

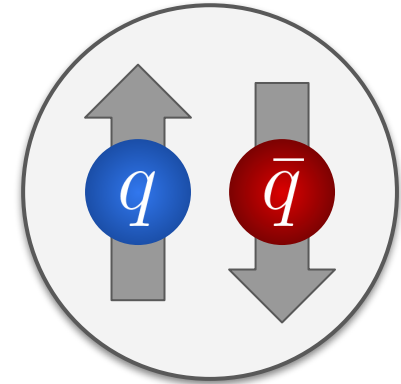
Meson Spectroscopy at Jefferson Lab

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Meson Spectroscopy

Experimental Meson Spectrum

Meson	M (Exp)
$\pi^+[u\bar{d}]_{J^{pc}=0^{-+}}$	139.57039 ± 0.00018
$\pi^-[d\bar{u}]_{J^{pc}=0^{-+}}$	139.57039 ± 0.00018
$\pi^0[(u\bar{u} - d\bar{d})/\sqrt{2}]_{J^{pc}=0^{-+}}$	134.9768 ± 0.0005
$\rho^+[u\bar{d}]_{J^{pc}=1^{--}}$	775.4 ± 0.4
$\rho^-[d\bar{u}]_{J^{pc}=1^{--}}$	775.4 ± 0.4
$\rho^0[(u\bar{u} - d\bar{d})/\sqrt{2}]_{J^{pc}=1^{--}}$	775.26 ± 0.23
$\omega[(u\bar{u} + d\bar{d})/\sqrt{2}]_{J^{pc}=1^{--}}$	782.66 ± 0.13
$K^+[u\bar{s}]_{J^{pc}=0^{-+}}$	493.677 ± 0.016
$K^-[s\bar{u}]_{J^{pc}=0^{-+}}$	493.677 ± 0.016
$K^0[d\bar{s}]_{J^{pc}=0^{-+}}$	497.611 ± 0.013
$\bar{K}^0[s\bar{d}]_{J^{pc}=0^{-+}}$	497.611 ± 0.013
$K^{*+}[u\bar{s}]_{J^{pc}=1^{--}}$	891.67 ± 0.026
$K^{*-}[s\bar{u}]_{J^{pc}=1^{--}}$	891.67 ± 0.026
$K^{*0}[d\bar{s}]_{J^{pc}=1^{--}}$	896.00 ± 0.025
$\bar{K}^{*0}[s\bar{d}]_{J^{pc}=1^{--}}$	896.00 ± 0.025



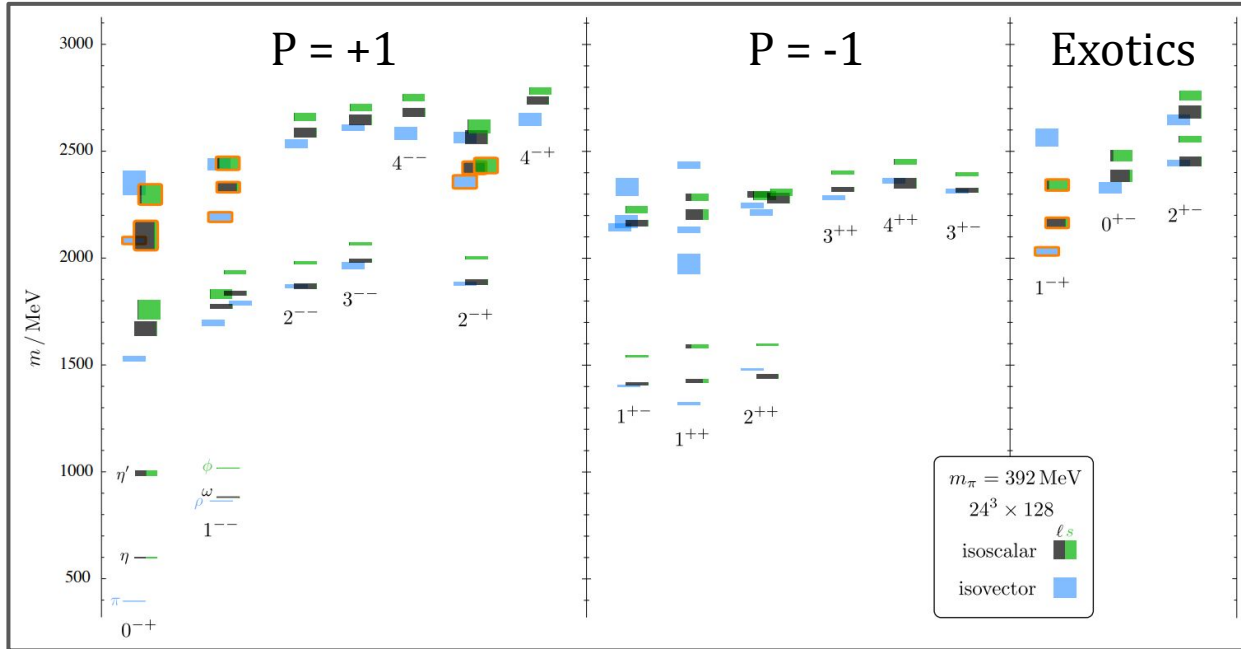
$$J = L + S$$

$$P = (-1)^{L+1}$$

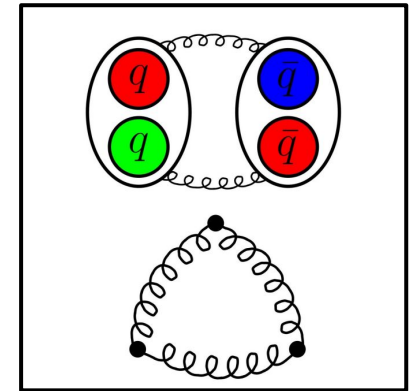
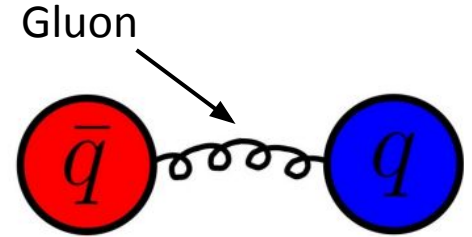
$$C = (-1)^{L+S}$$

Meson Spectroscopy

Lattice QCD Meson Spectrum



<https://arxiv.org/pdf/1909.06366>



Exotics

Meson Spectroscopy

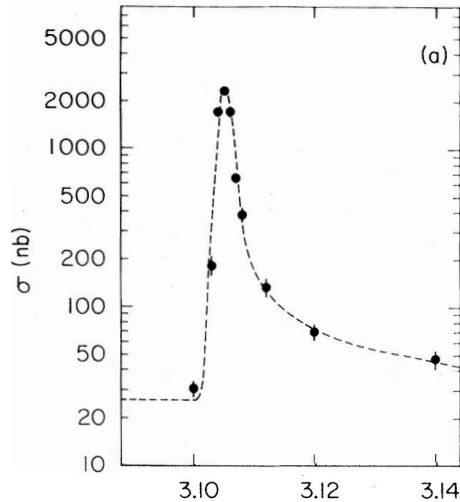


Meson spectroscopy objectives:

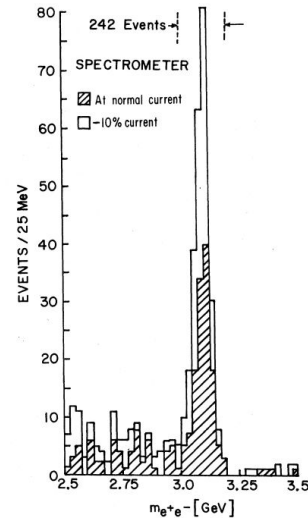
- Accurately determine properties of mesons
- Understand meson production and decay mechanisms
- Classify mesons
- Expand spectrum of known mesons
- Test predictions of lattice QCD
- Discover exotic mesons

Meson Spectroscopy

The November Revolution 1974

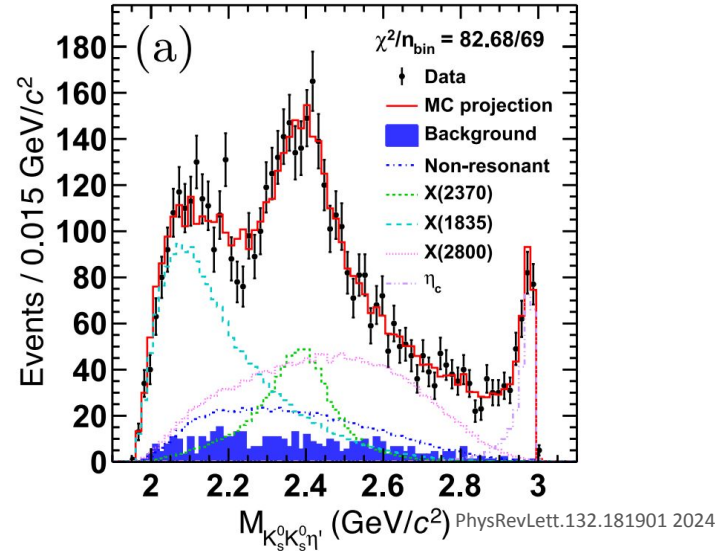


PhysRevLett.33.1406 1974 $E_{c.m.}$ (GeV)



