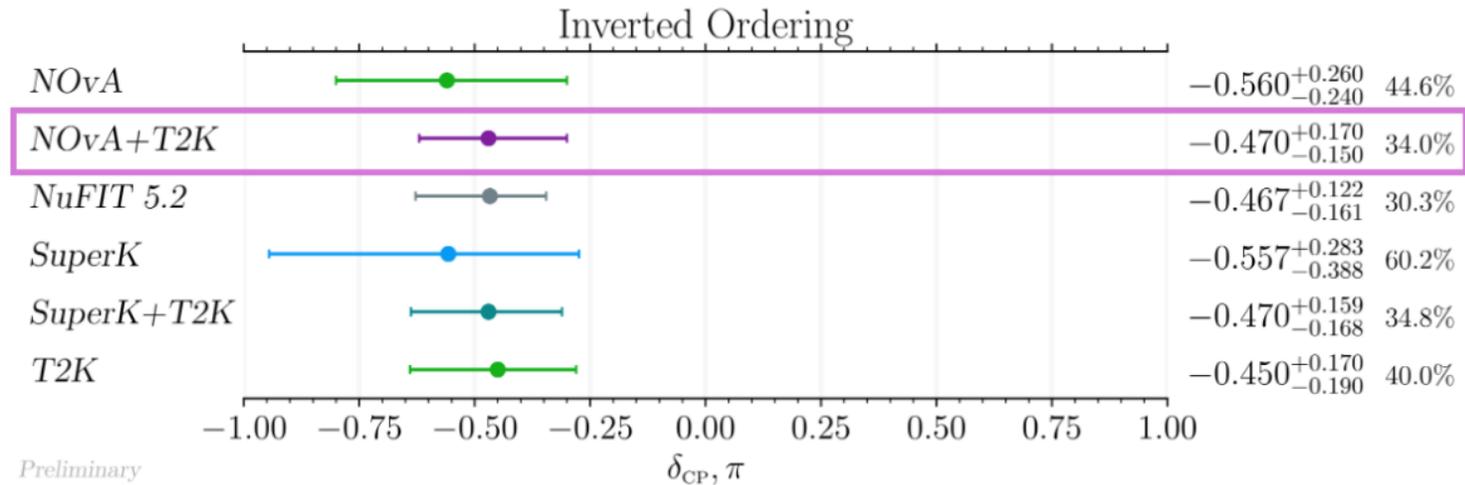
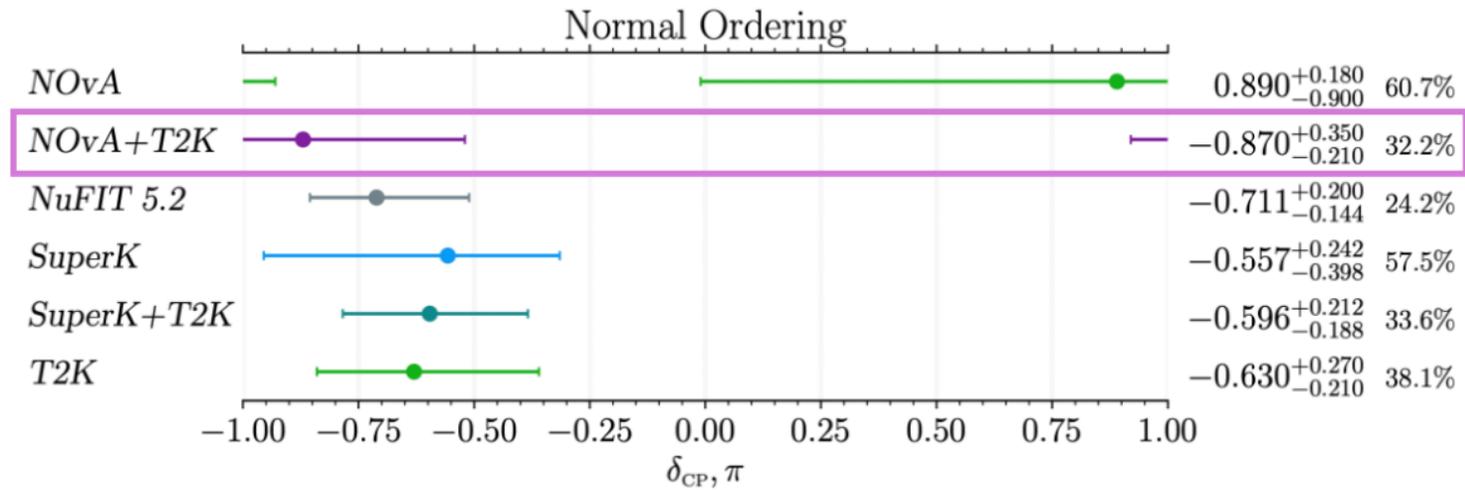
- Better  $\delta_{CP}$  sensitivity
- Degenerate for around  $\delta_{CP} = 0$  and  $\pi$  (no-CPV)