PhysRevLett.33.1404 1974

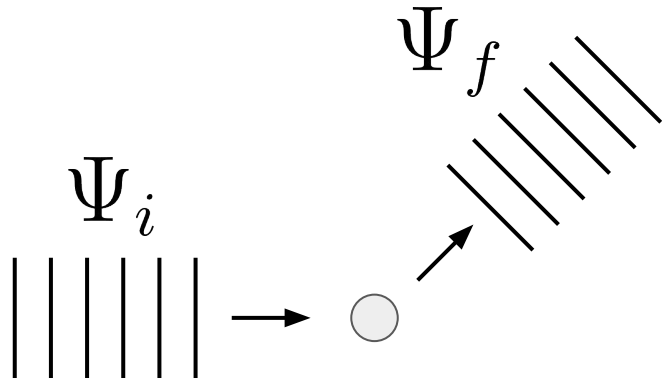
50 years on



$$J/\psi \rightarrow e^- e^+$$

$$X \rightarrow K_s^0 K_s^0 \eta'$$

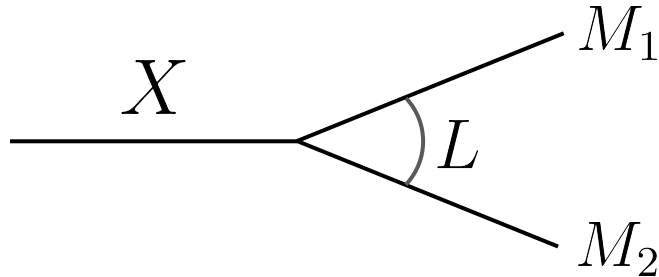
Partial Waves



$$\begin{aligned}\frac{d\sigma}{d\phi d\cos\theta} &= |\Psi_f - \Psi_i|^2 \\ &= \frac{1}{k^2} \left| \sum_{l=0}^{\infty} (2l + 1) T_l P_l(\cos\theta) \right|^2\end{aligned}$$

T_l are the amplitudes which correspond to the proportion of eigenstate with angular momentum l in the final state, these amplitudes are known as the partial waves

Partial Waves



Allowed X states:

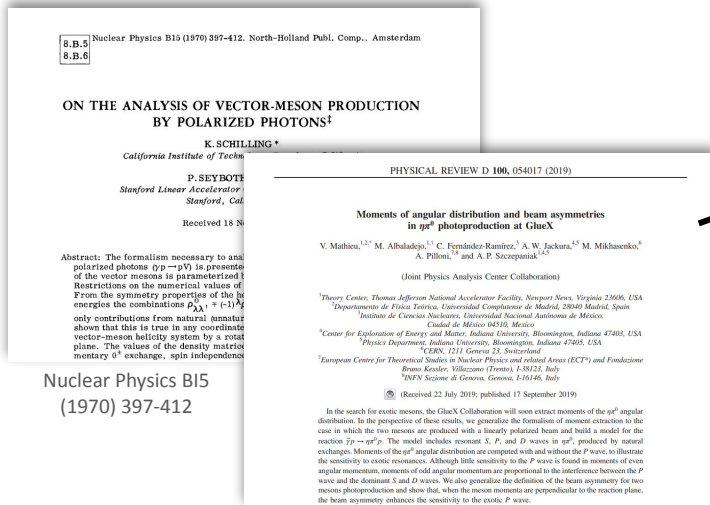
$\hat{S}_1 = \hat{S}_2 = 0, L = 0, 1, 2, \dots$
$J = L \quad P = C = -1^L$
$J^{PC} = 0^{++}, 1^{--}, 2^{++}, \dots$

For $l = 2$, the cross-section becomes,

$$\frac{d\sigma}{d\phi d\cos\theta} \propto T_0^2 P_0^2 + T_1^2 P_1^2 + T_2^2 P_2^2 + 2T_0 T_1 P_0 P_1 + 2T_1 T_2 P_1 P_2 + 2T_0 T_2 P_0 P_2$$

Reaction of Interest

- Polarisation is a fundamental property of the photon
- Understand role of polarisation in meson photoproduction



$$\frac{d\sigma}{dt dm_{KK} d\Omega d\Phi} \propto P_\gamma X \left| \sum_{l=0}^{l_{max}} T_m^l Y_l^m(\Omega) \right|^2$$

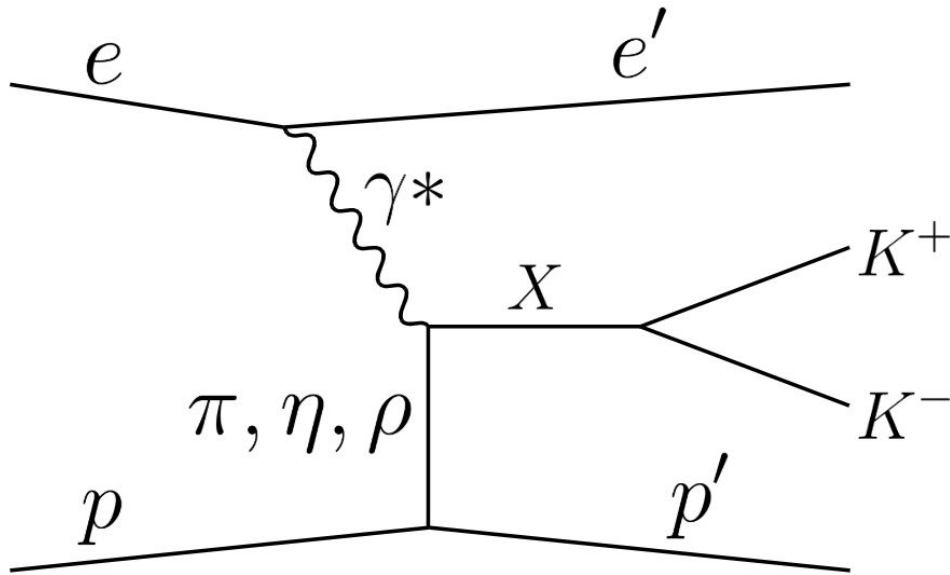
Photon linear polarization

$$X = \cos(2\Phi), \sin(2\Phi)$$

$\Omega = (\theta, \phi)$
Gottfried-Jackson frame

Reaction of Interest

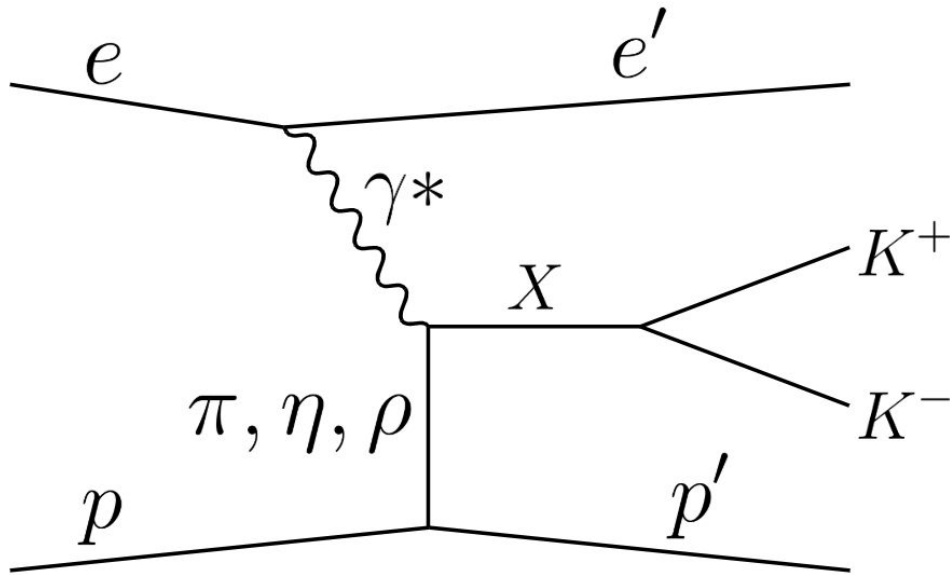
Reaction of interest: $ep \rightarrow ep' K^+ K^-$



- Photon (quasi-real) transfers momentum
- High degree of linear polarisation ($P_V > 70\%$)
- Pomeron exchange, access to various X quantum numbers

Reaction of Interest

Reaction of interest: $ep \rightarrow ep' K^+ K^-$



Cross-section:

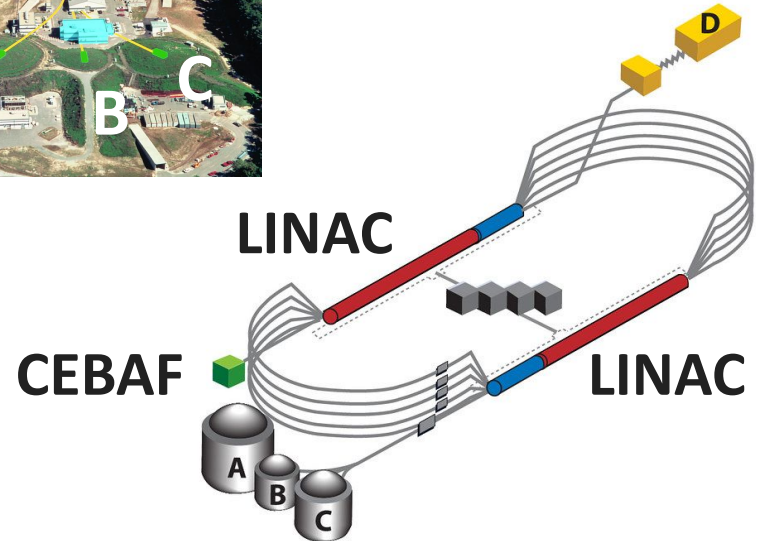
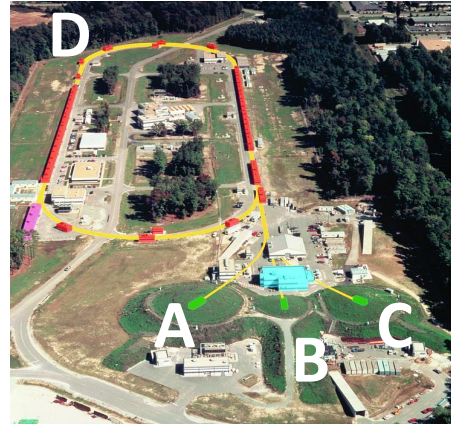
$$\frac{d\sigma}{dt dm_{KK} d\Omega d\Phi} \propto P_\gamma X \left| \sum_{l=0}^{l_{max}} T_m^l Y_l^m(\Omega) \right|^2$$

Allowed X states:

$$J^{PC} = 0^{++}, 1^{--}, 2^{++}, \dots$$

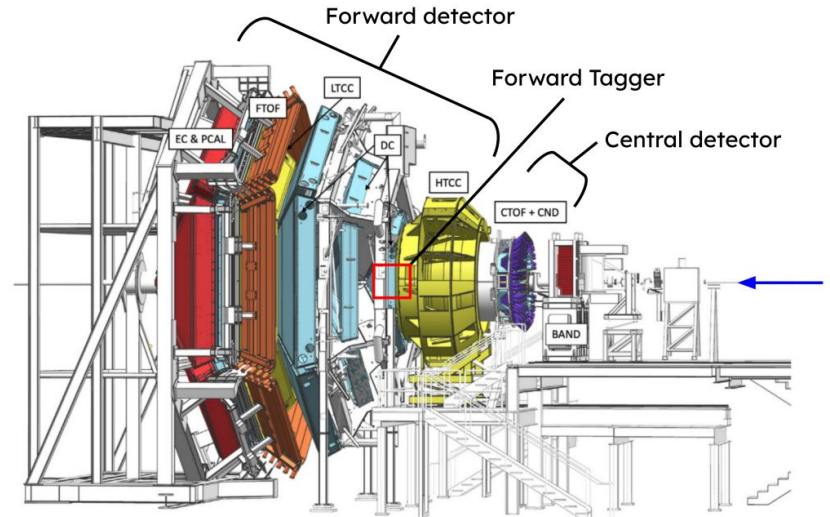
Jefferson Laboratory

- Multi-GeV electron beam
- High luminosity beam
- Spin polarised beam
- Four experimental halls



CLAS12

- Located in hall B
- Determination of 4-momenta of particles
- 2.5° to 125° acceptance



Experimental Data

Data was obtained under the following conditions:

- 10.2 GeV per electron
- Liquid hydrogen target

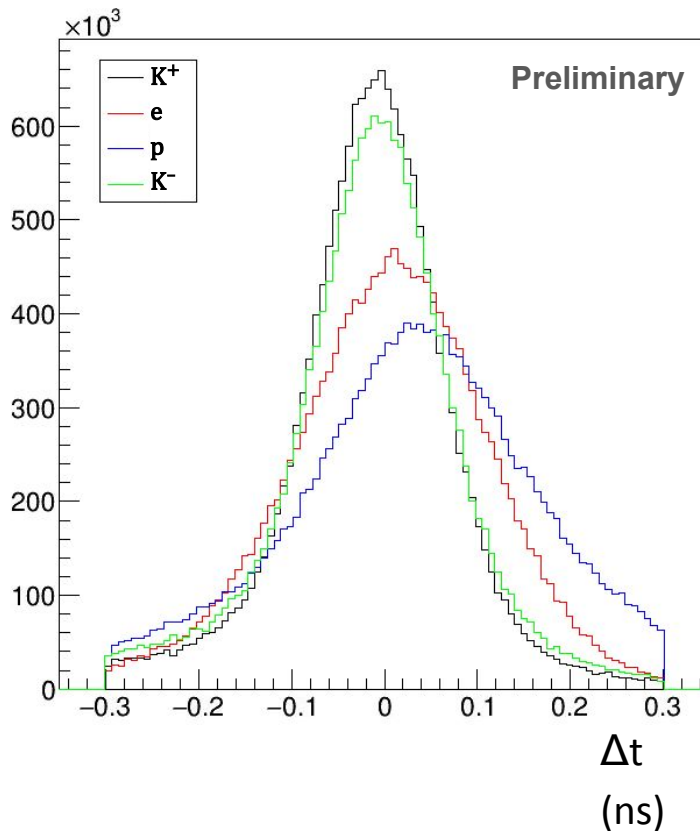
Obtaining events corresponding to the reaction of interest required:

- Event selection
- Reaction reconstruction

Event selection

Conditions:

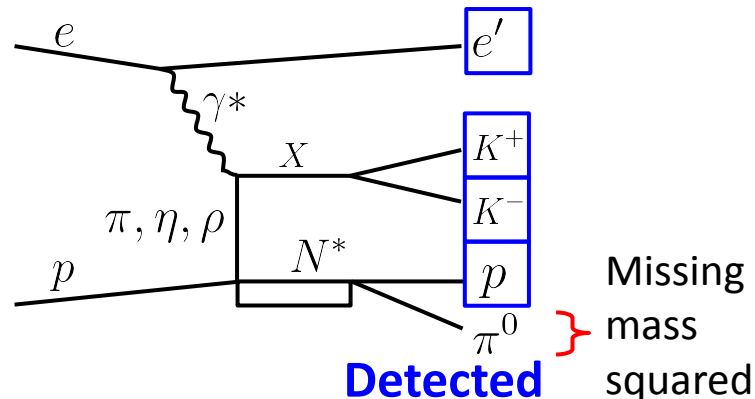
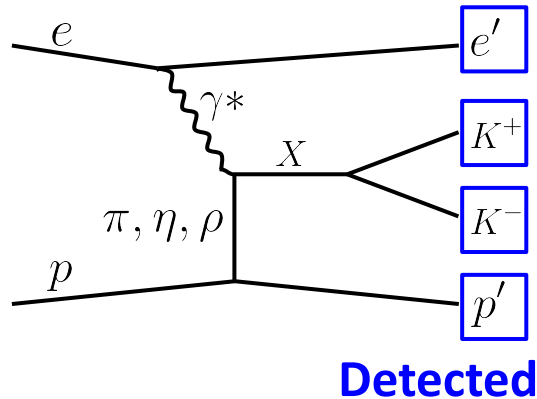
- Topology: epK^+K^-
- $\Delta t = |\text{TOF}_{\text{FTOF}} - \text{TOF}_{\text{DC}}| < 0.3 \text{ ns}$
- Scattered electron:
 - Forward Tagger
 - $0.4 < E < 5 \text{ GeV}$
- Kaons: Forward Detector