# Matrix



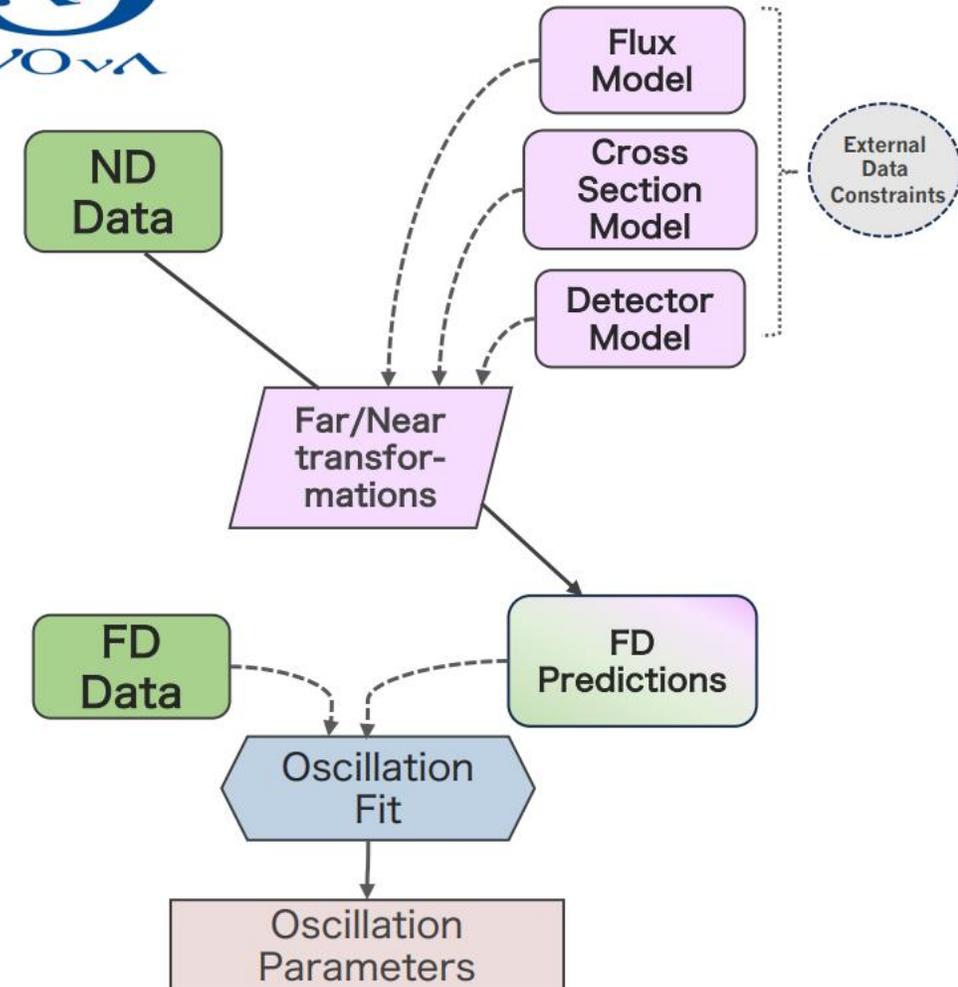
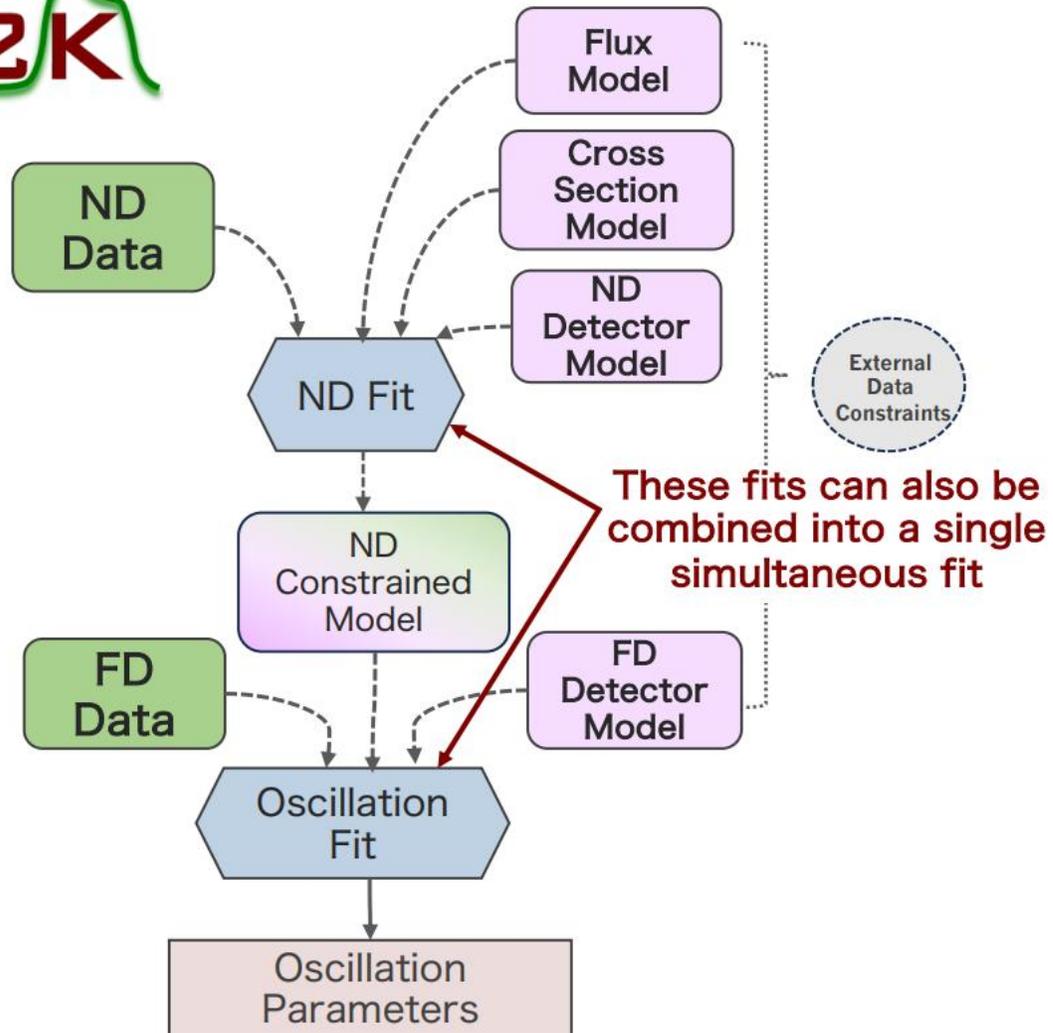
# $\delta_{CP}$ global comparisons