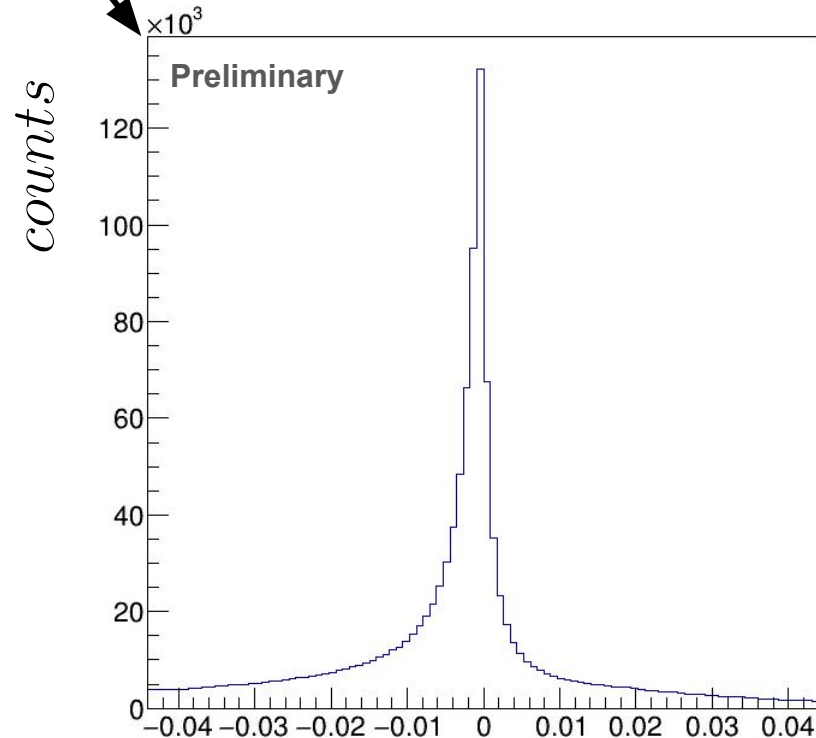
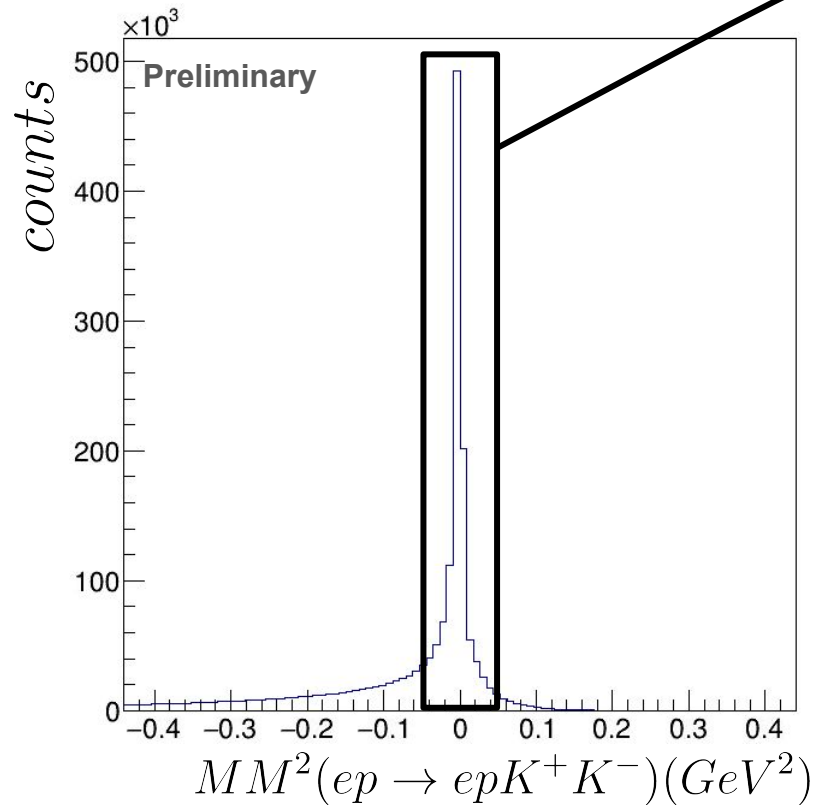
Reaction reconstruction

Missing mass squared of the event:

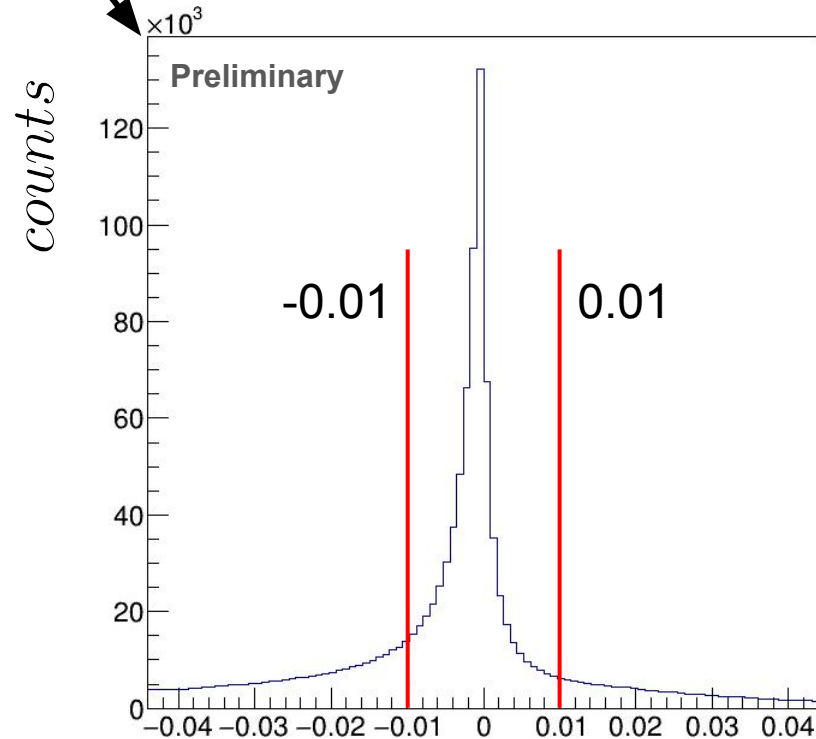
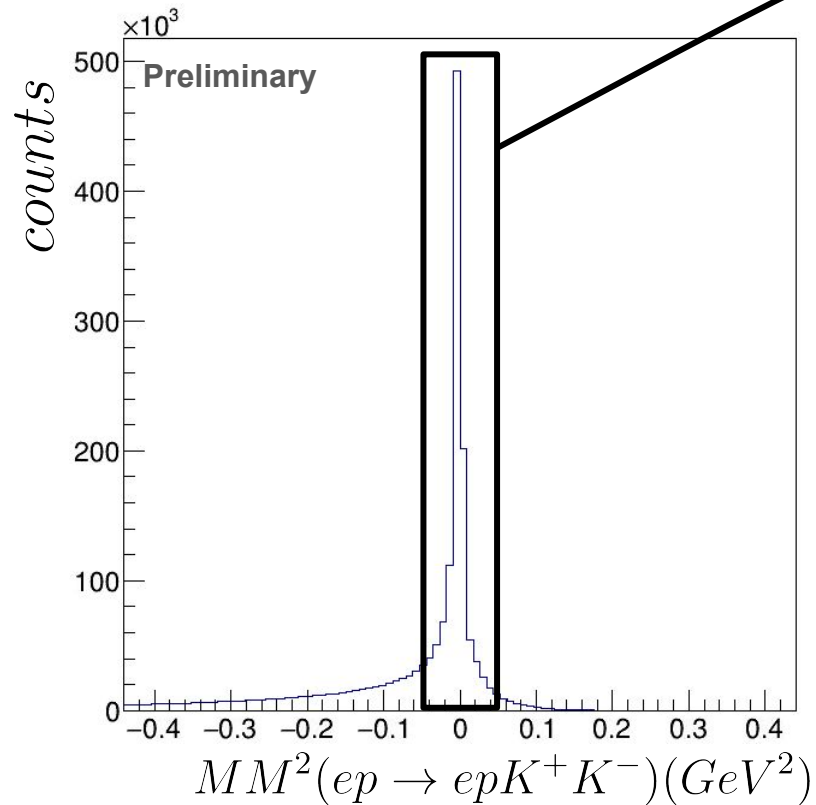
$$MM^2(ep \rightarrow e'pK^+K^-X) = |P_b + P_t|^2 - |P_{e'} + P_p + P_{K^+} + P_{K^-}|^2$$



Missing Mass



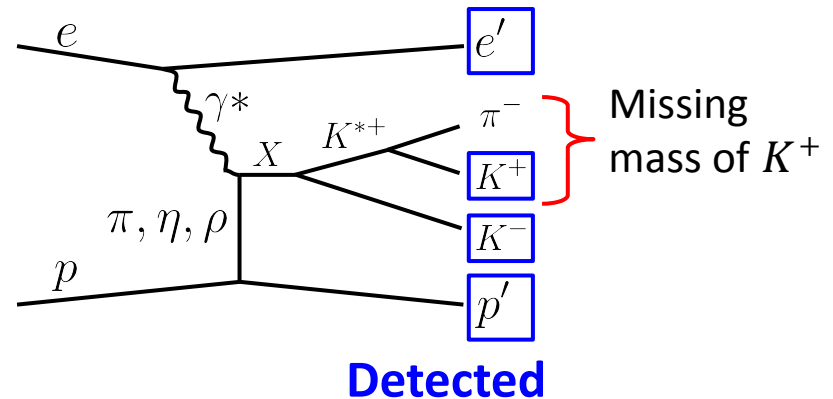
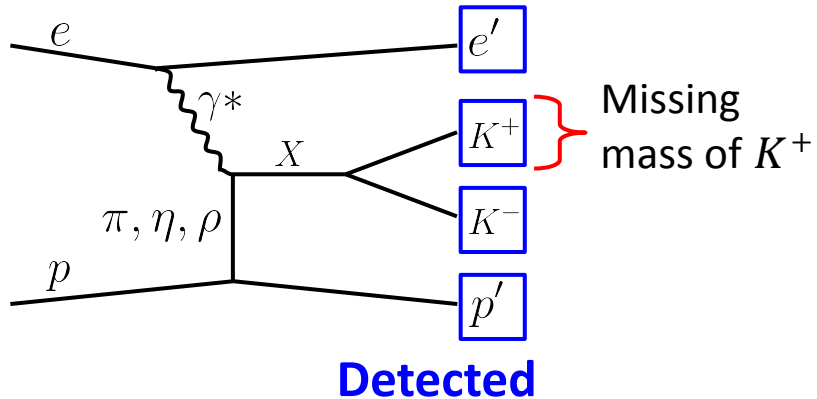
Missing Mass