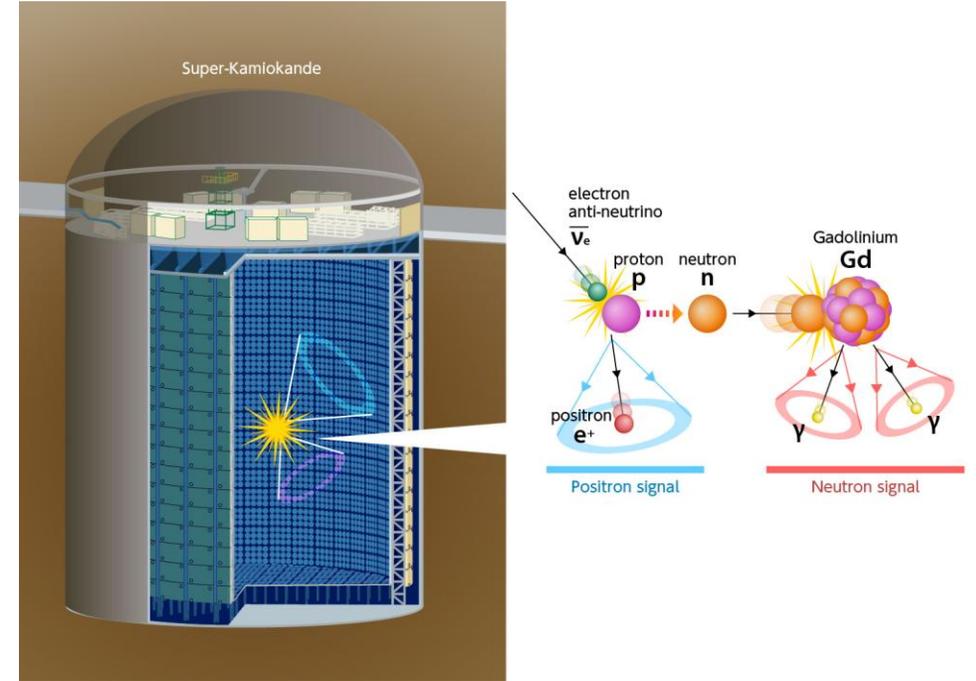
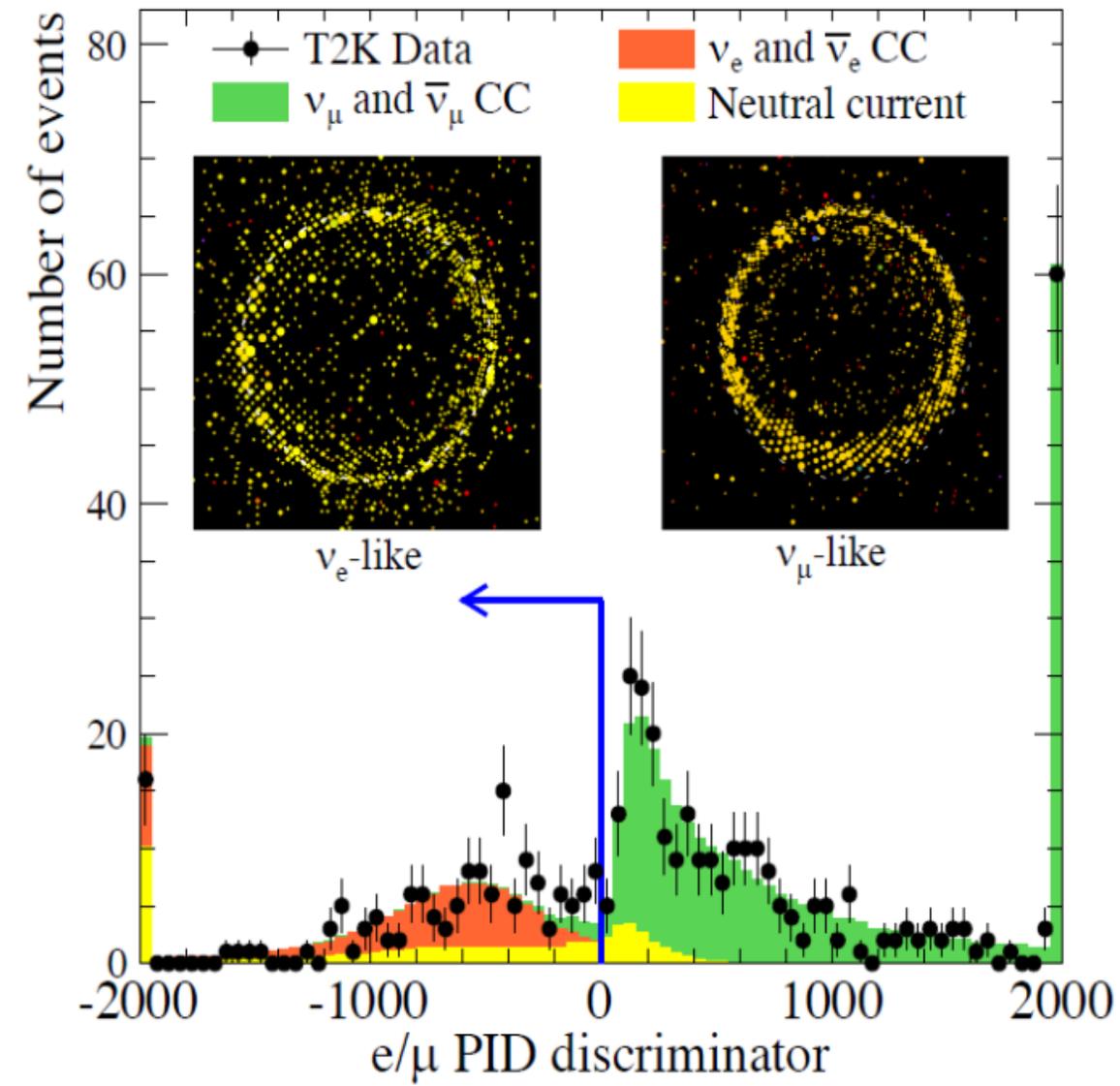