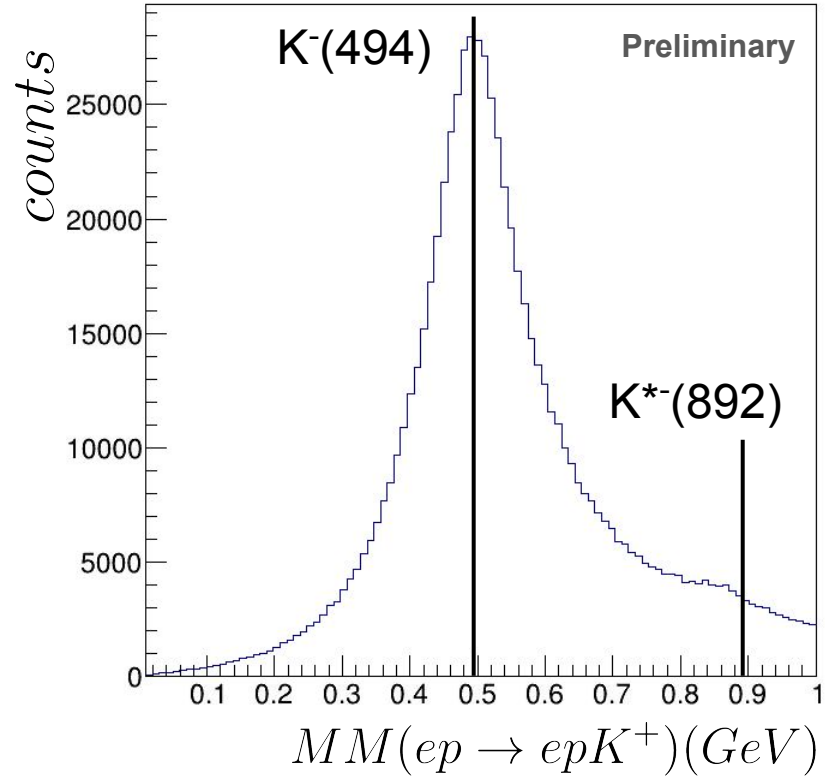
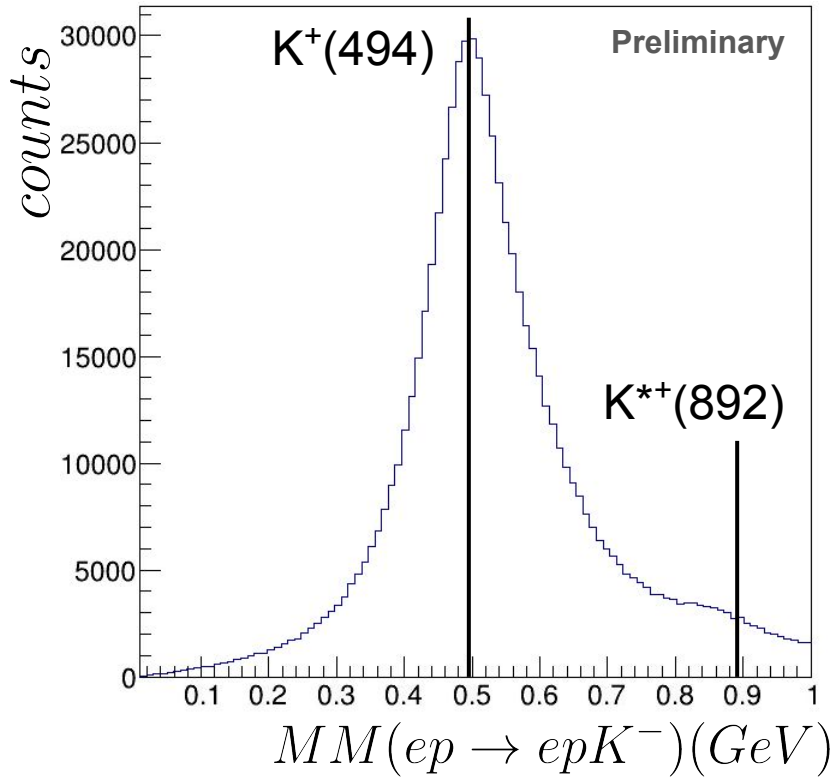
Reaction reconstruction

Missing mass of the kaons:

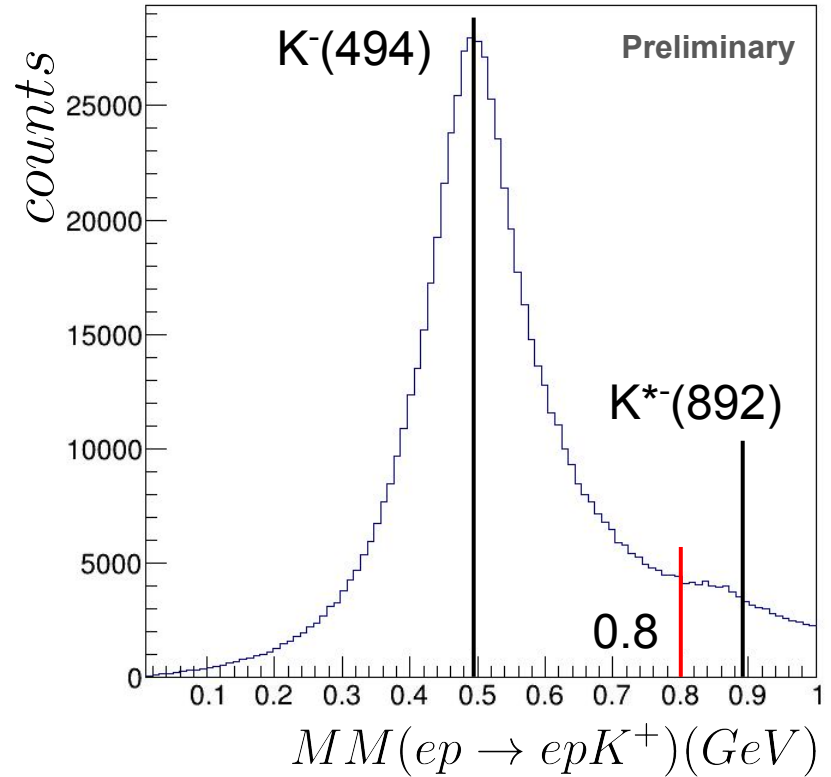
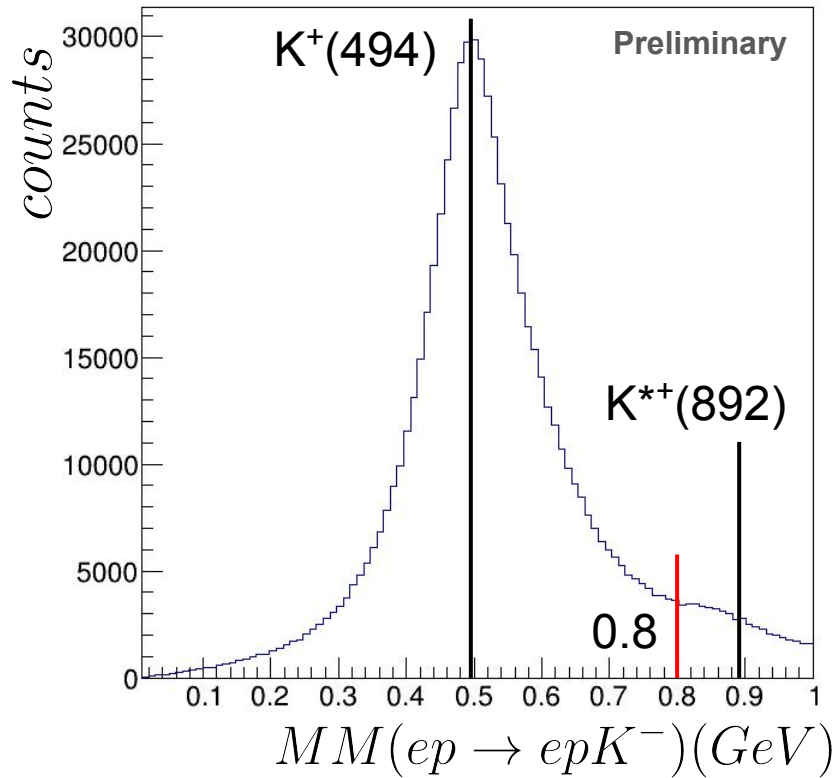
$$MM(ep \rightarrow e'pK^\pm X) = \sqrt{(|P_b + P_t|^2 - |P_{e'} + P_p + P_{K^\pm}|^2)}$$



Missing Mass



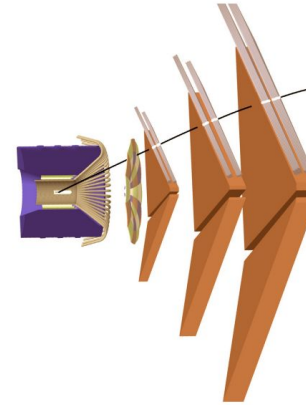
Missing Mass



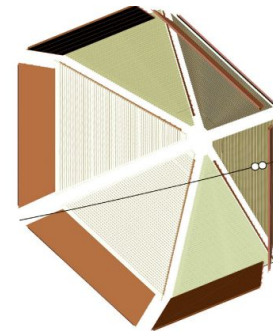
Simulations

Simulated data workflow:

- Created using Monte-Carlo event generator
- Passed through GEANT4 model of the detector
- Acceptances and efficiencies calculated
- Same event selection and reaction reconstruction was applied



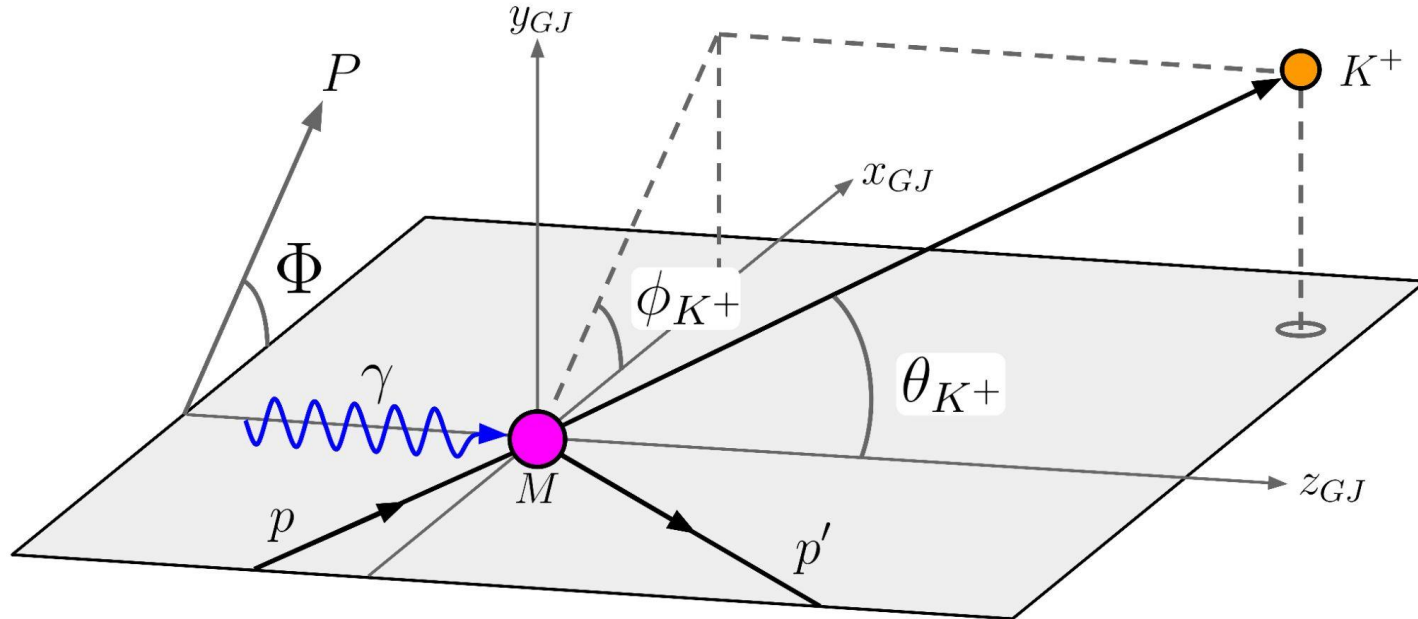
Drift
chambers



FTOF
system

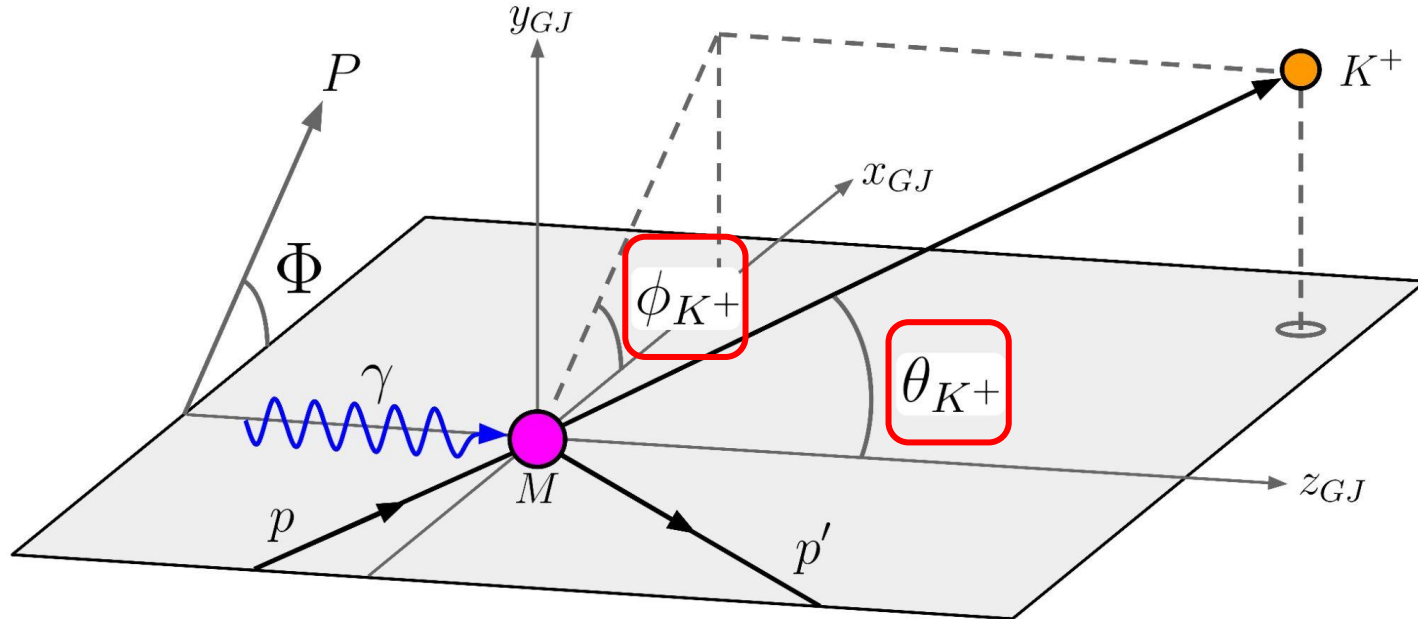
Angular distributions

Angular distributions in the Gottfried-Jackson frame were obtained.



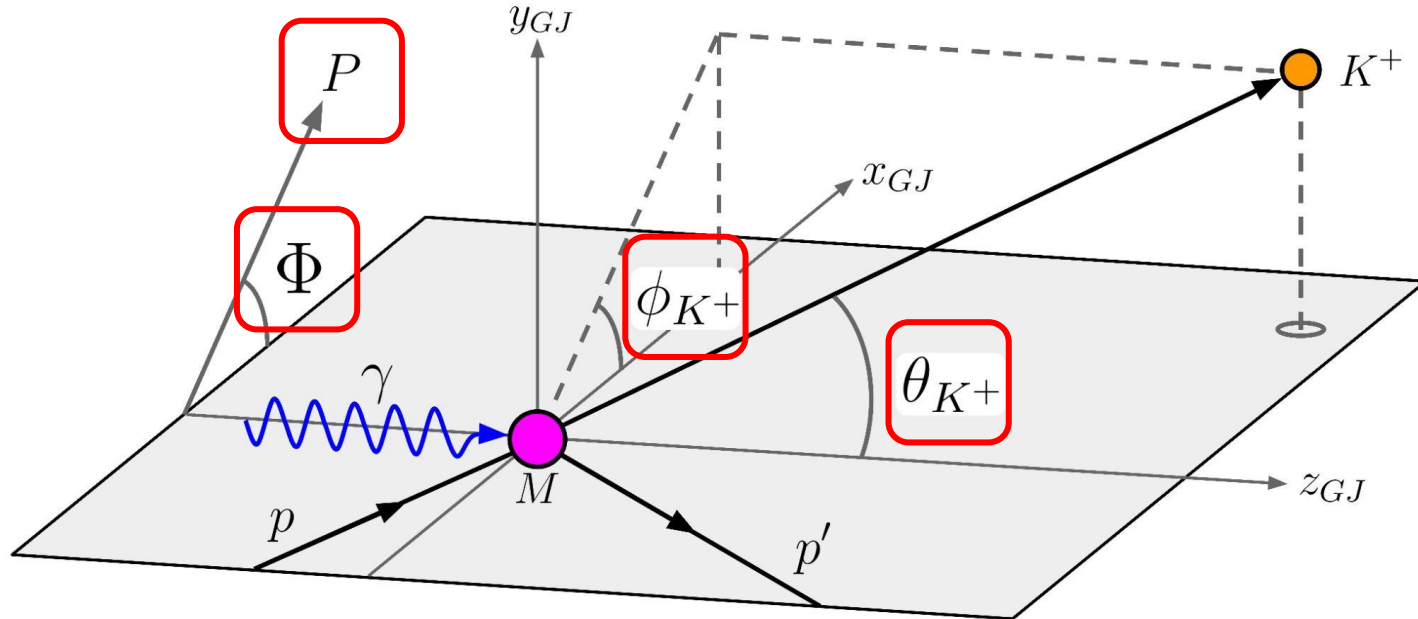
Angular distributions

Angular distributions in the Gottfried-Jackson frame were obtained.