v1 2023.12: git.jinr.ru/nu/osc

Preliminary  
Published

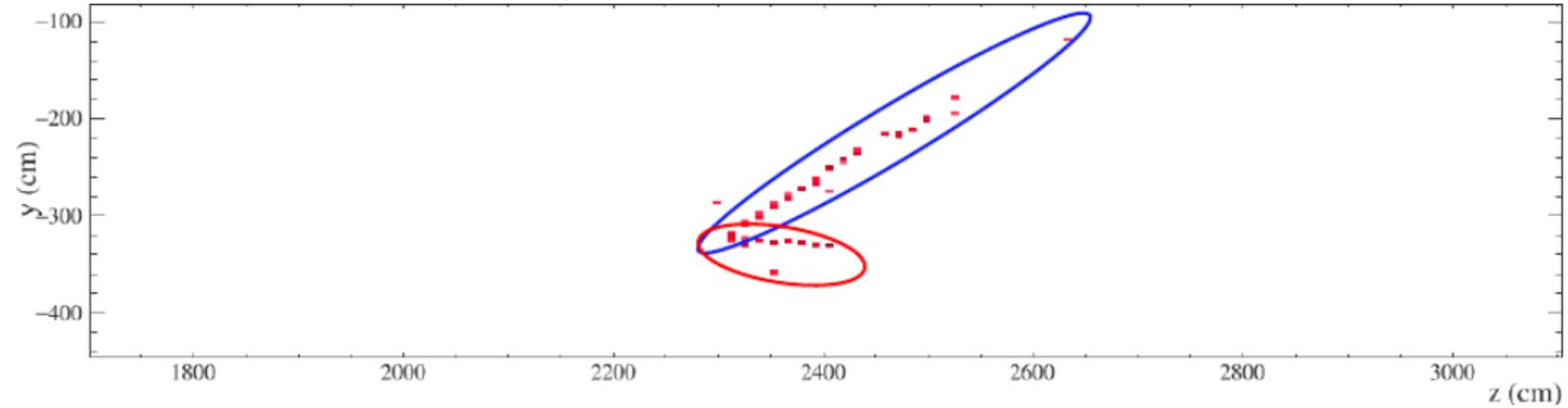
# Analysis Flow



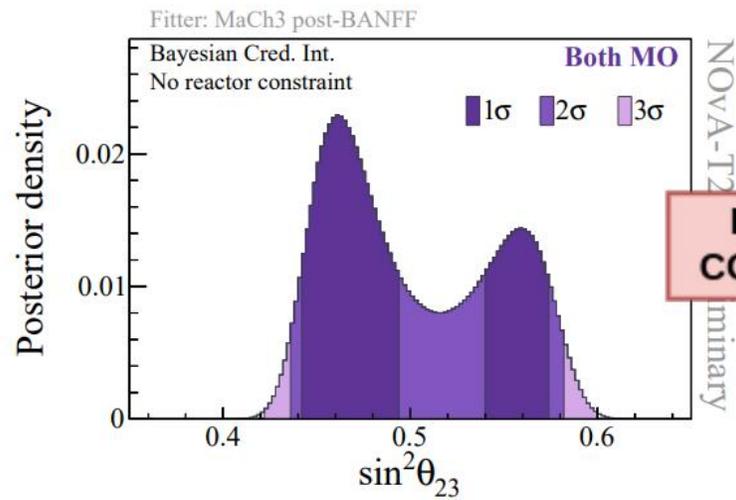