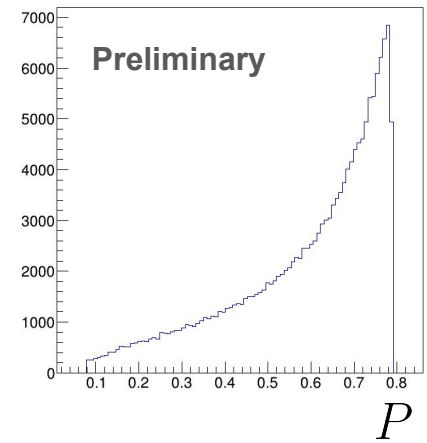
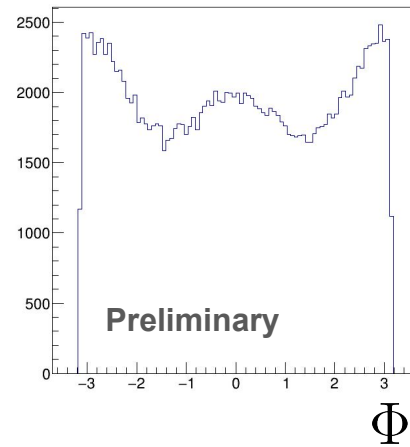
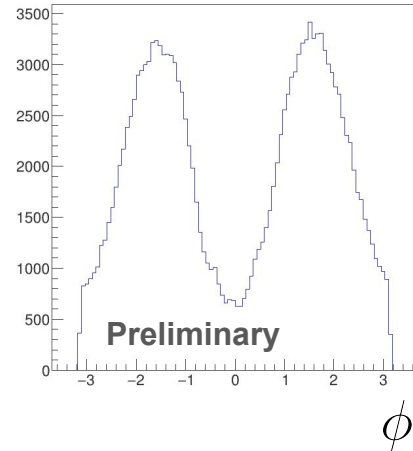
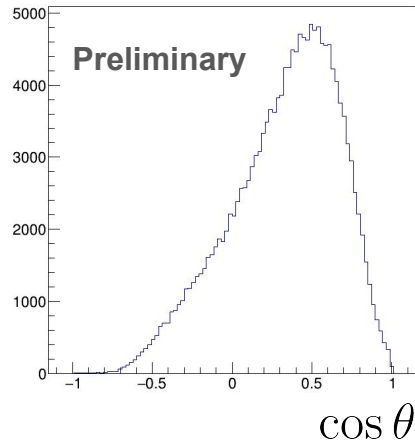
Angular distributions

Angular distributions in the Gottfried-Jackson frame were obtained.



Angular distributions

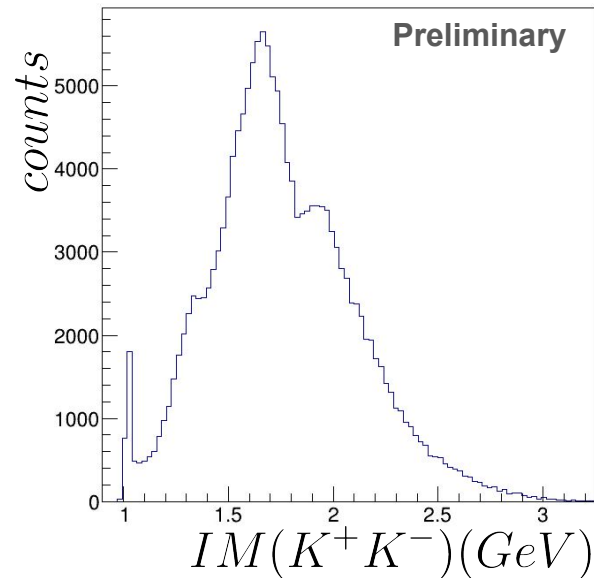
Gottfried-Jackson angular distributions and polarisation for experimental data.



Extracting Partial Waves

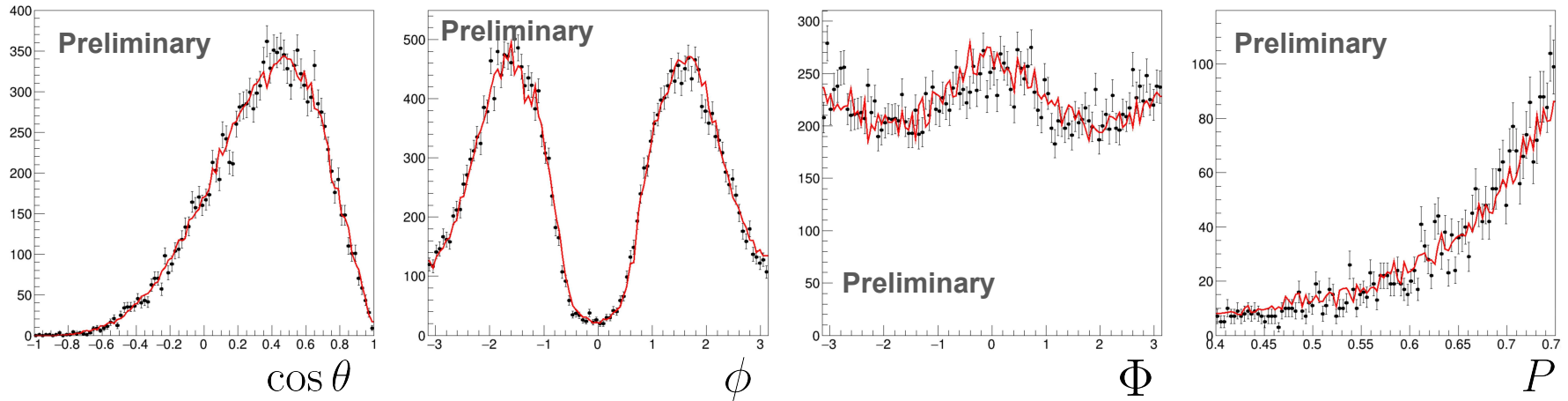
Partial waves were calculated using event-by-event maximum likelihood fitting and partial waves were acceptance- corrected.

Data were split into 40 K^+K^- invariant mass bins between 1.0 and 2.5 GeV. The partial waves were calculated independently in each bin.

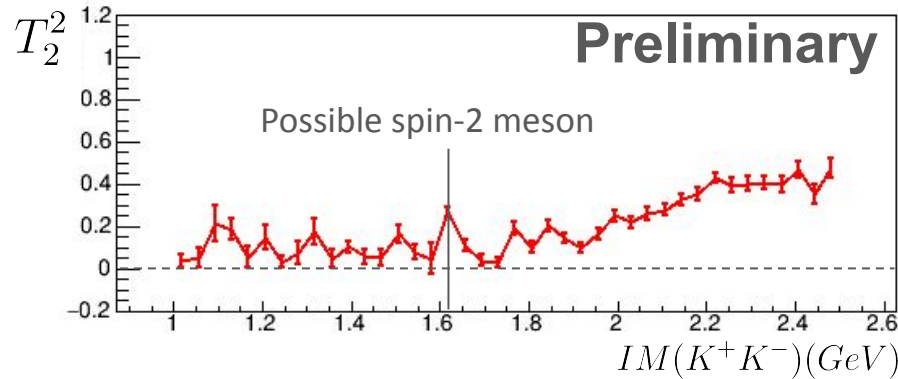
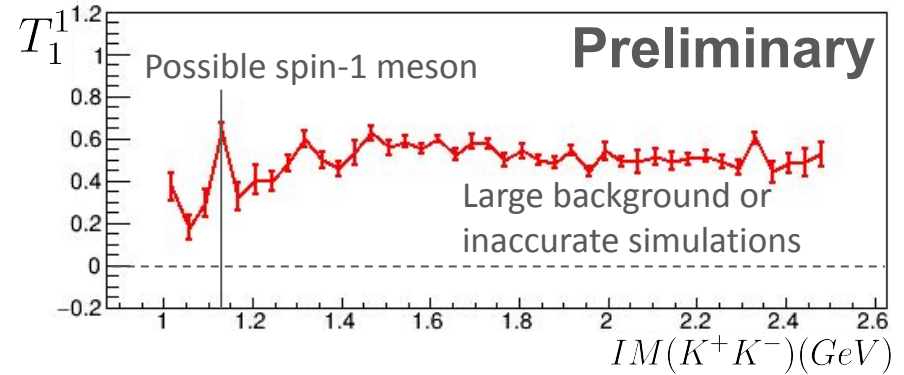
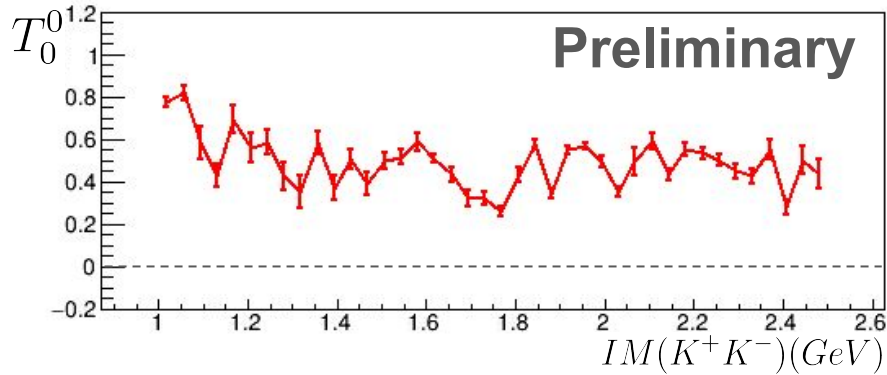


Extracting Partial Waves

Polarisation and angular distributions for experimental (black) and projection of fit for each variable (red).