# NOvA Em

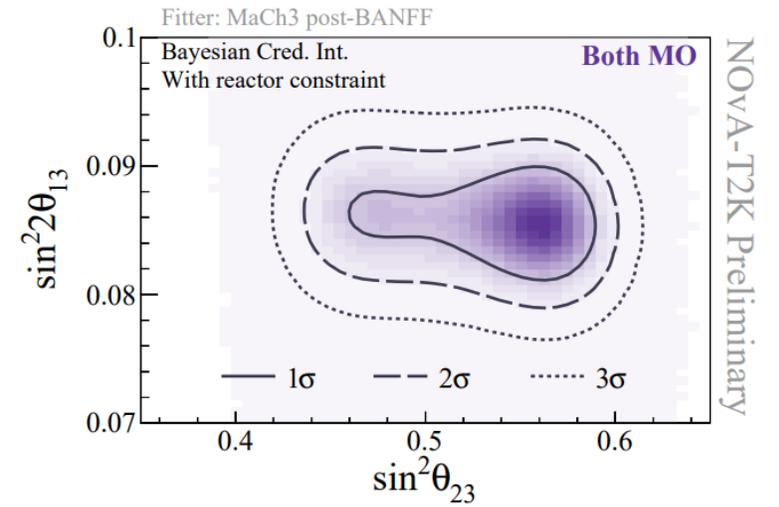
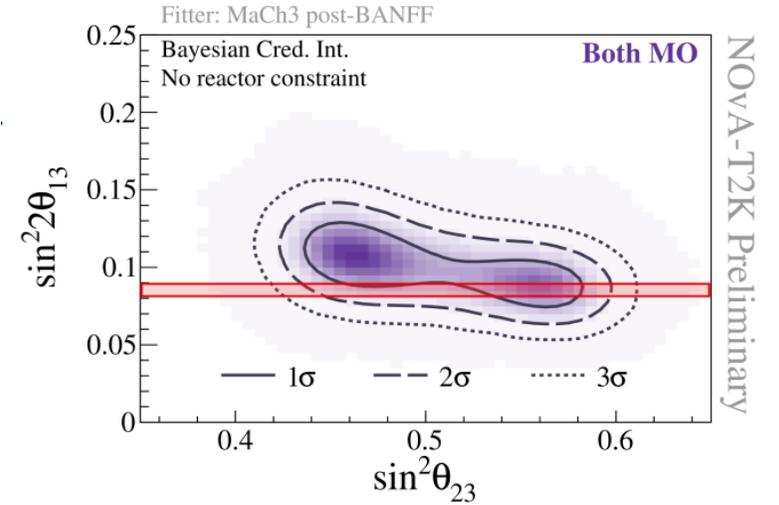
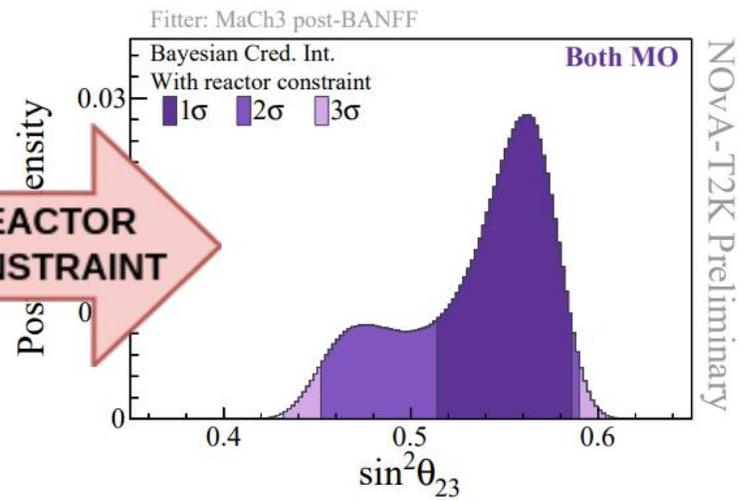
$\nu_e$  energy



$E_{\nu_e} = \text{quadratic function of } E_{\text{EM}} \text{ and } E_{\text{had}}$

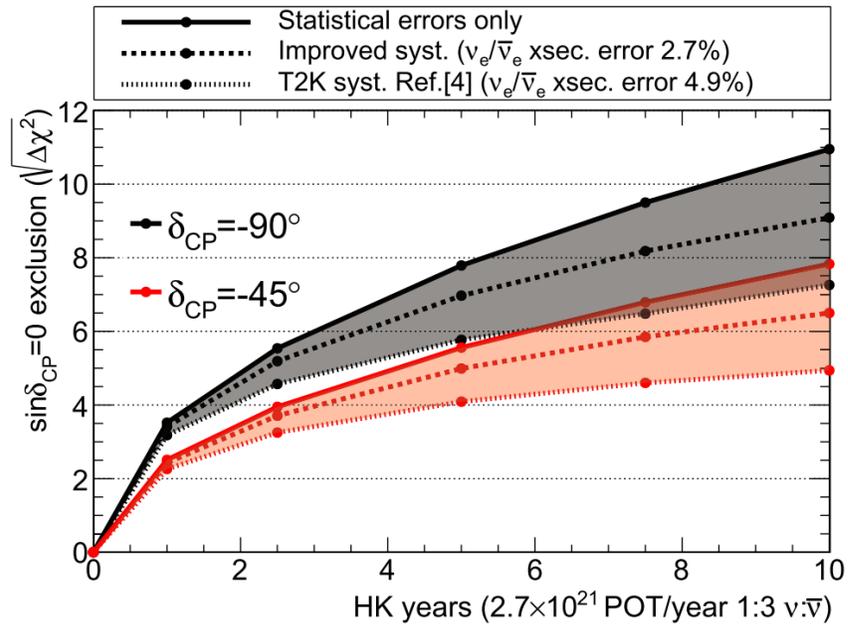


**REACTOR CONSTRAINT**



NOvA-T2K Preliminary

NOvA-T2K Preliminary

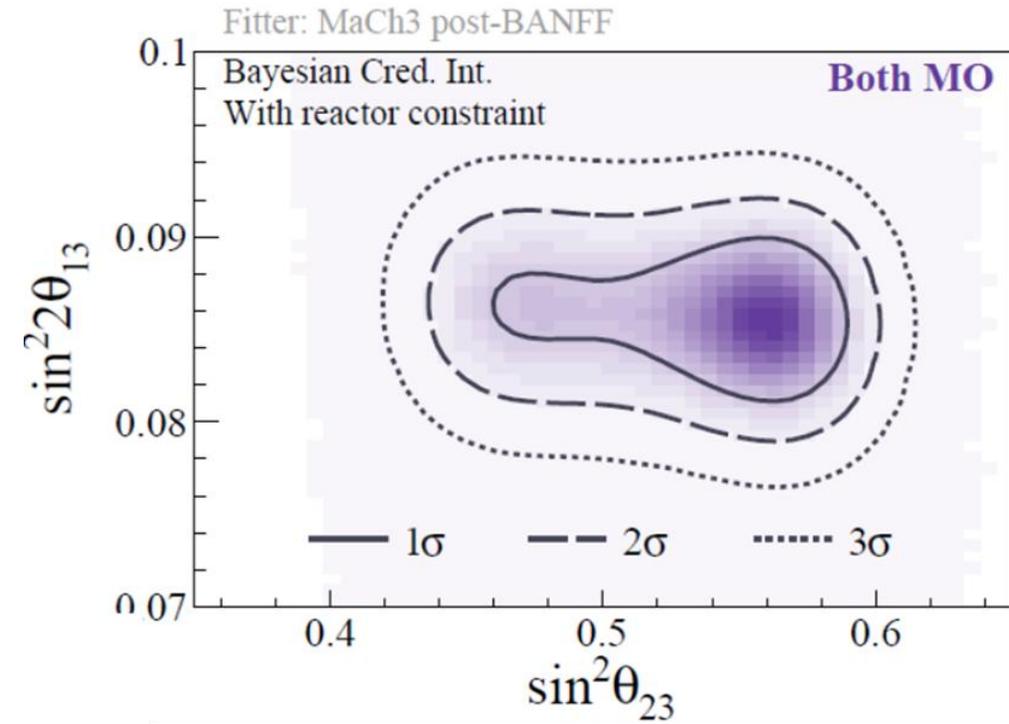


In the case of maximal CPV,  $\delta_{CP} = -\pi/2$ , Hyper-Kamiokande reaches a definitive  $5\sigma$  discovery in less than three years.

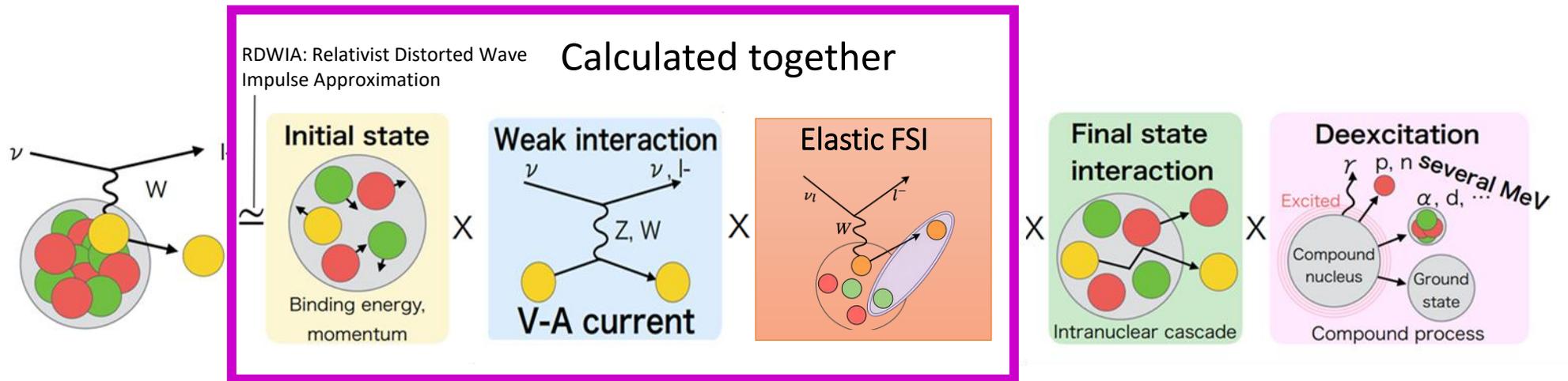
even with a very conservative assumption on the systematic uncertainties Hyper-Kamiokande will reach  $5\sigma$  sensitivity in less than 6 years.

If we consider the degenerate case of  $\delta_{CP} = -\pi/2$  and inverted ordering and the Hyper-Kamiokande sensitivity to MO using atmospheric and beam data, the CPV discovery would be delayed to 6 years also in the case of improved systematic uncertainties.

- Bayes factor of 3.6 for upper octant preference (modest) with RC
- Very weak preference for IO, Bayes factor 1.3



# Graph





# Meme