Results



Outlook

Topics of future research:

- Improve accuracy of simulated data
- Systematic studies on all reaction reconstruction conditions
- Implementation of background removal
- Study of other reactions such as $ep \rightarrow ep'K^+K^-\pi^0$

Thank you for listening

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Reaction of Interest

$$\begin{aligned}
 I(\Omega, \Phi) &\equiv \frac{d\sigma}{dt dm_{KK} d\Omega d\Phi} = \kappa \sum A(\Omega) \rho^\gamma(\Phi) A^*(\Omega) \\
 &= I^0(\Omega) - P_\gamma I^1(\Omega) \cos 2\Phi - P_\gamma I^2(\Omega) \sin 2\Phi
 \end{aligned}$$

Amplitude (points to $A(\Omega)$)
 Polarisation matrix (points to $\rho^\gamma(\Phi)$)
 Polarisation (points to P_γ)

$$I^n(\Omega) \propto \sum A(\Omega) A^*(\Omega)$$

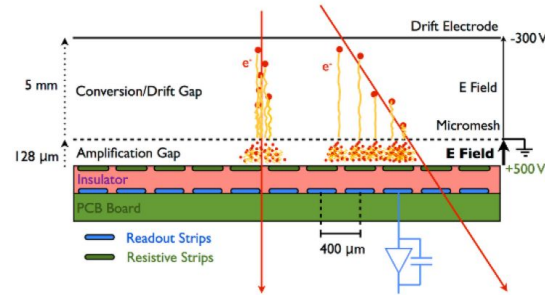
$$A(\Omega) = \sum T_m^l Y_l^m(\Omega)$$

$$\frac{d\sigma}{dt dm_{KK} d\Omega d\Phi} \propto P_\gamma \left| \sum_{l=0}^{l_{max}} T_m^l Y_l^m(\Omega) \right|^2$$

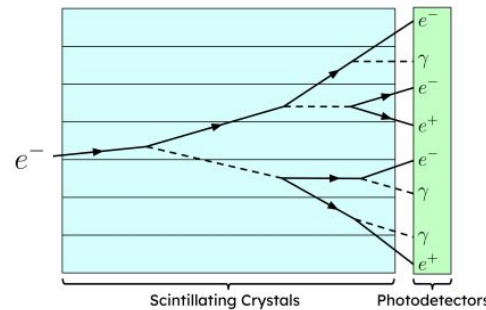
Partial waves

CLAS12

Micromegas gas tracker - determines vertex, momentum



Calorimeter - determines energy



$$M^2 = p_p^2 \cdot \frac{1 - \beta^2}{\beta^2}$$

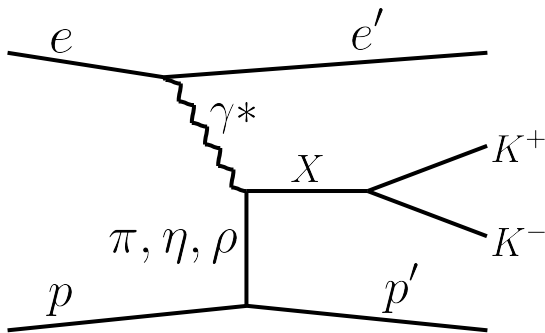
$$\beta = \frac{P_L}{t_p c}$$

p_p - particle momentum
 P_L - particle path length
 t_p - flight time over P_L

Missing mass

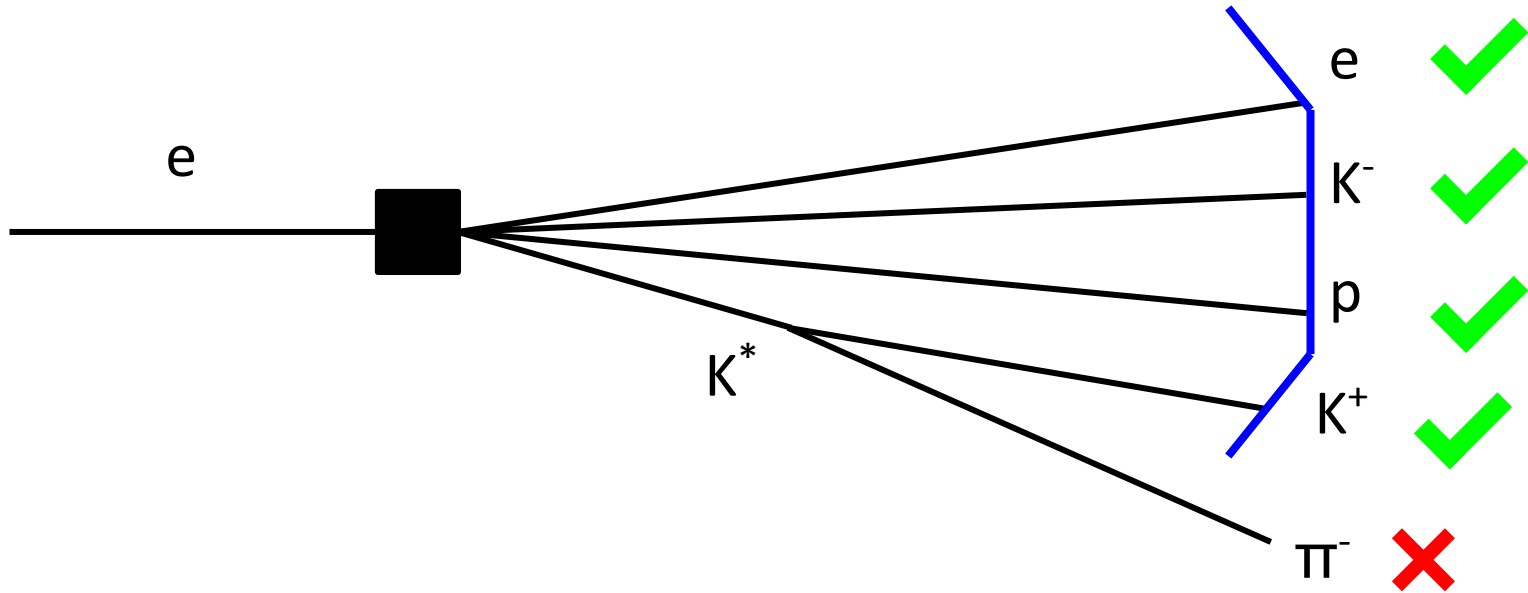
The missing mass squared of the reaction is given by:

$$\begin{aligned}
 MM^2(ep \rightarrow e' p K^+ K^- X) &= |P_b + P_t|^2 - |P_{e'} + P_p + P_{K^+} + P_{K^-}|^2 \\
 &= (E_b + m_t - E_{e'} - E_p - E_{K^+} - E_{K^-})^2 \\
 &\quad - |\bar{p}_b + \bar{p}'_e - \bar{p}_p - \bar{p}_{K^+} - \bar{p}_{K^-}|^2
 \end{aligned}$$



Missing mass

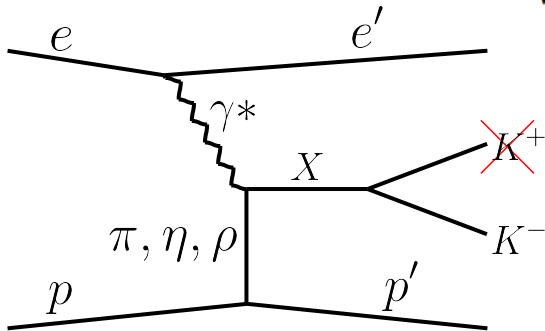
An example:



Missing mass

The K^+ missing mass is given by:

$$\begin{aligned}
 MM(ep \rightarrow e'pK^-X) &= \sqrt{|P_b + P_t|^2 - |P_{e'} + P_p + P_{K^-}|^2} \\
 &= \sqrt{(E_b + m_t - E_{e'} - E_p - E_{K^-})^2 - |\bar{p}_b + \bar{p}_{e'} - \bar{p}_p - \bar{p}_{K^-}|^2}
 \end{aligned}$$



Angular distributions

Angular distributions in the Gottfried-jackson frame were obtained.

$$P = \left[1 + 2 \frac{Q^2 + v^2}{Q^2} \tan^2 \left(\frac{\theta_{e'}}{2} \right) \right]^{-1}$$

$$Q^2 = 4E_b E_{e'} \sin^2 \left(\frac{\theta_{e'}}{2} \right)$$

